

# VNA-Based Material Characterization in THz Domain without Classic Calibration and Time-Gating

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**Abstract**— A method is presented to measure materials and extract the complex permittivity without using classic VNA calibrations and time-gating. It is based on normalization to a "Thru" connection and analyzing error-terms and multiple-reflection phenomena. Measurement results (in free-space) are presented in 75-110 GHz and 500-750 GHz bands. Normalization technique can reduce the overall measurement uncertainties and simplify the material characterization process.

**Index Terms**— Material characterization, parameter extraction, VNA time-gating, RF metrology, measurement uncertainty.

## I. INTRODUCTION

Free-space calibration techniques are complicated in THz domain because of precise-positioning challenges and lack of reliable Short and Line standards. Actually, non-perfect calibration together with time-gating attribute more uncertainties to the final extracted material parameters. Here, we try to use a simple normalization process, analyze/correct the error-terms and then reduce the standing-waves effects. Fig. 1 shows VNA measurement error-terms and the relations between  $S_{\text{(measured)}}$  and  $S_{\text{DUT}}$ .

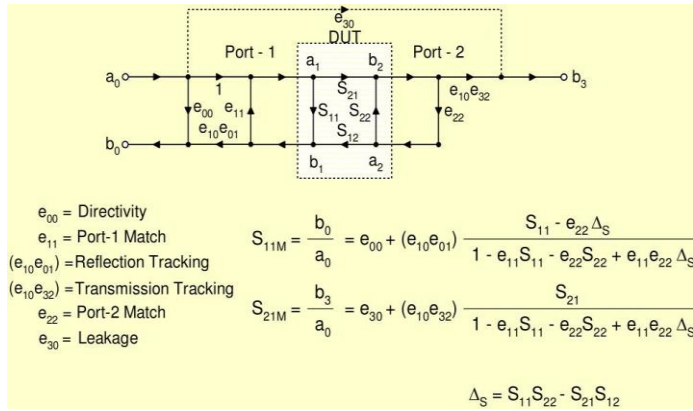


Fig. 1. VNA measured S-parameters ( $S_{ij,M}$ ), error-terms ( $e_{ij}$ ) and DUT S-parameters ( $S_{ij}$ ) (courtesy to IEEE-MTT Society).

Ignoring the leakage-term and assuming for DUT ( $S_{21,DUT}$ ,  $S_{11}=S_{22}$ ) and Thru-connection ( $S_{21}=S_{12}=1$ ,  $S_{11}=S_{22}=0$ ), yield:

$$\rightarrow S_{21}(DUT) = \frac{S_{21,M}(DUT)}{S_{21,M}(Thru)} \times \frac{1 - e_{11}e_{22}}{1 + e_{11}e_{22}(S_{11}^2 - S_{21}S_{21}) - S_{11}(e_{11} + e_{22})} \quad (1)$$

we can analyze the error-terms of Eq. 1 by looking at the Fabry-Perot effects inside a material-slab (MUT). If the material is not very lossy,  $|S_{21}|_{\text{max.}}$  and  $|S_{11}|_{\text{min.}}$  occur simultaneously [1] at the frequency-points for which  $\phi(S_{21}) = n\pi$ . Therefore, at  $|S_{11}|_{\text{min.}}$  ( $|S_{21}|_{\text{max.}} \approx 1$  &  $|S_{11}|_{\text{min.}} \approx 0$ , for low-loss materials):

$$\rightarrow S_{21}(MUT) = \frac{S_{21,M}(MUT)}{S_{21,M}(Thru)} \frac{1 - e_{11}e_{22}}{1 - e_{11}e_{22}(S_{21}S_{21})} \quad (2)$$

As deduced from Eq. 2, error-terms and system multiple-reflection on  $S_{21}(MUT)$  all approximately vanish for  $|S_{21}|_{\text{max.}}$  &  $\phi(S_{21})=n\pi$  points. This is demonstrated for two low-loss materials (Fig. 2: Pyrex and Quartz, 500-750 GHz).

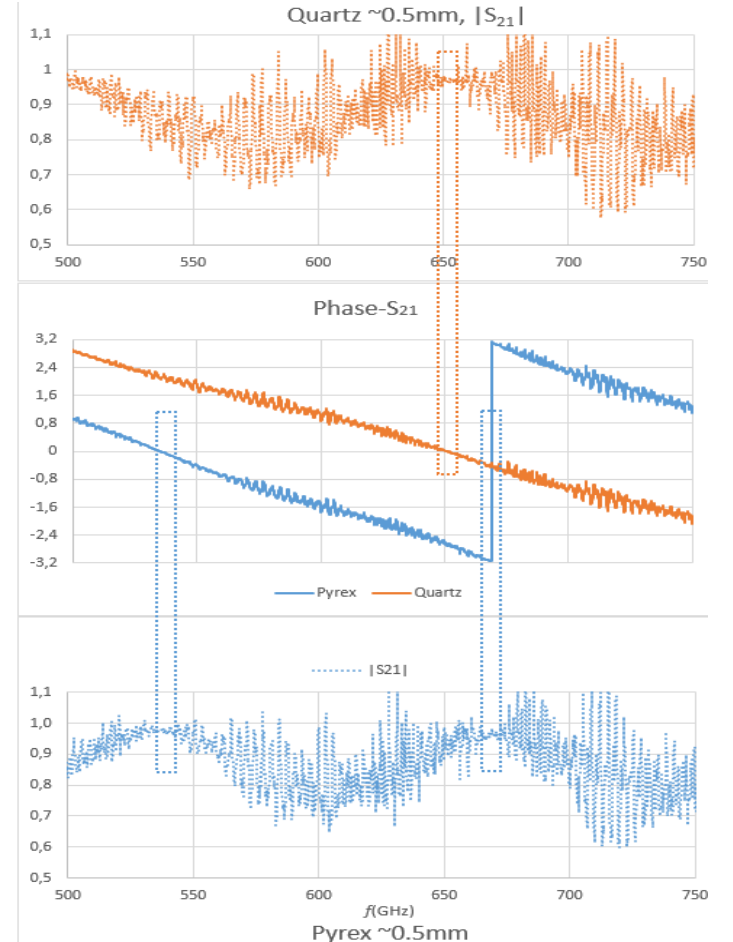


Fig. 2. Normalized  $S_{21}(MUT)$ : Pyrex and Quartz, 500-750GHz.

Actually, reliable results of  $S_{21}$  even for a limited number of points in a given frequency-range are of interest. "Normal" homogeneous materials have nearly constant permittivity (slight rising of imaginary-part with the frequency) in mm-wave/THz domain. Permittivity can be extracted at "best" points of  $S_{21}$  (phase and amplitude) using relevant extraction methods [2]. Fig. 3 show the results for a low-loss material (Quartz) and a thicker slab of Plexiglass. The free-space mode-converter here is Swissto12-MCK@ set of two corrugated horn antennas. The device is supposed to convert waveguide propagation modes to TEM on its aperture where the MUT is installed.

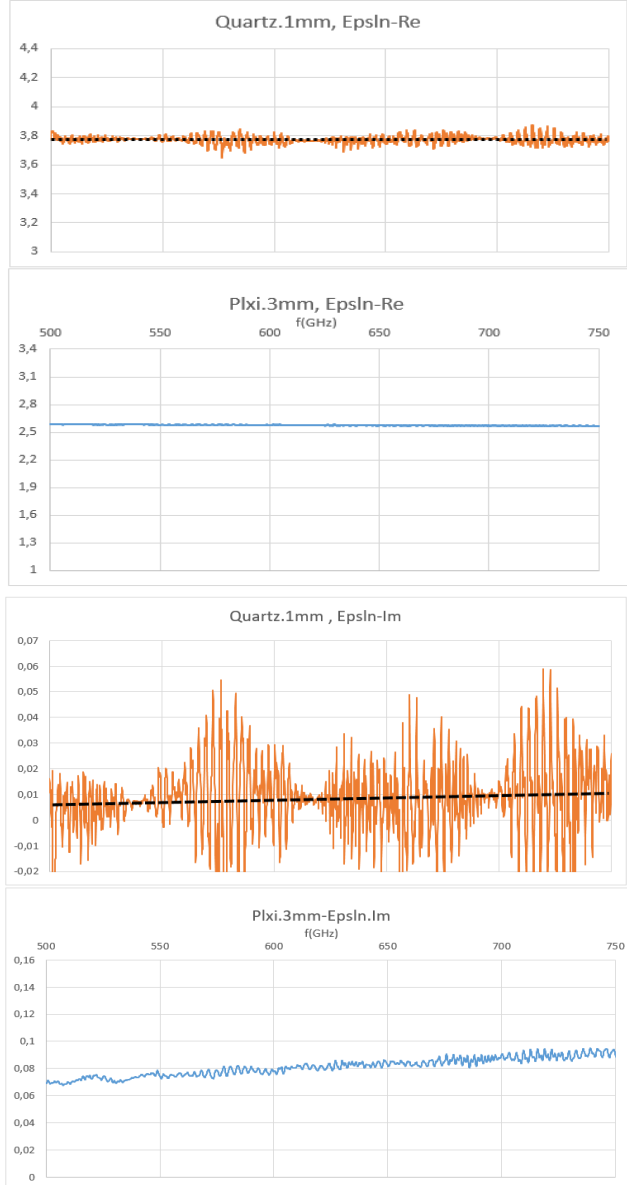


Fig. 3. Permittivity (Epsilon real & imaginary parts) of Plexiglass-3mm and Quartz-1 mm, 500-750 GHz.

As shown in Fig. 3, for a thicker material which is not very low-loss (Plexiglass, for example) multiple-reflection effects are less apparent because of energy damping in the MUT.

## II. REDUCING MULTIPLE-REFLECTION EFFECTS

From the VNA error-terms (Eq. 1-2), we can see  $S_{11}(\text{DUT})$  and " $e_{11} + e_{22}$ " have the most important roles.  $S_{11}(\text{DUT})$  can be reduced over the whole frequency-range (from the VNA point-of-view) by tilting the MUT slab. Meanwhile, inserting low-reflection absorbers will decrease " $e_{11} + e_{22}$ ".

Besides, we are working on some new techniques based on "standard-known" material instead of classic "Line" that can help to calculate " $e_{11} + e_{22}$ ", directly. A thin slab of low-loss materials (HR-Si, Quartz, Alumina ...) can be characterized as the "standard-known" load (the "best points" of  $S_{21}$  are enough in this case), and used as "Line" to calculate the error-terms.

The above-mentioned methods have been successfully tested for the 75-110 GHz band (Fig. 4), and are in progress for the 500-750 GHz frequency-range.

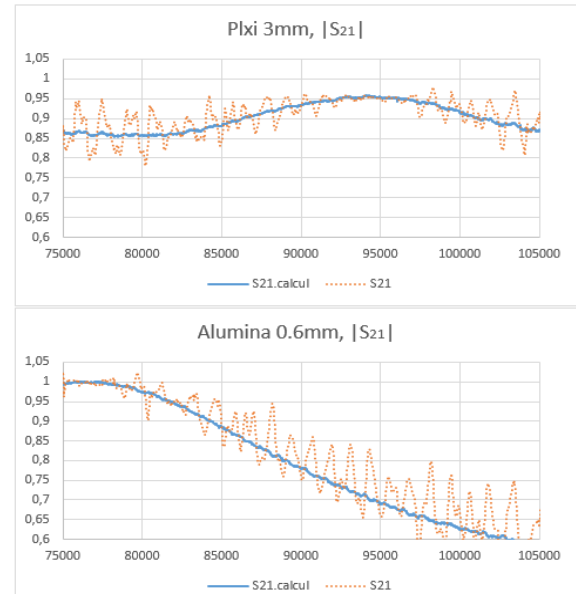


Fig. 4. Methods to reduce the multiple reflections,  $S_{21}|_{\text{normalized raw}}$  and corrected: 75-110 GHz, Alumina-0.6mm and Plexiglass-3mm.

## ACKNOWLEDGEMENT

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