

[Re] The cell-type specific cortical microcircuit: relating structure and activity in a full-scale spiking network model

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A reference implementation of

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Introduction

Most theoretical studies of cortical activity are based on networks of randomly connected units [2, 11, 5, 6] or with architectures artificially built from random networks [9]. In spite of the usefulness of these models, in order to understand the interplay between network structure and cortical dynamics it is essential to have computational models which accurately represent the cortical network architecture. Recently, Potjans and Diesmann [7] developed a network model of the local cortical microcircuit based on extensive experimental data on the intrinsic circuitry of striate cortex [8, 1]. The model contains two cell types (excitatory and inhibitory) distributed over four layers, L2/3, L4, L5, and L6, and represents the cortical network below a surface area of 1 mm² (a scheme is shown in Fig. 1).

The original implementation was based on the NEST simulator [3] and the source code is available at the Open Source Brain platform [10]. Here, we reimplemented the full model in the Brian 2 simulator [4] without direct reference to the original source code.

Methods

In this work, we replicated in Brian 2 every detail of the Potjans-Diesmann model as described in their original article [7]. Hereafter, we will refer to the original NEST implementation of the Potjans-Diesmann model [7] as reference (or original) article. In this section we explain how this reimplement was done. Further statistical analyses were performed using SciPy, NumPy, and Matplotlib libraries for the Python language.

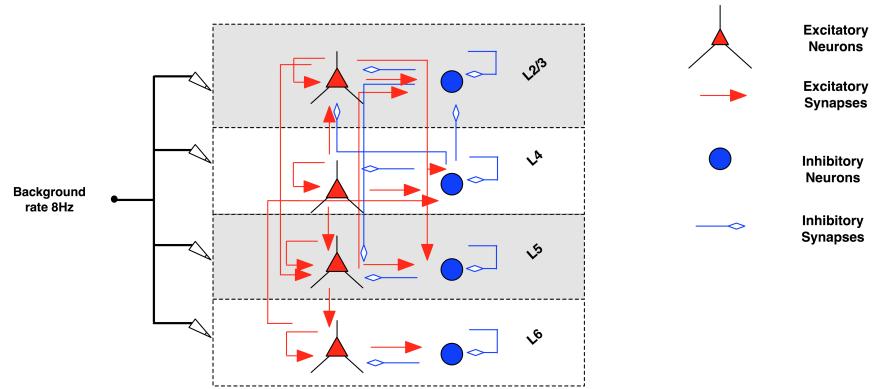


Figure 1: Schematic representation of the cortical network model (adapted from [7]). The model consists of four layers (L2/3, L4, L5 and L6), each one populated with excitatory (triangles) and inhibitory (circles) neurons (Table 2). Arrows represent connections with probabilities > 0.04 : excitatory in red and inhibitory in blue (Table 3). Black arrows represent background inputs.

Neurons

Network neurons are described by the leaky integrate-and-fire (LIF) neuron model. The subthreshold membrane voltage of neuron i obeys the equation

$$\dot{V}_i(t) = -(V_i(t) - V_{\text{reset}}) / \tau_m + I_i(t) / C_m, \quad (1)$$

where τ_m is the membrane time constant, C_m is the membrane capacitance, V_{reset} is the reset potential, and $I_i(t)$ is the total input current. When $V_i(t) \geq V_{\text{th}}$ the neuron emits a spike and the voltage is reset to V_{reset} , remaining fixed at V_{reset} for a refractory period τ_{ref} . The total input current $I_i(t)$ is divided into external $I_{i,\text{ext}}(t)$ and synaptic $I_{i,\text{syn}}(t)$. Whenever an excitatory (or inhibitory) neuron j presynaptic to neuron i fires at time t_j^f , the synaptic current to neuron i changes at time $t_j^f + d_e$ (or d_i) by an amount w (or $-gw$), where w is the excitatory synaptic weight, g is the relative weight of the inhibitory synapse, d_e is the excitatory synapse transmission delay, and d_i is the inhibitory synapse transmission delay. In the absence of synaptic inputs the synaptic current changes as

$$\dot{I}_{i,\text{syn}}(t) = -I_{i,\text{syn}}(t) / \tau_{\text{syn}} \quad (2)$$

where τ_{syn} is the postsynaptic current time constant (parameter values are shown in Table 1).

Network

The procedure to set up the network connections is the following:

- Start with a set of neurons $N = 77,169$, with model parameter described in Table 1.
- The N neurons are distributed over the eight different populations, L23e, L23i, etc, according to the numbers shown in Table 2.
- For each one of the sixty-four possible combinations of two from the eight cell populations, the total number K of synapses is calculated using equation (3) (compare with equation (1) of the original article), where $N_{\text{pre/post}}$ are the sizes

Table 1: Neuron and synaptic parameters. Neuron and synaptic parameters used in our simulations according to [7].

membrane time constant	τ_m	10 ms
refractory period	τ_{ref}	2 ms
postsynaptic current time constant	τ_{syn}	0.5 ms
membrane capacitance	C_m	250 pF
reset voltage	V_{reset}	-65 mV
threshold voltage	V_{th}	-50 mV
excitatory synaptic weight	w	$\mathcal{N}(\mu = 87.8, \sigma = 8.8)$ pA
relative inhibitory synaptic weight	g	4
excitatory synaptic transmission delay	d_e	$\mathcal{N}(\mu = 1.5, \sigma = 0.75)$ ms
inhibitory synaptic transmission delay	d_i	$\mathcal{N}(\mu = 0.8, \sigma = 0.4)$ ms
initial membrane potential	V_0	$\mathcal{N}(\mu = -58.0, \sigma = 10.0)$ mV

of presynaptic/postsynaptic populations and C_a is the corresponding connection probability given in Table 3 (the subindex a stands for ‘anatomical’ in the terminology of the original article).

$$K = \frac{\log(1 - C_a)}{\log(1 - 1/(N_{pre}N_{post}))} \quad (3)$$

- For every one of the sixty-four two-cell populations, the K synapses determined above are created by uniformly and randomly choosing K pairs of neurons (one from each population) and placing a connection between them. This is done with repetition to allow the creation of multiple synaptic contacts between any pair of neurons.
- The synaptic weight for connections originating from excitatory neurons is set to w and the synaptic weight for connections from inhibitory neurons is set to $-gw$. In addition, the synaptic weight for connections from neurons of layer L4e to L23e is doubled [7, 12].

Table 2: Layer population sizes (extracted from [7]). Neurons were distributed over four different layers (L23, L4, L5 and L6), and for each layer they were divided into excitatory (L23e, L4e, L5e and L6e) and inhibitory (L23i, L4i, L5i and L6i) subpopulations. The thalamic population is represented by Th.

L23e	L23i	L4e	L4i	L5e	L5i	L6e	L6i	Th
20683	5834	21915	5479	4850	1065	14395	2948	902

The ordinary differential equations were solved with the exact integration method for linear equations available in Brian 2 with a time step $\Delta t = 0.1$ ms. All simulations were carried out in a computer equipped with 2 Intel Xeon processors (E-2650v3, 2.3GHz) with 128GB of RAM.

External input

We chose from the reference paper three different types of external (“background”) inputs:

Table 3: Connectivity matrix between the different populations of the model (extracted from [7]). The connectivity matrix describes the probabilities of the target-specific connections between populations of neurons.

		from								
		L23e	L23i	L4e	L4i	L5e	L5i	L6e	L6i	Th
to	L23e	0.101	0.169	0.044	0.082	0.032	0.0	0.008	0.0	0.0
	L23i	0.135	0.137	0.032	0.052	0.075	0.0	0.004	0.0	0.0
	L4e	0.008	0.006	0.050	0.135	0.007	0.0003	0.045	0.0	0.0983
	L4i	0.069	0.003	0.079	0.160	0.003	0.0	0.106	0.0	0.0619
	L5e	0.100	0.062	0.051	0.006	0.083	0.373	0.020	0.0	0.0
	L5i	0.055	0.027	0.026	0.002	0.060	0.316	0.009	0.0	0.0
	L6e	0.016	0.007	0.021	0.017	0.057	0.020	0.040	0.225	0.0512
	L6i	0.036	0.001	0.003	0.001	0.028	0.008	0.066	0.144	0.0196

1. **Layer specific:** Neurons from each layer receive specific background spike-trains drawn from a Poisson distribution with firing rate $\nu = 8\text{Hz}$. The number of inputs per neuron is given in the first row of Table 4.
2. **Layer independent:** Spike-trains are drawn from an 8 Hz Poisson distribution as above, but now the number of inputs per neuron is the same for all the excitatory layers and the same for all the inhibitory layers as shown in the second row of Table 4.
3. **DC input:** The Poissonian background is replaced by constant DC currents to all neurons. The number of inputs per neuron follows the layer specific configuration (first row in Table 4). Observe that the number of inputs per neuron is multiplied by an effective factor which is given by $\nu \times w \times \tau_{syn} = 0.3512 \text{ pA}$. This factor is determined by calculating the time average of the synaptic current delivered by n spikes of the Poisson background to a given neuron.
4. **Transient thalamic input:** A thalamic population (Th) of 902 neurons, represented by Poissonian spike trains with firing rate of 120 Hz, is connected with the network following the connection probabilities in Table 3. In a simulated time period of 1 s, the thalamic input is applied at time $t = 700 \text{ ms}$ and lasts for 10 ms. This protocol is repeated hundred times to compute the average activity of 2.5% randomly sampled neurons from each layer of the network.

Additionally to these inputs, in Fig. 5C we simulate the network in several trials where the number of external inputs change. In every trial, the external inputs to each of the excitatory layers is a number randomly drawn between the layer specific and the layer independent inputs reported in Table 4. The inhibitory layers have their number of external inputs randomly decided between the already chosen number of their respective excitatory layer and the number calculated by

$$C_i = \left(\frac{1 - T}{1 + T} \right) C_e, \quad (4)$$

where T is the target specificity defined in [7] and is assumed here to be $T = 0.1$. However, there is an exception to this rule: L6i is allowed to have $T = 0.2$ due to the high number of inputs to L6e.

Table 4: Estimated numbers of external inputs per neurons in all network layers. The total number of external inputs is rounded.

	L23e	L23i	L4e	L4i	L5e	L5i	L6e	L6i
Layer specific	1600	1500	2100	1900	2000	1900	2900	2100
Layer independent	2000	1850	2000	1850	2000	1850	2000	1850
Background rate (ν)	8 Hz							

Measures

Here, we define the measures used to characterize the layer-specific activity of the network. They are the same ones used in the original article.

The spike train of a neuron i is represented by a sequence of temporal events (sum of delta functions). The firing rate over an interval T is obtained by summing the number of spikes during that interval and dividing by T (spike-count firing rate). The average firing rate of a population of N neurons is computed by calculating the firing rates of the neurons and dividing by N . With this procedure we calculated the average firing rates of the eight populations in the network.

To characterize irregularity in the network we use the coefficient of variation (CV) of the interspike interval (ISI) distribution. The CV_i for each neuron i is computed as the ratio of the standard deviation over the mean of its ISI distribution. Exponential distributions have $CV \approx 1$ while more regular distributions have $CV < 1$.

Synchrony is characterized by the variability of the histogram of population spiking activity (bin size = 3 ms). The synchrony index is computed as the variance of the spike count histogram divided by its mean.

The degree of asynchronous and irregular activity in a population is quantified by a measure called AIness%. This is the percentage of the population with mean firing rate < 30 Hz, irregularity between 0.7 and 1.2, and synchrony < 8 .

To compare the distributions of firing rates and CVs obtained from simulations in Brian 2 and NEST we use the Kolmogorov-Smirnov statistical test (KS-statistics). To apply this non-parametric test, cumulated histograms were constructed with bin size chosen as the square root of data size.

Results

In the following, we present results of the replicated studies (with the same data sampling sizes) done in the reference article for the network with parameters as defined in Methods. We did not replicate analyses which involve changes in the network structure.

Spontaneous Activity

The simulated spontaneous activity is asynchronous and irregular (Fig. 2A) and the cell-type specific firing rates are in agreement with the ones observed in the reference article, including the lowest rates for the excitatory cells of layers 2/3 and 6 and the highest rates for L5 cells (Fig. 2B). For all layers the inhibitory cell firing rates exceed the ones of excitatory cells. The firing rate variabilities (Fig. 2B) and the single-cell firing rate irregularities (Fig. 2C) are also similar to the ones reported in the original article. The irregularity measure is > 0.80 for all cell populations (Fig. 2C). The profile of the synchrony of spiking activity across the cell populations is also consistent with the one reported in the reference article. The highest degree of synchrony is found in L5e and the lowest one in L6.

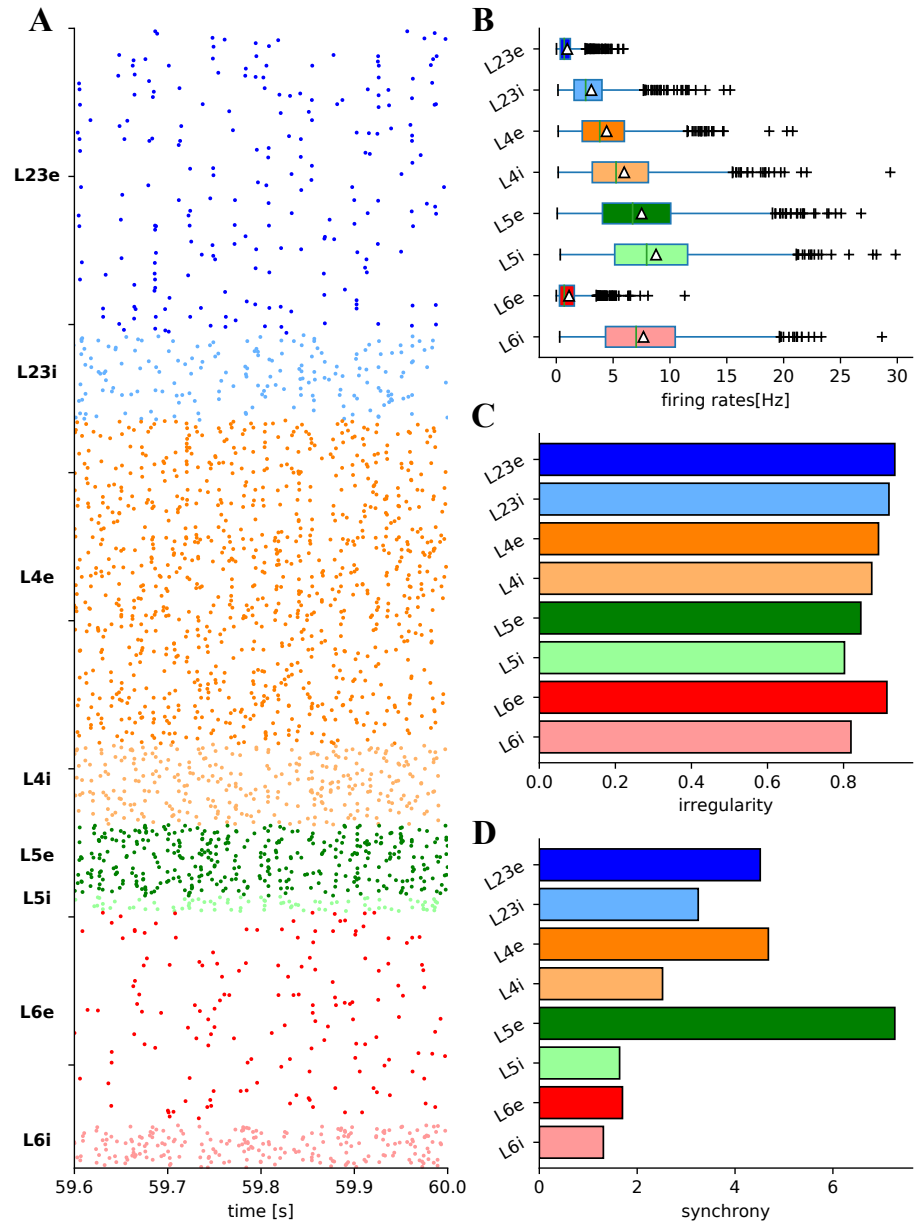


Figure 2: Spontaneous cell-type specific activity (to be compared with Fig.6 from the original article). In this simulation, $g = 4$ and background rate is layer-specific (8 Hz). **(A)** Raster plot of spiking activity for 0.4 s of all cell layers (from top to bottom; dark color: Excitatory cells, light color: Inhibitory cells). Number of displayed spike trains corresponds to 2.5% of the total number of neurons (preserving relative number of cells per layer). **(B–D)** Statistics based on samples of 1000 neurons per layer recorded for 60 s. **(B)** Single-cell firing rate boxplot. Triangles indicate population mean firing rates, crosses show outliers. **(C)** Irregularity of single-cell firing rates. **(D)** Synchrony of spiking activity.

In order to compare the Brian 2 with the NEST implementations of the Potjans-Diesmann model, we used the available pyNEST code [10] to run NEST simulations of the model with the same parameters given in Methods. The comparisons were made in terms of the cumulative distributions of the CVs of ISIs (Fig. 3) and the firing rates (Fig. 4) of the eight cell populations in the network. The two-sample Kolmogorov-Smirnov test pointed that no difference was found between NEST and

Brian 2 simulations, as observed by the close agreement of the cumulative histograms (orange lines with filled circles and green lines, respectively) in Figs. 3 and 4.

Besides the creation of the network connections by the procedure described above, which is the one used in the original article, it is also possible to connect the neurons in the network using the alternative expression for the total number of synapses between two cell populations,

$$K = C_a(N_{pre}N_{post}), \quad (5)$$

which comes from the first-order Taylor series approximation to the connection probability C_a as explained in the original article (see equation (2) and following text in the original article).

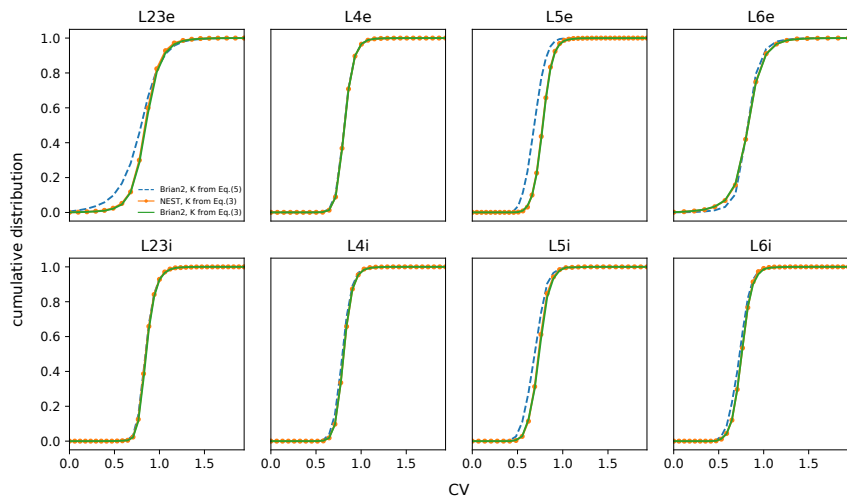


Figure 3: Cumulative distribution of CVs of ISIs for the eight cell populations (indicated atop each panel) for simulations implemented in Brian 2 using equation (5) (blue), in Brian 2 using equation (3) (green), and in NEST using equation (3) (orange). NEST code taken from [10].

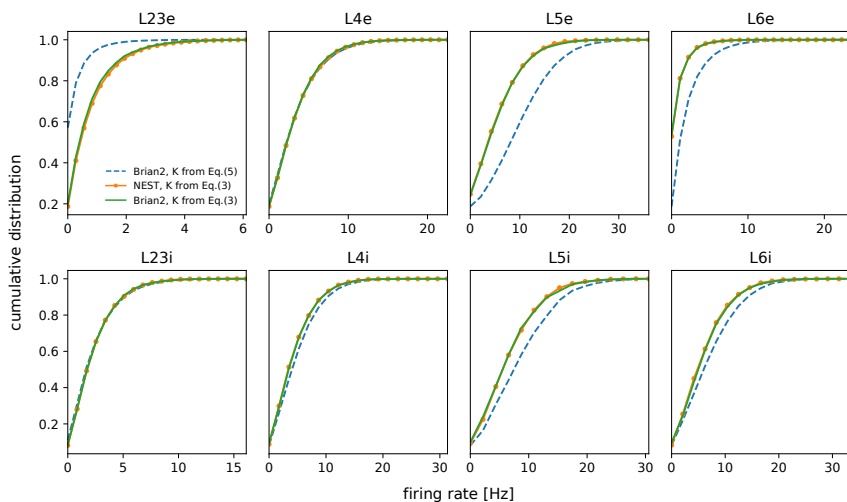


Figure 4: Cumulative distribution of firing rate for the eight cell populations (indicated atop each panel) for simulations implemented in Brian 2 using equation (5) (blue), in Brian 2 using equation (3) (green), and in NEST using equation (3) (orange). NEST code taken from [10].

To test for possible effects of using this approximate equation, we constructed the network in Brian 2 using both equations (5) and (3). We found that the use of the approximate equation brings discrepancies in comparison with the original model. The comparisons were made in terms of the cumulative distributions of the CVs of ISIs (Fig. 3) and the firing rates (Fig. 4) of the eight cell populations for simulations of the Brian 2 code with K calculated from equations (5) and (3).

When comparing the network constructed in Brian 2 with equation (5) and the one constructed with equation (3) (the same used in the original NEST code), the KS-statistics for layer L5e in the CVs of ISIs (2.43), and layers L23e, L5e and L6e in the firing rate (2.96, 1.79 and 1.87, respectively), revealed significant differences between the two implemented networks (≥ 1.63 for $\alpha = 0.01$). For the remaining layers, all comparisons indicated no significant differences for the firing rate and CV distributions. These results are summarized in Figs. 3 and 4, where the cumulative histogram for simulations using equation (5) are shown in blue dashed lines.

The differences found highlight the importance of using the exact expression for the total number of synapses K given in equation (3) (which corresponds to equation (1) of the original article) in simulations of the Potjans-Diesmann model.

We now return to the reimplementation of the Potjans-Diesmann model in Brian 2 using equation (3), which will be kept for the rest of this replication work.

Dependence of Spontaneous Activity on External Inputs

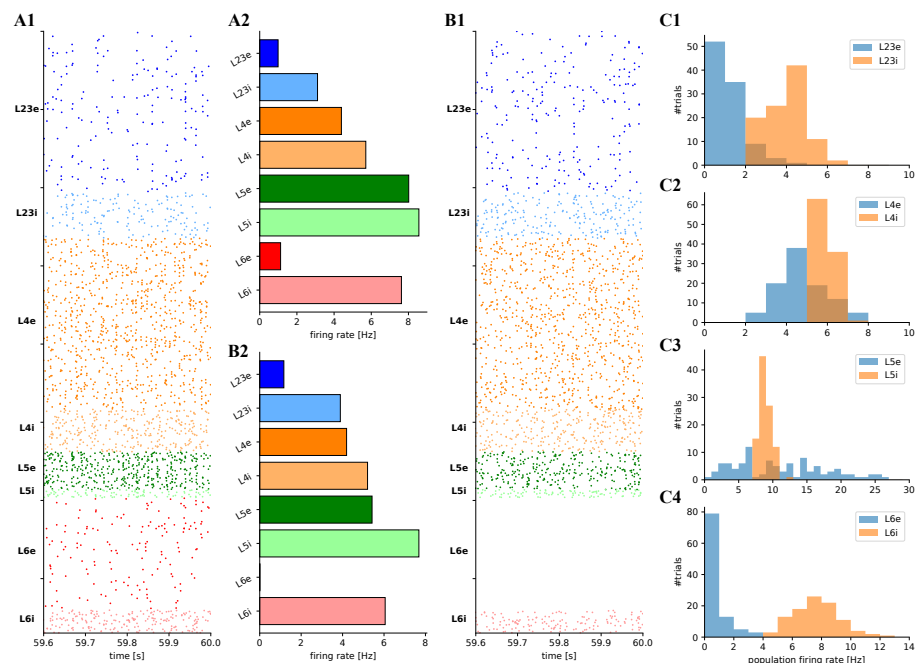


Figure 5: Raster plot of spiking activity over a 0.4 s period and average firing rate for different types of external input (to be compared with Fig. 7 of the original article). Color codes and sample cell sizes as in Fig. 2. (A1–A2) DC input. (B1–B2) Layer independent input. (C1–C4) Histograms containing the population firing rates of 100 trials where the external inputs were drawn with a specific rule (see details in methods).

In agreement with the results obtained in the reference article, the activity features of the Brian 2 implementation are also robust to changes in the external inputs. These are shown in Fig. 5A, in which the Poissonian inputs are replaced by constant DC currents, and in Fig. 5B, in which the layer-dependent Poissonian inputs are replaced by layer-independent inputs. In the latter case, the absence of activity in L6e resulting

from the layer-independent inputs indicates the importance of realistic input structure to yield plausible activity in all layers. In Fig. 5C we present the population firing rates for 100 trials with the rule explained in the methods section. This latter experiment presented an excellent agreement with the histograms observed in Fig. 7 of the original article.

Stability of Network Activity

The activity features obtained in the original article by changing the relative strength of inhibitory synapses and the background rate are reproduced in our reimplementation (Fig. 6).

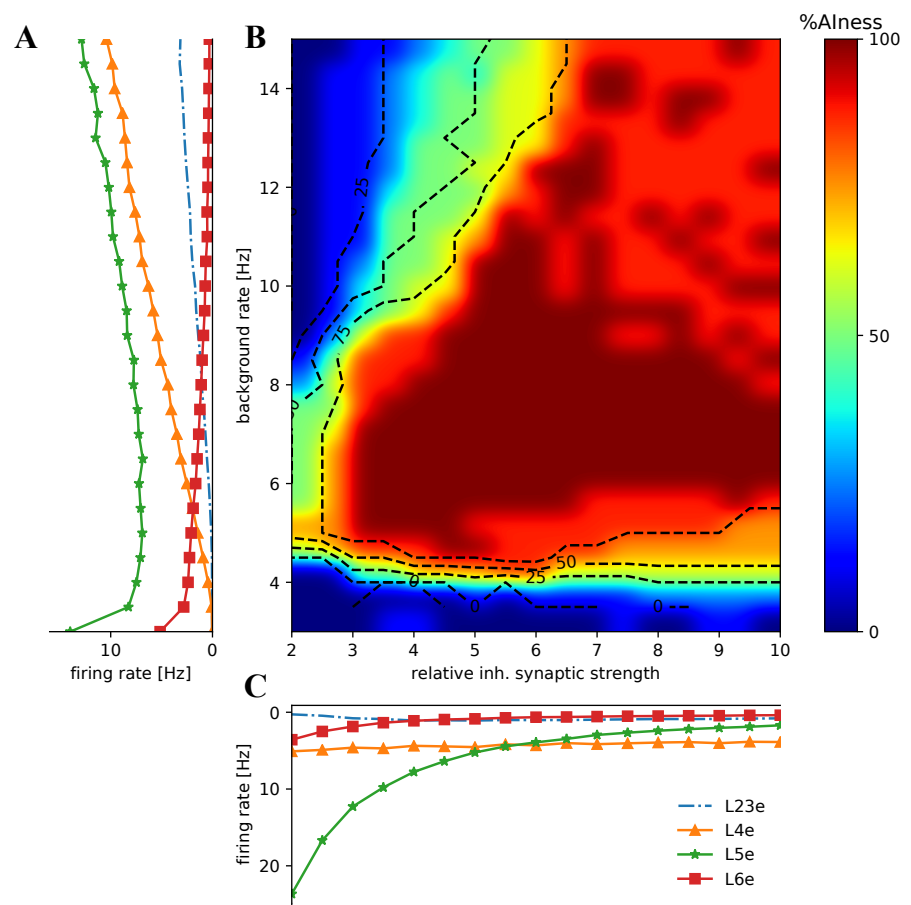


Figure 6: Network activity dependence on background rate and relative inhibitory weight (to be compared with Fig. 8 of the original article). (A) Mean population firing rates of excitatory neurons in layers 2/3 (dashed line), 4 (triangles), 5 (stars) and 6 (squares) as a function of the background rate for fixed $g = 4$. (B) AIness% (see Methods) as a function of the background rate and the relative inhibitory synaptic strength g . Labeled dashed contour lines indicate areas where 25%, 50% and 75% of all populations fire in an asynchronous and irregular mode at low rate. (C) Mean population firing rates of excitatory neurons as a function of the relative inhibitory synaptic strength g for fixed background rate 8 Hz (markers as in (A)).

The asynchronous and irregular activity of the reimplemented network model, as characterized by the AIness%, is similar to the one found in the reference article for background rates >5 Hz and relative inhibitory synaptic strengths >4 Hz. In comparison with the reference article, the relative order of excitatory firing rates is maintained

for every combination between background rate and relative synaptic strength, with highest values in L5 and smallest in L2/3 and L6. Similarly to the original article, the firing rate of L4e cells is the most sensitive to variations in the background rate whereas the firing rate of L5e cells is the most sensitive to variations in the relative inhibitory synaptic strength g .

Propagation of Transient Thalamic Inputs

In this section we make use of the thalamic inputs as described in the last column of Table 2. For further information on how thalamic inputs are applied we refer to the Methods section.

As described in the results section of the original article, when thalamic input is delivered to the network the output is rather stereotypical. This is confirmed by our results presented in Fig. 7, which shows the response of the network replicated in Brian 2 to transient thalamic input. By comparing histograms in Fig. 7B with the ones in Fig. 10B we think that our model replicates the original article.

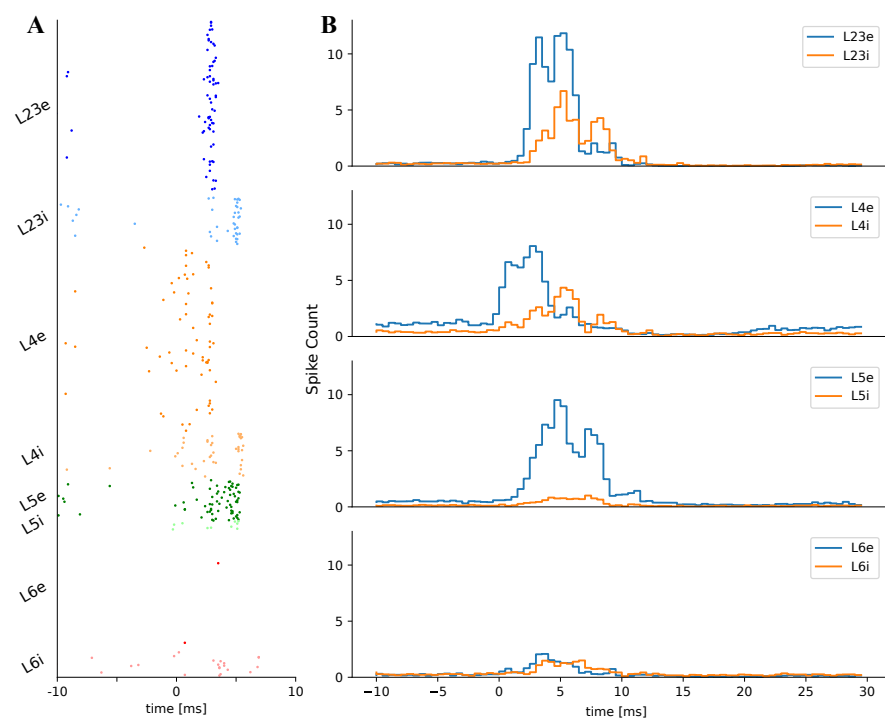


Figure 7: Response to transient thalamic input (to be compared with panels A and B of Fig. 10 from the original article). Note that the time axis is centralized at the beginning of the thalamic input, which lasts for 10 ms. (A) Sample raster plot of the network while receiving transient thalamic input as described in the Methods section. (B) Cell-type specific population spike-counts averaged over 100 different applications of thalamic stimuli.

Important information needed during replication

Most of the information necessary for the replication done here was available in the original article. However, a few details were found only in the NEST implementation of the code available in the Open Source Brain (OSB) platform [10]. In this section we list these details.

- When replacing the Poissonian background by a DC current the number of inputs per neuron was multiplied by the factor 0.3512 pA as explained in the Methods

section of this article. This factor is not explicitly explained in the original article.

- There is no mention to the initial voltage values in the original article. This information was found in the OSB NEST code where one can observe that the initial voltage values are randomly drawn from the normal distribution $\mathcal{N}(\mu = -58, \sigma = 10)$ mV.
- In the original article, the equation for the integrate-and-fire model does not explicitly state the resting potential. This could suggest to a naïve reader that the resting potential is 0 mV, whereas the correct resting potential is the reset voltage V_{reset} (cf. equation (1)).
- The thalamic input in the original article is described as having 15 Hz, however in the OSB NEST code it is actually 120 Hz, which is the correct value to be used.

Conclusion

Using the Brian 2 reimplementations of the Potjans-Diesmann model we were able to reproduce the main results of the original article [7]. The spontaneous activity of the network reimplementations is asynchronous and irregular as evaluated by the different measures used to characterize spiking behavior.

We also have shown the importance of using the exact expression in equation (1) of the original article instead of the approximate one in equation (2) in implementations of the model. The use of the approximate expression leads to mean firing rates of L5e neurons significantly higher than in the original implementation of the model.

The successful replication of the results of the reference article confirms the robustness of the original implementation of the model.

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