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#### Abstract

Art. XXVII.- On the Morphological Laws of the Configurations formed by Magnets floating vertically and subjected to the attraction of a superposed magnel; with notes on some of the phenomena in molecular structure which these experiments may serve to explain and illustrute; by Alfred M. Mayer.


In the April and June numbers of this Journal (pages 276 and 477 of vol. xv), I published short notes on my experiments with magnets floating vertically and subjected to the attraction of a superposed magnet. The object of this paper is to present accurate diagrams of the configurations formed by the floating magnets and to give the laws ruling these configurations, with some notices of the peculiarities of these forms. At the same time I will show how neatly these experiments illustrate several phenomena in the molecular structure of matter.

The Diagrams.* - These diagrams show the configurations formed by numbers of magnets extending from two to twenty. They were obtained as follows: the number of needles forming a configuration were floated in a bowl filled to its brim with water. The eye ends of the needles, which protruded a short distance beyond the tops of the corks, were of S . polarity. A cylindrical magnet, $38^{\mathrm{cm}}$ long and $15^{\mathrm{mm}}$ in diameter, was clamped in a vertical position, with its N . end at the constant distance of 60 millimeters above the tip of the needle which floated in the line of the axis of the magnet. I tipped the ends of the needles with printer's ink, and when the configuration had formed and was stationary, I brought down upon the needles a piece of flat card-board, and thus obtained prints

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from nature. Around each of the dots on the card-board I drew a black disk. The centers of these disks I joined by lines, in order to bring before the eye the contours of the configurations. After the diagrams of the configurations had been obtained in this way they were placed at a fixed distance from the camera, and photo-engravings were thus made of about one half the sizes of the original prints.

The Morphological Laws of the Configurations.-The configurations made by the floating magnets form well marked groups or classes, which may be designated in order as primary, secondary, tertiary, quaternary, etc. The stable configurations of one class form the nuclei to the succeeding ones.

Looking at the diagrams the reader will see that figures 2 to $8 a$ inclusive form the primaries. Figure $8 b$ begins the secondaries, for it is the hexagon with 2 for nucleus. Configurations $8 b, 8 c$, $9,10 b, 10 a, 11,12,13,14,15,16,17,18 a, 18 b$ and $19 a$ are secondaries, having respectively for nuclei the primaries $2,2,2,2$, $3,3,4,4,5 a, 6 a, 7,7,7,8 a, 8 a$. The configuration $10 b$ is not found in the diagrams; it is the same as the 10 which forms the nucleus of 20 , only the two central lateral needles are further removed outward from the vertical axis of the fig. 10.

The group of $19 b$ begins the tertiaries. Of these I do not give diagrams, but indicate their structure by giving the numbers of the secondaries forming their nuclei and then give the numbers of needles grouped around these nuclei. Thus, the structure of the configuration formed of 47 needles is indicated by $47=(18+14)+15$; which means that 47 needles form a configuration which has 18 for its inner nucleus, surrounded by 14 needles, and these in turn surrounded by 15 ; and as $18+14$ forms the tertiary which is the nucleus to this quaternary 47 , we inclose 18 and 14 in parenthesis.

I here give the configurations to 51 inclusive, which form begins the quinaries.

The configurations of the same number of magnets are lettered $a, b, c$, to indicate their degrees of stability; $a$ being always the most stable form. I have, however, lettered the configuration of 8 magnets in the order of their increasing areas in order to make them serve better for the purpose of illustrating the phenomena of isomerism. Really, $8 c$ is more stable than $8 b$.

## Tertiaries.

| $19 b=9+10$ | $25 a=12+13$ | $29 b=17+12$ |
| :--- | :--- | :--- |
| $20 a=9+11$ | $25 b=13+12$ | $30 a=17+13$ |
| $20 b=10+10$ | $26 a=13+13$ | $30 b=18+12$ |
| $21 a=10+11$ | $26 b=14+12$ | $31=18+13$ |
| $21 b=11+10$ | $27 a=14+13$ | $32=18+14$ |
| $22=11+11$ | $27 b=15+12$ | $33=18+15$ |
| $23=11+12$ | $28 a=15+13$ | $34 a=(8 a+12)+14$ |
| $24 a=12+12$ | $28 b=16+12$ |  |
| $24 b=11+13$ | $29 a=16+13$ |  |


| Quaternaries. |  |  |
| :---: | :---: | :---: |
| $34 b=(9+10)+15$ | $40=(13+13)+14$ | $47=(18+14)+15$ |
| $35 a=(9+12)+14$ | $41=(13+13)+15$ | $48=(18+15)+15$ |
| $35 b=(10+12)+13$ | $42=(13+14)+15$ | $49=(18+15)+16$ |
| $36=(10+12)+14$ | $43=(15+14)+14$ | $50=(8+11+15)+16$ |
| $37=(10+13)+14$ | $44=(15+14)+15$ | $51 a=(8+12+15)+16$ |
| $38=(11+13)+14$ | $45=(16+14)+15$ |  |
| $39=(11+13)+15$ | $46=(18+14)+14$ |  |
|  | Quinaries. $51 b=(9+12+14)+$ |  |

I do not say that the above list contains all the possible combinations. The list is more for the purpose of establishing the laws which I have already formulated.

In my first publication I gave two configurations for four needles; one having the needles at the corners of a square, and a stable form ; the other unstable and formed of a triangle containing a central needle. I have concluded that this form does not exist ; at least, its existence is so transient that it has never remained long enough for me to take a print of it.

I bave stated that $19 b$ begins the tertiaries. This is an unstable configuration, and is formed of 9 surrounded by 10 magnets. The other $19,19 a$, is stable, and is formed of $8 a$ surrounded by 11 magnets. It is to be remarked that not alone the tertiaries but the configurations in the other classes begin with an unstable group of magnets. Thus, $8 c$ begins the secondaries, $19 b$ the tertiaries, $34 b$ the quaternaries, and $51 b$ the quinaries.

The reader has seen that a given number of magnets may form two or more different configurations. Thus, five magnets form two, $5 b$ a square with a magnet at its center, and $5 a$ a pentagon. Six magnets give $6 a$ and $6 b$. With eight magnets we obtain three configurations, $8 a, 8 b$, and $8 c$. Now the different configurations formed of the same number of magnets always exhibit different degrees of stability. Vibration of the less stable forms (produced by alternately lifting and lowering the superposed magnet) sends them into the stable forms. Thus, $5 b$ on vibration rearranges itself into $5 a ; 6 b$ into $6 a$; and $8 c$, or $8 b$, into $8 a$. With the configurations of higher classes (the tertiaries, quaternaries, etc.), even a knock on the table is sufficient to cause the needles of the unstable configuration to move to positions of stable equilibrium.

On looking at the diagrams it will be observed that only the stable primaries form the nuclei of the secondaries, and, moreover, those primaries which are not dimorphous, like $2,3,4$ and 7 , serve as nuclei to more than one secondary. Thus, 2 is the nucleus of $8 a, 8 b, 8 c, 9$ and $10 b: 3$ is the nucleus of $10 a$ and 11 ; and 7 is the nucleus to 16,17 and 18 ; while each of the other stable and dimorphous primaries, $5 a, 6 a$ and $8 a$,
appears only once, as nucleus respectively to 14,15 and $18 b$. This same power of the most stable nuclei to resist outside stress is shown in the configurations of the tertiary and quaternary classes, where the secondary 11 appears as nucleus to 21,22 , 23 and 24 . The secondary $18 a$ persists in even a more marked manner as a nucleus. This $18 a$ has the contour of that very stable 7 (the only configuration possible with 7 magnets), which forms its nucleus. Among the tertiaries $18 a$ is the nucleus of $30 b, 31,32$ and 33 , while in the quaternaries it forms the inner nucleus of $46,47,48$ and 49 . The fact of the persistence of these stable forms as nuclei may be suggestive to chemists and crystallographers.
It is here to be remarked that (as a general rule holding good in all the classes) of two configurations made up of the same number of magnets, that configuration is the more stable which has the least number of needles for its nucleus.

Illustrations of Molecular Structure. (1.) Unstable Molecular Equilibrium. -That the molecules in a body may be in a state of unstable equilibrium, so delicately balanced that a slight extraneous action of pressure, of heat, light, etc., may cause a new molecular arrangement in the body, is shown in many facts. A few of the more familiar ones will answer for our purpose. Thus, quiet water, which remains liquid at a temperature of $10^{\circ} \mathrm{C}$., or more, below $0^{\circ} \mathrm{C}$., changes suddenly into ice when agitated ; and during this solidification its temperature rises. In like manner a supersaturated solution of disodium sulphate solidifies when a crystal of this substance is dropped into it. Another instance of a sudden change from an unstable to a stable molecular condition is shown when the yellow crystals of mercuric iodide change, on the touch of a glass rod, to a scarlet color with a perceptible motion of their particles. These and similar phenomena are illustrated by the change of unstable to stable configurations caused by vibration, shock, and varying conditions of stress. Thus, $5 b$ changes into $5 a ; 6 b$ into $6 a$; and $8 c$ and $8 b$ into $8 a$.
(2.) Illustrations of the Expansion on Solidification, as shown by water, bismuth, antimony, cast-iron, etc., are readily given by the floating magnets. One volume of water at $0^{\circ} \mathrm{C}$. expands on freezing into about one and one-tenth volume of ice. It happens that the area of $5 b$ is greater than the area of $5 a$ by about one-tenth; so that the increase in area which takes place when the pentagon of $5 a$ is changed into the square $5 b$ may represent the increase in the volume of water when it changes into ice.

It will be observed, on an examination of the diagrams, that of two configurations, formed of the same number of needles, that configuration which has the larger area has a magnet in its
center. Thus, $5 b$ exceeds in area $5 a$, and $6 a$ is of greater area than $6 b$. To see the effect of a repulsive center on a configuration, compare the areas of the two squares 4 and $5 b$, and of the two pentagons $5 a$ and $6 a$. The most marked effect of a repulsive central magnet is seen on comparing 14 with 15 . The outside contour of each is formed of 9 magnets. The nucleus of 14 is the peculiar flattened pentagon, which is expanded into symmetry on the addition of another magnet, while at the same time the outside contour of 15 conforms to the regular pentagonal nucleus. These phenomena are so suggestive that I make bold to put the question: may it not be that there is an actual centralization of atoms in the molecule when a body expands in solidifying, and in the case where of two or more isomeric bodies one has always the minimum density? I offer this as a suggestion which may be worthy of the consideration of crystallographers.
(3.) Illustrations of Allotropy and Isomerism.-The most interesting of our experiments with the floating magnets are those illustrating the phenomena of allotropy and isomerism. It is well known that an elementary substance may exist under very different forms. By the action of heat, electricity, etc., an element may have its physical and chemical properties so changed that no one would suppose that the different bodies thus made out of one and the same element were really all of the same substance; yet the body remains elementary under the different appearances, for it is impossible by any means of subtraction to get anything but the elementary substance from it. Phosphorus, sulphur and carbon give instances of allotropy. Thus graphite and the diamond are both carbon, yet how different are they. One is soft, opaque, black, and with a metallic luster; the other is the hardest of bodies, transparent, and resplendent by its refractive action on light. Graphite is a good conductor of electricity ; crystallizes in small six-sided tables which belong either to the hexagonal or monoclinic system, and have a specific gravity of $2 \cdot 2$; while the diamond is a bad conductor of electricity, crystallizes in the monometric system, and has a specific gravity of 3.5 . Whenever an element or a compound takes two different crystal forms, these different crystals always differ in their density.

These differences of form and density shown in allotropy and isomerism are well illustrated in the configurations which are formed of the same number of magnets. Take figures $5 a$ and $5 b$. The first is a pentagon. The second is a square with a magnet in its center. The forces in these floating magnets and in the superposed magnet remain the same in all the configurations, and these have all been printed from needles floated in water whose surface was at a constant perpendicular distance
from the pole of the superposed magnet. Thus we see how the same atoms endowed with forces of the same strength, may take different relative positions, and thus produce very different crystal-forms in the same matter. We may take $5 a$ for an illustration of the atomic arrangement in the diamond, while $5 b$ may stand for graphite. But there is always a change of density accompanying the different forms in allotropy, and this fact is also illustrated by configurations $5 a$ and $5 b$. In bodies formed of the same kind of elementary atoms, as in allotropy, it is evident that their relative densities will be directly as the number of atoms contained in the unit of volume. As our configurations illustrating allotropy contain the same number of magnets, it follows that the relative densities of these configurations are inversely as their areas. Now the area of $5 \alpha$ (measured on the original prints) is 818 square millimeters, and the area of $5 b$ is 992 square millimeters, hence the density of $5 a$ is to the density of $5 b$ as 992 is to 818 . Thus we see bow the arrangement of magnets in $5 a$ may stand for the molecular structure in the diamond while $5 b$ may stand for that in graphite.

Numerous instances exist in chemistry of the same elements combined in the same porportions, yet producing bodies crystallizing in different forms, and having different densities, color, transparency, hardness, etc. As examples of this phenomenon of isomerism we may cite calcium carbonate, which crystallizes in two forms differing in density, viz: as calc spar of a specific gravity of 2.72 , and as aragonite of a specific gravity of 2.93 . Configuration $6 a$ may stand for the molecular structure of calc spar, while $6 b$ may stand for that of aragonite. The relative densities of these two configurations are as 208 to 247.

A striking example of isomerism is given in titanic acid, which crystallizes in three distinct forms: as anatase, specific gravity 3.82 ; as brookite, specific gravity 4.02 ; and as rutile, specific gravity $4 \cdot 25$. These three isomers may be illustrated by $8 c, 8 b$ and $8 a$, which have respectively the densities of 382 , 364 and $3 b^{2} 0$.

It will, of course, be understood that the above paralellisms are given merely as illustrations of how our experiments may serve to explain and illustrate the phenomena on the assumption of the atomic hypothesis and on the supposition that the actions which, in the experiments, take place in a plane, may similarly take place among repelling aud attracting points sitwate in space of three dimensions.

Other forms of the Experiments.-Instead of floating the magnets they may be suspended by fine silk fibers. In this method of experimenting the attractive action of the superposed magnet is replaced by the action of gravity, which draws the mutually repellant needles toward the vertical.

An advantage of this form of the experiment is that the configuration can be transported, and may thus serve in illustration of a moviug molecule as is set forth in the kinetic theory of gases. It is interesting to watch the mutual actions of two or more approaching configurations, and to observe the motions in the exterior and in the contour of a suspended configuration on its impact against a resisting or a yielding surface.

Professor O. N. Rood suggested to me to replace the suspended magnets by gilded pith balls, hung by silk fibers and similarly electrified.
Professor Frederick Guthrie, of London, under date of May 21, writes: "If the corks are made somewhat wider than in your larger needles, the needles move and arrange themselves very quickly if they are turned over and floated on perfectly pure and freshly filtered mercury. Those which reach the edge incline with their corks in the capillary trough."


Method of projecting the magnified images of the experiments on a screen.-To exhibit these experiments before a large audience it is best to use short magnets made as follows: Magnetize rather large sewing needles with their points all of the same polarity, then take each needle between the flat jaws of a pair pliers and with a pair of cutting-pliers snap off the needle close to the jaws of the other pliers. Thus form a series of magnets about $\frac{8}{4}$ inch in length. Run each of these through a thin section of a small cork and then coat both needle and cork with shellac varnish. Float these magnets in a glass tank placed over the condensing lens of a vertical-lantern, or you may even float them directly on the condenser itself if this is
made of an inverted glass shade filled with water. This form of condenser was first used by Dr. R. M. Ferguson, of Edinburgh.

Fig. 1 shows the arrangement of the experiment. The rays of light, $R$, from a heliostat, or from an oxyhydrogen light, fall on an inclined mirror, A, placed under the water condenser C. The needles float on the surface of the water in this condenser. The rays which have passed through the lens, L, are reflected by the swinging mirror, B , to the distant screen, where they form the images of the floating magnets. The magnet is held over the needles at M, by means of a wire which is wrapped round the magnet to serve as a handle. If a long magnet be used it will work well if its pole is brought over the needles* by inclining it.

These experiments with floating magnets give forcible presentations of the reign of law. It is indeed quite impressive to see order being evolved out of chaos as we hold a magnet over a number of needles, carelessly thrown on water, and witness them approaching and, one after the other, entering into the structure of that geometric figure which conforms to the number of magnets composing it.


[^0]:    * I am indebted to the courtesy of Mr. A. E. Beach, of the Scientific American, for the use of the engravings of the diagrams which illustrate this article.

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