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of $L_{\perp}/n_h = 0.050 \pm 0.005$, which is thus five times larger than that of Ni.

For a direct comparison of the E_{MCA} in Ni and Co, we need to know the proportionality factors in Eq. 1. We performed fully relativistic first-principles band structure calculations in the local spin-density approximation (13) for both Co and Ni (Fig. 3). Their face-centered lattices were tetragonally distorted to various degrees, resulting in a simultaneous change in E_{MCA} and L_{\perp} . These quantities show a linear relation with the same proportionality factor over a wide distortion range. This is surprising, because ξ for Ni is about 12% greater than that for Co. The small deviations from the linear behavior can be assigned to additional terms neglected in Eq. 1, such as the magnetic dipole contribution (9). Applying the curve in Fig. 3 to our experimental data, we obtain for the magnetic anisotropy energy of the 33-ML Ni and 3-ML Co layers per unit cell values of $E_{MCA}^{Ni} = 14$ meV and $E_{MCA}^{Co} = -11$ meV (14), where we used the calculated number of $3d$ holes of $n_h^{Ni} = 1.4$ and $n_h^{Co} = 2.4$. The measurements show unambiguously that the Ni spins in both cases favor a perpendicular orientation, and it is the anisotropy contribution of the Co layer that determines the spin orientation of the entire film. For the 3-ML Co/33-ML Ni film, the anisotropy contributions nearly cancel each other, resulting in the mixed in-plane and perpendicular easy-axis characteristics of Fig. 1. A small increase in the Co layer thickness causes a negative total anisotropy energy, and consequently, the easy magnetization direction will be completely in the film plane in agreement with the hysteresis measurements.

The strong exchange interaction through the Co/Ni interface mediated by $3d$ electrons couples the spins of the two layers parallel (2). Our element-specific TMCXD measurements establish the competition between the in-plane anisotropy of the Co orbital moment and the out-of-plane anisotropy of the Ni layer. This leads to the observed Co thickness-dependent reorientation of the total spin magnetic moment. Such measurements can be performed in a fixed geometry and only involve monitoring of the x-ray absorption cross-section, which in principle can be done in reflection or transmission. Combined with x-ray microscopy, this technique could be used to image magnetic anisotropy of nanostructures and devices.

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11. MCA is usually described as a perturbation expansion in ξ (8). In low-symmetry nanostructures, the

- dominant contribution is the so called uniaxial anisotropy, which is of second order in ξ . Only this term is considered here.
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14. Using the Cu substrate unit cell of 0.255 by 0.255 nm, we obtain $E_{MCA}^{Ni} = 34$ mJ/m² and $E_{MCA}^{Co} = -27$ mJ/m². These values come out to be very large (2), probably because band structure calculations overestimate the proportionality factor between E_{MCA} and L_{\perp} (10).

14 March 1997; accepted 21 May 1997

Glacial Cycles and Astronomical Forcing

Richard A. Muller and Gordon J. MacDonald

Narrow spectral features in ocean sediment records offer strong evidence that the cycles of glaciation were driven by astronomical forces. Two million years ago, the cycles match the 41,000-year period of Earth's obliquity. This supports the Croll/Milankovitch theory, which attributes the cycles to variations in insolation. But for the past million years, the spectrum is dominated by a single 100,000-year feature and is a poor match to the predictions of insolation models. The spectrum can be accounted for by a theory that derives the cycles of glaciation from variations in the inclination of Earth's orbital plane.

Nearly as soon as the ice ages were discovered, their origin was attributed to astronomical causes. In the late 1800s, James Croll assumed that the ice ages were driven by changes in insolation (solar heating) brought about by variations in Earth's orbit and spin axis (1, 2). According to Croll, and to Milankovitch after him (3, 4), the main orbital parameters that affect insolation and its distribution are Earth's orbital eccentricity, obliquity (the tilt of Earth's poles toward the sun), and precession (the lag between equinox and perihelion). However, it was not until 1970 that Broecker and van Donk (5) established that glaciation in the late Pleistocene was truly periodic and was dominated by a 100,000-year (100-ky) cycle. This period was soon identified with the quasiperiodic 100-ky cycle of Earth's eccentricity. (We will offer evidence that this identification was premature.) In addition, another strong cycle was discovered with a 41-ky period that matched the cycle of changes in Earth's obliquity (6). This 41-ky cycle appears to have dominated glacial changes from 1.5 to 2.5 million years ago (Ma) (7). The 100-ky cycle has dominated from 1 Ma to the present.

Much of the best data for paleoclimate studies comes from ocean sediments, in which proxies for climate, preserved in

fossils, are measured as a function of depth. The oxygen isotope ratio $\delta^{18}O$ is believed to reflect the amount of Earth's water frozen in ice and thus is a measure of Earth's global ice volume. To turn a record of $\delta^{18}O$ versus depth into a record versus time, the sedimentation rate must be estimated. This is often done with a process called tuning, in which the instantaneous sedimentation rate is deduced by matching cycles in $\delta^{18}O$ to calculated perturbations in Earth's orbit. Parameterized sedimentation rates are adjusted to bring the observed proxy variations into consonance with the predictions of the model. This approach is potentially circular if the results are used to validate the climate model used to tune the record. Neeman (8) has demonstrated with Monte Carlo tests that, given enough parameters, tuning procedures can successfully match data to an incorrect model, resulting in an inaccurate time scale as well as in a false validation of the model. Therefore, for the present work, we emphasize the use of time scales that are untuned and assume constant sedimentation with average rates constrained by radiometrically measured control points.

A strong case for astronomical forcing of glacial cycles comes from analysis of $\delta^{18}O$ data for the age interval 1.5 to 2.5 Ma from Deep Sea Drilling Project (DSDP) site 607, located on the west flank of the Mid-Atlantic Ridge. For a full description of the stratigraphy, dating, and magnetic correlation, see Ruddiman *et al.*

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(7) and Raymo *et al.* (9). In their spectral analysis of the $\delta^{18}\text{O}$ data for the time interval 1.60 to 2.75 Ma, Ruddiman *et al.* (10) found a 41-ky peak with a full width at half maximum (FWHM) $\Delta f/f$ of 12%. This is close to the width that would be obtained for a pure sine wave, using the low-resolution spectral method that was employed [Blackman-Tukey (11) with 1/3 lags (12)]. However, the time scale of this record had been tuned to obliquity, so it was conceivable that the relatively narrow width was an artifact of tuning.

The $\delta^{18}\text{O}$ data versus depth are shown in Fig. 1A. To make an analysis that does not depend on tuning, we calculated the spectral power as a function of cycles per meter, using a method (13) that has about three times better frequency resolution than the method used by Ruddiman *et al.* The resulting spectrum is shown in Fig. 1B. It has one strong peak near 0.52 cy-

cles/m, with statistical significance greater than 99.9% (14). To place a time scale on the data, we assumed the same average sedimentation rate (15) used by Raymo *et al.* for this interval: 45.6 m per million years. With this sedimentation rate, the peak in Fig. 1B appears near the 41-ky period of obliquity.

The narrow width of this peak is the salient feature for the present discussion. The peak has a FWHM of $\Delta f/f = 3.7\%$. This is the same width that we obtain when we perform the same analysis on a pure 41-ky sine wave (or on any other perfectly periodic function, such as triangular, whose fundamental component is at 41 ky) for the same 1-million-year duration (16). The fractional width of a periodic signal is independent of the assumed sedimentation rate but depends solely on the number of cycles in the interval (17). The presence of a narrow peak in untuned

data requires two phenomena: the existence of a nearly constant sedimentation rate and the presence of a truly periodic signal.

The narrow width has important implications for climate models. In any climate model that depends on free oscillation, the width will be significantly broadened if substantial energy loss (friction) is present or if the mode of oscillation is not isolated from other modes. For this reason, free-oscillation climate models generally predict broad spectral peaks. Likewise, climate models based on relaxation oscillators usually have broad peaks. Relaxation oscillators tend to lose their phase stability (and their narrow spectral peaks) unless the energy exchange mechanisms are exceptionally constant over many cycles, a condition not expected to be met in the geophysics of climate. In contrast, a climate model that depends on forced oscillations has a spectrum that reflects the spectrum of the driving force, so that regardless of losses, narrow spectral features in the force will also appear in the response (18). The only natural driving forces in physics that have narrow spectra tend to be astronomical and quantum-mechanical, because friction is often negligible both in space and in atoms. (This is why the motions of the Earth, moon, and planets provided the original calendars, and it is why quantum-mechanical devices provide the most accurate clocks.) Because we have no plausible way to relate the phase stability of the glacial cycles to quantum mechanics, we conclude that the oscillation is driven by an astronomical source. This is a general argument for the astronomical origin of the 41-ky cycle that does not depend on the details of any specific astronomical theory, such as the Croll/Milankovitch insolation model, or even on the frequency match between this cycle and the obliquity cycle.

Similar evidence for the astronomical origin of the 100-ky glacial cycle can be found in $\delta^{18}\text{O}$ data from Ocean Drilling Program (ODP) site 659, located in the Atlantic Ocean off northwest Africa, near 18°N and 21°W (19, 20). The untuned $\delta^{18}\text{O}$ data for the age interval from 0 to 900,000 years ago (ka) is shown in Fig. 2A. The time axis was derived by taking the age of Tiedeman *et al.* (20) for the maximum depth and assuming constant sedimentation. The spectrum is shown in Fig. 2B. A strong narrow peak appears near $f = 0.01$ cycles/ky (100-ky period). The FWHM of the peak is $\Delta f/f = 9.8\%$, which is indistinguishable from the width one would obtain for a sine wave (16). It is highly unlikely that a single narrow peak would appear in the untuned data unless

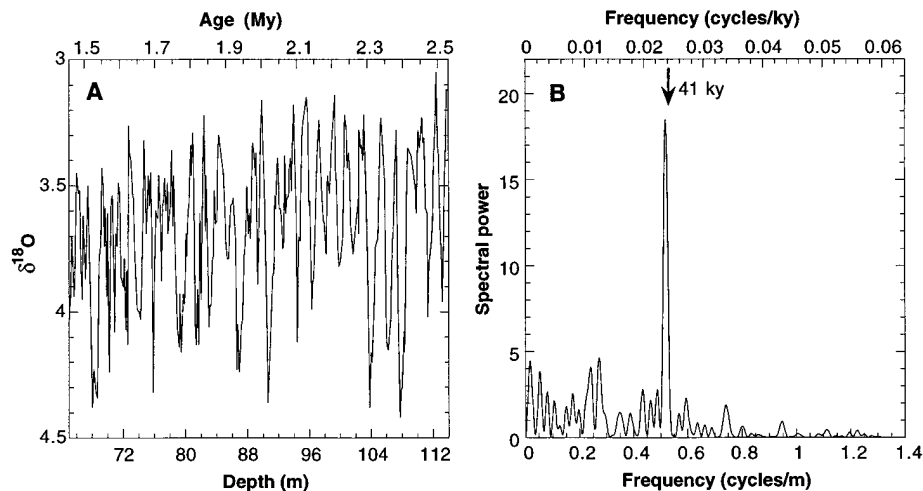


Fig. 1. (A) $\delta^{18}\text{O}$ data in parts per thousand and (B) spectral power for DSDP site 607, for the interval from 1.5 to 2.5 Ma. The time scale assumes a constant sedimentation rate.

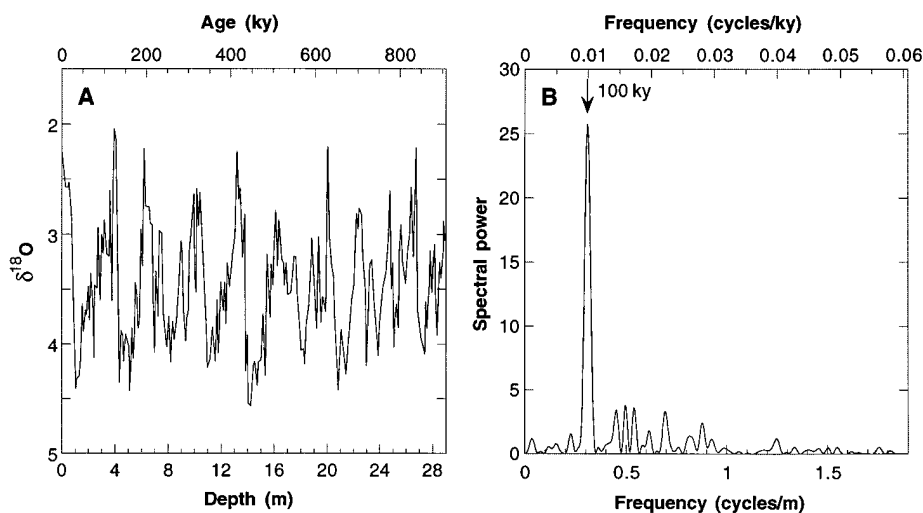


Fig. 2. (A) $\delta^{18}\text{O}$ data in parts per thousand and (B) spectral power for ODP site 659 for the interval from 0 to 900 ka. The time scale assumes a constant sedimentation rate.

the sedimentation rate were relatively constant and there were a driving force with a strong single period. We conclude that the 100-ky cycle is astronomically driven.

To make a more comprehensive study of the 100-ky cycle and to compare it with theory, we examined $\delta^{18}\text{O}$ records for cores at the following DSDP and ODP sites located in the Atlantic, Pacific, and Indian oceans: site 552 (21), site 607 (7, 9), site 659 (19, 20), site 664 (22), site 677 (23, 24), site 806 (25, 26), site 849(27), and the Specmap stack (28). Site 806 has been shown to have a nearly constant sedimentation rate for the interval from 0 to 840 ka (29). A narrow peak in the untuned data, which is evidence for nearly constant sedimentation, was also found in the spectra for site 664 for the interval from 0 to 600 ka.

In order to facilitate comparisons among the sites, we chose a common time interval covered by all the $\delta^{18}\text{O}$ data sets: 0 to 600 ka. In column A of Fig. 3 we show the spectra for this period expected from three climate models: a linear eccentricity model, a nonlinear ice model that derives its quasi-100-ky cycle from the envelope of the precession parameter (30), and an orbital inclination model (31–33). The frequency scale has been expanded to facilitate comparisons of the peak shape and structure. The orbital spectra were calculated using the results of Quinn *et al.* (34). The orbital inclination was transformed to the invariant plane as described by Muller and MacDonald (33); the values for the past 3 million years have been posted on the World Wide Web at www-muller.lbl.gov. The insolation-based models have spectral fingerprints with three peaks near 0.0025, 0.008, and 0.0105 cycles/ky, corresponding to periods of 400, 125, and 95 ky. The fingerprint of the inclination model has a single prominent peak near frequency 0.01 cycles/ky, corresponding to a period of 100 ky.

The spectra of the $\delta^{18}\text{O}$ data are plotted in the remaining columns of Fig. 3. Column B contains the spectra for the sites at which there was evidence (as discussed above) that the sedimentation rate was nearly constant: sites 659, 664, and 806. Column C contains the data for which the sedimentation rate showed evidence of variability during the 0- to 600-ka interval but for which a minimally tuned time scale was available: sites 552, 607, and Specmap. (By minimally tuned, we mean that the sedimentation rate was tuned, at most, to obliquity and precession, but that there was no 100-ky cycle in the target curve. Such tuning can artificially enhance and narrow the 41- and 23-ky peaks; if done badly, it could destroy

the 100-ky peak, but it is unlikely to artificially narrow the 100-ky peak.) Column D has spectra of data that showed strong evidence for sedimentation rate variability and for which the only time scale that had been published was tuned to a climate model that included eccentricity.

There is a remarkably consistent pattern in the $\delta^{18}\text{O}$ spectral fingerprints in Fig. 3. All show a single narrow peak near frequency 0.01 cycles/ky (period 100 ky), which is similar to the spectrum of the orbital inclination model. None of the spectra show the multiple peak structure expected from the insolation theories. Even the fully tuned data sets in column D, which are suspect because they were tuned to eccentricity, are a better match to the inclination model than to the eccentricity or nonlinear ice models. This evidence suggests that orbital inclination is the primary driving force for the global ice proxy $\delta^{18}\text{O}$ during the past million years, although we cannot rule out a small contribution by eccentricity or precession. Several of the spectra show small peaks near $f = 0.008$ (period 125 ky), which are characteristic of the insolation models, but these peaks have low statistical significance and could be noise fluctuations. None of the $\delta^{18}\text{O}$ data show either the expected doublet (125- and 95-ky periods) or the strong peak near $f = 0.0025$ (400-ky period) that is present in the insolation models. It has been argued that the 400-ky

cycle can be suppressed by the geologic response (35). However, there are at least two other climate records, unrelated to glacial volume, that show the complete triplet structure expected from eccentricity (400-, 125-, and 95-ky peaks): the coarse component (large foraminifera fraction) of sediment at site 806 (29) and Triassic lake-bed depth ranks (36). These examples show that the 400-ky peak is not necessarily suppressed by the Earth response, and so its absence from the $\delta^{18}\text{O}$ record must be considered additional evidence against eccentricity or precession as a driving force for variations in global ice volume. These examples also show that eccentricity and precession do affect other aspects of climate. At site 806, signals from inclination and eccentricity were found to be present simultaneously (29). However, the eccentricity signal was in a proxy thought to be sensitive to local climate (the coarse fraction of the sediment), whereas the inclination signal was in the proxy for global ice fraction ($\delta^{18}\text{O}$).

The shift of the dominant glacial cycle from 41 to 100 ky, which took place about a million years ago, can be understood if the mechanism that links orbital inclination to climate is the accretion of extraterrestrial dust. In 1994, Muller (31) postulated that the sudden onset of the 100-ky cycle might have been caused by an increase in the amount of interplanetary

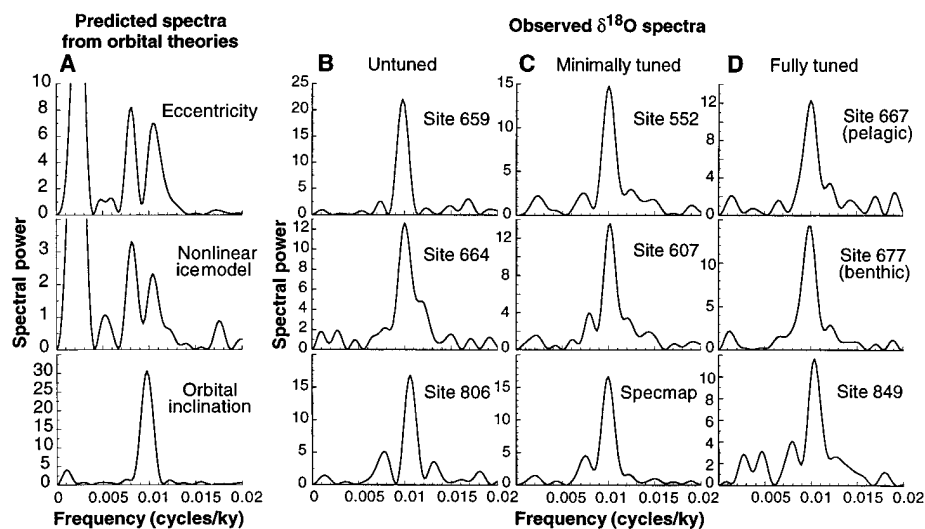


Fig. 3. Spectra of orbital models and of the $\delta^{18}\text{O}$ data (a proxy for global ice) for the interval from 0 to 600 ka. The frequency scale has been expanded to facilitate comparison of peak shapes near 0.01 cycles/ky (period, 100 ky). Column (A) shows spectra of three possible drivers for the glacial data: a linear eccentricity model, a nonlinear ice model that derives the 100-ky signal from the envelope of precession parameter, and an orbital inclination model. The next three columns show the spectral power of $\delta^{18}\text{O}$ data. Column (B) shows data with untuned time scales. Column (C) shows data with minimally tuned time scales (tuned to periods of 41 and 23 ky). Column (D) shows data with fully tuned time scales, that is, the target climate model included an explicit 100-ky eccentricity cycle. All the data show a similar pattern: a single narrow peak near frequency $f = 0.01$ cycles/ky (period, 100 ky), which is in good agreement with the orbital inclination theory and in disagreement with the complex spectra predicted by the eccentricity- and precession-based theories.

dust or meteoroids at that time. An abrupt increase in accreted dust at about 1 Ma was subsequently reported by Farley in a study of ^3He in sediment (37). When accretion was low, the dominant driving force for glaciation was obliquity, perhaps through a Croll/Milankovitch insolation mechanism. After the dust increase, the 41-ky obliquity cycle continued but was obscured under the stronger dust-driven inclination cycles. The strongest cycle predicted by many insolation models has a period of 23 ky. Yet this cycle is weak in all the $\delta^{18}\text{O}$ records we have studied. This cycle would be naturally suppressed, even when insolation is the dominant driving force of glaciation, if ice volume is not particularly sensitive to the north/south land mass asymmetry on Earth. Previous insolation mechanisms could not invoke this suppression because they required a strong precession contribution in order to account for the 100-ky cycle; a cycle we attribute instead to inclination.

One of the predictions of the accretion theory was that 100-ky cycles in dust or meteoric material could be found in sedimentary material or glacial ice, although an initial search failed to achieve sufficient sensitivity (31). To test this prediction, Farley searched for cycles of ^3He in sediment and found the predicted 100-ky cycle, with the times of high accretion being roughly coincident with the interglacials (38). It is possible that the bulk of the dust would have a different phase. The ^3He measurements are sensitive primarily to dust particles with a diameter of about 7 μm , whereas most of the accretion comes from particles larger than 50 μm (39). The orbits of the dust particles depend strongly on size, because their path to Earth is determined primarily by the Poynting-Robertson effect (viscosity from sunlight), and while enroute to Earth, their orbits are perturbed by Jupiter and the other planets.

A narrow ring of dust around the sun was detected by the Infrared Astronomical Satellite (40, 41). This ring is within 1/2 degree of the dust band assumed in the accretion model. According to Dermott *et al.* (42), this dust is continually replenished by collisions among the members of the Themis and Koronis asteroid families. Kortenkamp *et al.* (43) have calculated that most of the extraterrestrial accretion on Earth comes from this narrow solar ring. The event a million years ago that increased the rate of injection of interplanetary dust could have been a particularly disruptive collision in the Themis or Koronis families. According to Kortenkamp *et al.* (43), the cyclicity of accretion observed by Farley is a necessary consequence of the known dust orbits combined

with orbital calculations.

Although the $\delta^{18}\text{O}$ spectra imply that the global ice volume is forced predominantly by orbital inclination and obliquity, other aspects of climate seem to be driven by eccentricity or precession. Thus it appears that glacial cycles are not completely synonymous with climate cycles. It will be a challenge to future geophysical models to account for the dichotomy.

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12. The Blackman-Tukey method obtains the spectral power by first forming the autocorrelation function of the data and then performing a Fourier transform. If only a partial autocorrelation is performed, for example, if the maximum delay is only 1/3 of the time interval of the data set, then we say the "lag" is 1/3. The spectral peak in the lagged analysis is broadened by a factor equal to 1/lag.
13. Spectral power is computed by interpolating the data to equally spaced points, removing the average (but not the trend), using a boxcar window (that is, taking all points equally weighted), and then taking the square of the Fourier transform. The spectrum is normalized to unit mean. The data presented here have also been examined with other spectral methods (such as Blackman-Tukey with various lags, and Lomb-Spergel) and other windows (such as Hanning and Parzen). The conclusions are robust to all data methods, excluding those that significantly degrade the resolution and therefore could not resolve the narrow features from which we draw our conclusions.
14. The background spectral power in the vicinity of this peak is 1.5; the height of the peak is 18.5; this means that the peak is significant at the level of $\exp(-18.5/1.5) = 4 \times 10^{-6}$. Because there are approximately 50 independent frequencies in the plot, the confidence level for this peak is $\text{CL} = 1 - (50)(4 \times 10^{-6}) = 99.98\%$.
15. The age of 1.5 Ma corresponds to an adjusted depth of 66.83 m, and the age of 2.5 Ma corresponds to an adjusted depth of 112.40 m. These give an average sedimentation rate of 45.6 m per million years.
16. The FWHM Δf of the spectral peak that results from calculating the spectral power of a pure sine wave (or any other perfectly periodic signal) of duration T , is $\Delta f = 0.886/T$. This width could be made larger by applying a window to the data (such as a Hanning window) that deemphasizes data at the beginning and end of the interval; the width can be made small-

er by applying a window that emphasizes the two ends of the interval. In this paper we weight all data equally; this is sometimes called a flat or a boxcar window. For a 600-ky interval, the width is $\Delta f = 0.886/600 = 1.5 \times 10^{-3}$ cycles/ky; the separation of the components of the 95/125 eccentricity doublet is significantly larger: 2.5×10^{-3} cycles/ky. For a 900-ky interval, the width is $\Delta f = 9.8 \times 10^{-4}$ cycles/ky.

17. The frequency of oscillation is $f = 1/P$, where P is the period; the FWHM is $\Delta f = 0.886/T$, where T is the duration of the interval. Therefore the fractional width is $\Delta f/f = (0.886/T)P = 0.886/N$, where $N = T/P$ is the number of cycles in the interval T .
18. The response may have a different phase than the driving force, but it has the same frequency, even if several resonances are present. For a simple introduction to some of the properties of forced and free oscillations, see J. B. Marion and S. T. Thornton, *Classical Dynamics of Particles and Systems* (Harcourt Brace Jovanovich, New York, 1988).
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44. We thank W. Alvarez and the Renaissance Geology Group for many stimulating discussions, and M. Raymo, W. Berger, M. Yasuda, P. Olsen, and S. Clemens for providing data in digital form. Additional data were obtained over the World Wide Web from the site maintained by the National Oceanic and Atmospheric Administration at www.ngdc.noaa.gov. Supported in part by the Department of Energy (under contract DE-AC03-7bSF00098) and by the Ann and Gordon Getty Foundation.

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