

Determining the Power-Law Wind-Profile Exponent under Near-Neutral Stability Conditions at Sea

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ABSTRACT

On the basis of 30 samples from near-simultaneous overwater measurements by pairs of anemometers located at different heights in the Gulf of Mexico and off the Chesapeake Bay, Virginia, the mean and standard deviation for the exponent of the power-law wind profile over the ocean under near-neutral atmospheric stability conditions were determined to be 0.11 ± 0.03 . Because this mean value is obtained from both deep and shallow water environments, it is recommended for use at sea to adjust the wind speed measurements at different heights to the standard height of 10 m above the mean sea surface. An example to apply this P value to estimate the momentum flux or wind stress is provided.

1. Introduction

The vertical distribution of the wind or wind shear over the water surface is an important factor to consider since it is not only related to the momentum flux, which is the driving force in the generation of wind waves and wind-drift ocean currents, but also to the wind loads on ships and marine structures such as oil platforms.

In the atmospheric surface boundary layer extending to not more than 100 m above the surface (e.g., Sutton 1953, 14–15), the logarithmic wind profile has been used extensively (e.g., Panofsky and Dutton 1984). For practical applications at sea, however, in situ measurements of the aerodynamic roughness length are not always available, because it is related to both the wind speed and to the wave characteristics (Hsu 1988). Therefore, the simple power-law wind profile is often employed because it is quite accurate and useful for engineering applications (e.g., Panofsky and Dutton 1984).

The power-law wind profile states that

$$\frac{u_2}{u_1} = \left(\frac{z_2}{z_1} \right)^P, \quad (1)$$

where u_2 is the wind speed at height z_2 , u_1 and z_1 are the wind speed and height already known, respectively,

at a reference height, and the exponent P is a function of both the atmospheric stability in the layer over which P is determined to be valid and the underlying surface characteristics.

Davenport (1965) speculated that for the open sea, the exponent P is approximately 0.10. On the basis of a detailed tether-sounding of the atmospheric boundary layer over the Mediterranean Sea under near-neutral stability conditions, Hsu (1988, 201–203) found that $P = 0.10$. The near-neutral condition over the water surface is defined as the $|z/L| \leq 0.4$ (where L is the Monin–Obukhov stability length) (see Hsu 1992). The purpose of this research note is to further substantiate this value based on more datasets available recently.

2. Methods

In order to obtain the exponent P in Eq. (1), we take the logarithm on both sides of the equation so that

$$\ln \left(\frac{u_2}{u_1} \right) = P \ln \left(\frac{z_2}{z_1} \right)$$

or

$$P = \frac{\ln(u_2/u_1)}{\ln(z_2/z_1)}. \quad (2)$$

Since many marine operations such as frequent helicopter landings on offshore oil rigs require wind information at elevations much higher than the 5–10 m

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above the sea surface as normally measured by most National Data Buoy Center (NDBC) buoys, meteorological measurements at higher elevations are needed. The airflow distortion by the rig structure itself must be minimized, however (e.g., Katsaros et al. 1987). On the basis of both field measurements (e.g., Thornthwaite et al. 1965) and laboratory simulations (Wills 1984), the datasets selected for this study are considered to be representative within 5% between the measurements employed and those under undisturbed conditions. Note that because the flow distortion problem was considered in the very beginning for the instrument siting by NDBC, the anemometers on these offshore structures are located in the area where the structure effect is minimal. Since the aggregate wind estimation error cannot be less than 10% at airports on land, where most official weather service stations are located (see Wieringa 1980), the offshore wind measurements selected for this study are considered to be reasonable.

a. Open-ocean conditions

For open-ocean conditions, two platforms in the Gulf of Mexico along the continental shelf break with anemometers at different heights were available, as shown in Fig. 1. Note that at both sites dual wind measurements were needed to ensure data continuity (one was considered a backup). They were Coastal-Marine Automated Network (C-MAN) station Garden Banks block 236A and moored buoy station 42019. A description of the platforms and data retrieval methods is provided as follows (National Data Buoy Center 1990a, 1992):

1) GARDEN BANKS 236A (GBCL1)

GBCL1 is a high-pressure natural gas production platform installed and operated by Chevron Oil Company in the Gulf of Mexico (Fig. 2). The measurements were taken by an NDBC C-MAN system consisting of two anemometers and an air temperature sensor mounted on a gas boom approximately 57.5 m above mean sea level (MSL) and a barometer with the vent port on the boom at 49.7 m MSL (Fig. 3). The boom slightly obstructed the anemometers in a narrow zone between approximately 180° and 200°T. The water temperature sensor was mounted at approximately 1.5 m below MSL on the inboard side of a boat landing on the west side of the platform. Unfortunately, the C-MAN station at GBCL1 was removed in the summer of 1992.

2) MOORED BUOY STATION 42019

NDBC buoy station 42019 is a 3-m disc-shaped buoy made of aluminum (Fig. 4). The buoy design and characteristics are discussed in detail by Hamilton

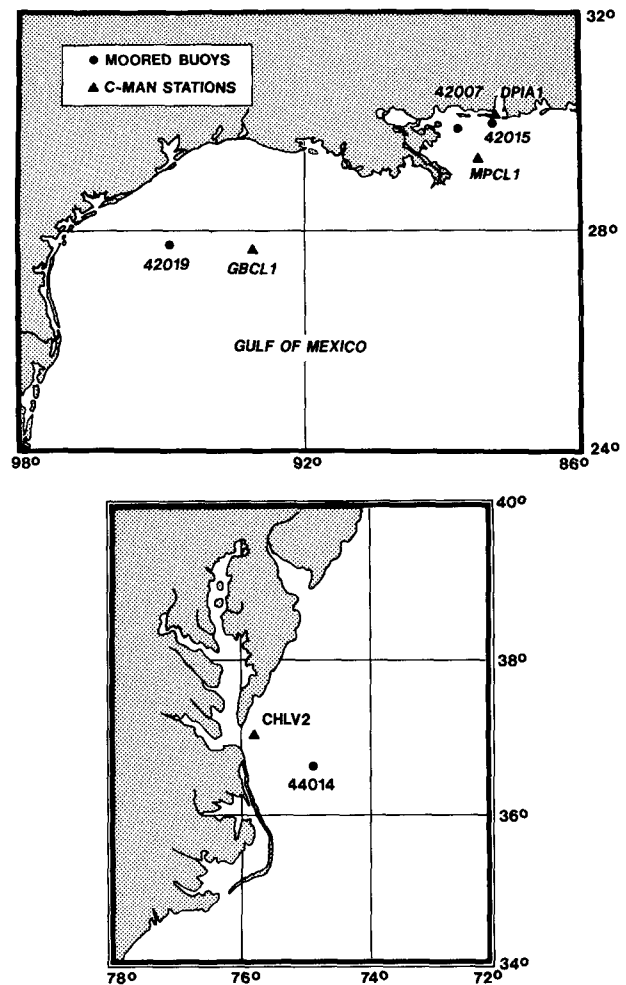


FIG. 1. Map showing the locations of moored buoys and C-MAN stations used in this study: (a) in the northern Gulf of Mexico; (b) on the mid-Atlantic coast near Chesapeake Bay, Virginia. Buoy station 42016 is not plotted, because of its close proximity to station 42015.

(1988). The buoy provides the same kind of measurements as GBCL1. The anemometers are located approximately 4.9 m above the nominal waterline. The barometers and thermometer are 3.5 m above the water, while sea temperature is measured through the hull at a depth of approximately 0.5 m. Meteorological measurements are taken during an 8-min sampling period at 1 Hz starting 18 min before each hour.

b. Coastal ocean conditions

Three pairs of dual-anemometer stations were incorporated into this study. Two station pairs are in the northern Gulf of Mexico. They are Main Pass 133C (MPCL1) and moored buoy station 42007, and Dauphin Island (DP1A1) and either moored buoy station 42015 or 42016. The third pair was the Chesapeake



FIG. 2. Chevron Oil Company's Garden Banks 236A gas production platform. The photo was taken prior to installation of the C-MAN measurement equipment, including a 6.1-m mast and anemometers near the end of the boom.

Light Station (CHLV2) and moored buoy 44014 located off the mid-Atlantic coast (Fig. 1 and Table 1).

1) MAIN PASS 133C (MPCL1)

The anemometers at MPCL1 were located 40.2 m above the water on a mast near the end of a flare boom that extended due south from the south corner of the platform. They were slightly obstructed to due south by the flare boom itself. The thermistor was at 40.2 m, water temperature was measured by a thermistor on the south platform leg at approximately 1-m depth.

2) MOORED BUOY STATION 42007

Moored buoy 42007 is a discus-shaped hull made of steel that is 12 m in diameter. The two anemometers and the air temperature sensor are 10 m above the

water. Water temperature is measured through the hull at 1.1-m depth.

3) DAUPHIN ISLAND (DPIA1)

DPIA1 is collocated with a National Ocean Service (NOS) tide station just north of the eastern end of Dauphin Island, Alabama. The station is at the end of a pier that extends northeast approximately 75 m from shore. Wind sensors are 17.4 m above MSL; air temperature is measured at 16.8 m; sea temperature is measured at 1-m depth. Fort Gaines, a large structure, is located approximately 100 m southwest of the DPIA1 pier. While the anemometers are approximately 10 m above the Fort Gaines battlements, the size of the fort probably influences winds blowing from the southwest.

4) MOORED BUOY STATIONS 42015 AND 42016

The moored buoys at both 42015 and 42016 are 3-m discus buoys described earlier. Data from 42015



FIG. 3. A close-up view of the C-MAN anemometer system on the boom of station GBCL1. Note that the dual-anemometer system was installed on the station so that one of them could act as a backup.

was used in the study except for periods during which it failed or was retrieved. In these events, data from 42016 were used.

5) CHESAPEAKE LIGHT STATION (CHLV2)

CHLV2 is a steel framework tower operated by the U.S. Coast Guard. The anemometer is located 43.3 m above the water in an unobstructed position on the southeast corner of the structure. The air temperature is measured at 22.3 m above the water, while the water temperature thermistor is attached to a leg of the structure approximately 2.5 m below MSL.

6) MOORED BUOY STATION 44014

Moored buoy 44014 is a 3-m discus buoy similar to the systems described earlier, except that a wind fin was attached to the buoy's nominal stern in order to turn the buoy into the wind. This feature should have no effect on the data in this study.

c. Data sampling and retrieval

Data for all fixed platforms were obtained during a 2-min sampling period at 1 Hz. For GBCL1, MPCL1, and DPIA1, the sampling interval was from minute 23 to 25 of each hour; for CHLV2, the interval was from minute 58 to 60. All moored buoy data were sampled

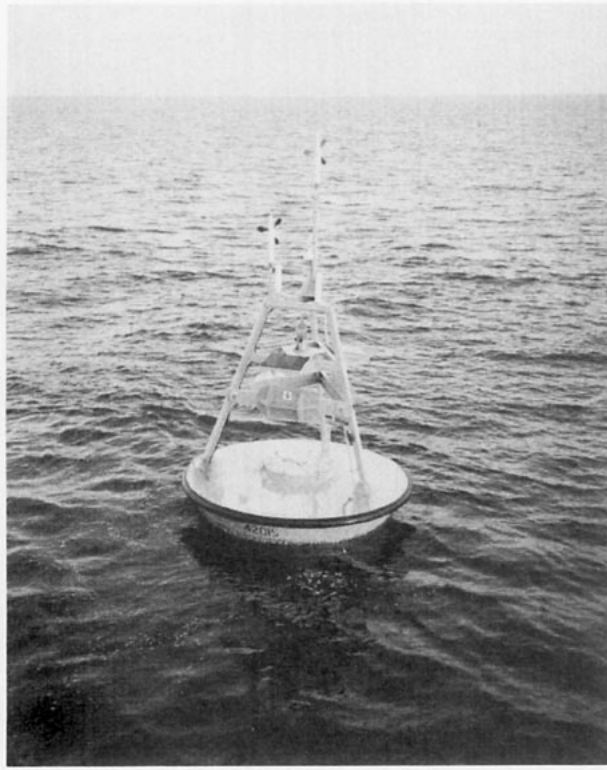


FIG. 4. Photograph of an NDBC 3-m disc buoy similar to the system deployed at station 42019. Note that the dual-anemometer system was installed on the station so that one could act as a backup.

at 1 Hz for 8 min from minute 42 to 50 of each hour. Wind directions represent a unit-vector average; wind speeds were scalar averaged on both fixed platforms and moored buoys. Although wind information is normally available at NDBC from the two anemometers at each station, data from only one instrument is archived and used in this study. There are two main purposes of the second anemometer: first, it is heavily relied upon to verify data quality from the “primary” anemometer in “real time”; second, it is a hot backup in the event the operational anemometer fails.

Following sampling, data underwent preliminary processing and transmission each hour via a National Oceanic and Atmospheric Administration Geostationary Operational Environmental Satellite to ground receiving facilities operated by NOAA’s National Environmental Satellite Data and Information Service at Wallops Island, Virginia. From Wallops Island, data were transferred by landline to the National Weather Service Telecommunications Gateway, Silver Spring, Maryland, for further processing that included data quality checking, encoding, real-time distribution, and archiving.

3. Results and discussions

In order to ensure that the stability is near neutral based on the criterion provided in Hsu (1992), only monthly maximum wind speeds for these stations as published in the *Mariners Weather Log* are used in

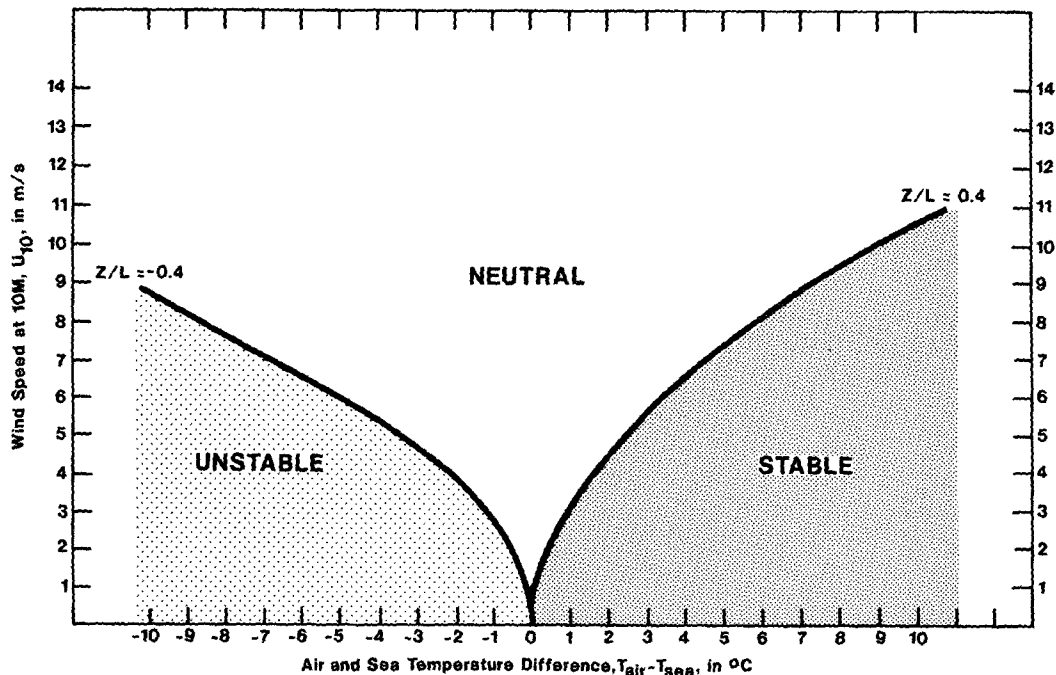


FIG. 5. The stability criteria used in this study [simplified from Hsu (1992)].

TABLE 5. Same as Table 2 except C-MAN station CHLV2 and NDBC buoy station 44014 off east coast of United States (see Fig. 1). Values of the exponent P of the power-law wind profile are calculated from Eq. (2).

Month	Day/hour (UTC)	C-MAN CHLV2				Buoy 44014					P
		$u_{43.3\text{ m}}$ (m s^{-1})	Wd ($^{\circ}$)	Pressure (Pa)	$T_{\text{air}} - T_{\text{sea}}$ ($^{\circ}\text{C}$)	Day/hour (UTC)	$u_{4.9\text{ m}}$ (m s^{-1})	Wd ($^{\circ}$)	Pressure (Pa)	$T_{\text{air}} - T_{\text{sea}}$ ($^{\circ}\text{C}$)	
October 1990	26/1100	24.1	4	999.8	-7.7	26/1300	21.6	352	994.4	-5.9	0.050
February 1991	14/1500	16.5	223	998.0	5.2	14/1500	14.5	210	988.9	1.3	0.059
June 1991	23/2100	15.1	40	1014.5	-1.8	23/2100	13.4	31	1012.4	-0.9	0.055
October 1991	17/1300	23.2	332	1008.1	-8.6	17/1100	18.2	282	1005.0	-4.2	0.111
November 1991	09/2200	23.8	45	1017.7	-2.8	09/2300	17.4	25	M	-1.5	0.144
February 1992	29/1600	18.9	345	M	-2.0	29/1900	16.1	325	1010.2	-4.2	0.074
June 1992	22/0500	12.9	341	1014.8	-2.4	22/0600	9.9	338	1012.7	M	0.121
Mean		19.2					15.9				0.088
Standard deviation											0.037

Note that, according to Panofsky and Dutton (1984, p. 131),

$$P = \left[\ln \left(\frac{z}{z_0} \right) \right]^{-1}, \quad (3)$$

where $z = 10$ m and z_0 is the roughness length. For the smooth terrain on land ($z_0 = 1$ cm), therefore, $P = 0.14$ or $1/7$, a value commonly suggested in engineering texts for land-based use. For offshore applications, however, z_0 ranges from 10^{-4} to 10^{-3} m (see Panofsky and Dutton 1984, Table 6.2, p. 123). Therefore, P varies from 0.087 to 0.109. If we take the mean z_0 of 5×10^{-4} m and substitute it into Eq. (3), we have a typical offshore value of $P = 0.10$, which is nearly identical with the value as suggested in our study. The discussion explains that the typical value of P on land is 0.14, and offshore 0.10. This is mainly due to the larger value of roughness length z_0 on land than offshore.

It should also be noted that, according to Panofsky and Dutton (1984, p. 123), the value of z_0 for off-sea wind in coastal areas is around 10^{-3} m, which is on the top of their list for large expanses of water. Therefore values of P for the coastal regions such as provided in Tables 3 and 4 are larger than those farther offshore as shown in Table 2. Since z_0 is inversely proportional to the wave age at sea for the same wind speed (Maat et al. 1991) and since the Atlantic along the eastern seaboard (Table 5) experiences more swell (older waves) than the Gulf of Mexico, the value of P is also smaller. In order to demonstrate that the result is useful, Table 6 is provided. From this table and Fig. 5 it can be seen that from a marine climatic point of view the near-neutral stability prevails in the surface boundary layer at sea. Therefore, Eq. (1) with $P = 0.11$ should be applicable most of the time at sea.

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TABLE 6. Monthly mean wind speeds and air-sea temperature differences for NDBC buoys 42008 (1980-84), 42007 (1981-88), and CHLV2 (1984-88). For station locations, see Fig. 1.

Month	42008		42007		CHLV2	
	$T_{\text{air}} - T_{\text{sea}}$ ($^{\circ}\text{C}$)	$u_{14.9\text{ m}}$ (m s^{-1})	$T_{\text{air}} - T_{\text{sea}}$ ($^{\circ}\text{C}$)	$u_{10\text{ m}}$ (m s^{-1})	$T_{\text{air}} - T_{\text{sea}}$ ($^{\circ}\text{C}$)	$u_{43.3\text{ m}}$ (m s^{-1})
January	-0.5	6.4	-2.8	5.5	-2.4	8.1
February	-0.7	6.8	-0.5	5.6	-0.6	8.0
March	-0.2	6.4	-0.6	5.7	1.1	8.4
April	0.2	6.6	-0.4	6.0	1.3	7.6
May	-0.5	6.6	-0.7	5.3	1.2	6.4
June	-0.8	6.0	-0.7	4.7	1.0	6.4
July	-1.0	5.6	-0.7	4.1	0.8	5.6
August	-1.3	5.3	-0.9	4.2	-0.2	5.8
September	-1.4	6.4	-1.3	5.1	-1.0	6.2
October	-0.8	6.5	-1.6	5.4	-1.8	7.1
November	0.6	6.3	-1.5	5.9	-2.0	7.7
December	0.1	7.0	-2.0	5.9	-2.6	7.5

* Data source: National Data Buoy Center 1990b.

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