

$$g_{ij} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$a = a^x \mathbf{e}_x + a^y \mathbf{e}_y + a^z \mathbf{e}_z$$

$$b = b^x \mathbf{e}_x + b^y \mathbf{e}_y + b^z \mathbf{e}_z$$

$$a \bar{\times} b = a^x b^x + a^y b^y + a^z b^z$$

$$a \times b = (a^x b^y - a^y b^x) \mathbf{e}_x \wedge \mathbf{e}_y + (a^x b^z - a^z b^x) \mathbf{e}_x \wedge \mathbf{e}_z + (a^y b^z - a^z b^y) \mathbf{e}_y \wedge \mathbf{e}_z$$

$$A = A^{xy} \mathbf{e}_x \wedge \mathbf{e}_y + A^{xz} \mathbf{e}_x \wedge \mathbf{e}_z + A^{yz} \mathbf{e}_y \wedge \mathbf{e}_z$$

$$B = B^{xy} \mathbf{e}_x \wedge \mathbf{e}_y + B^{xz} \mathbf{e}_x \wedge \mathbf{e}_z + B^{yz} \mathbf{e}_y \wedge \mathbf{e}_z$$

$$A \bar{\times} B = -A^{xy} B^{xy} - A^{xz} B^{xz} - A^{yz} B^{yz}$$

$$A \times B = (-A^{xz} B^{yz} + A^{yz} B^{xz}) \mathbf{e}_x \wedge \mathbf{e}_y + (A^{xy} B^{yz} - A^{yz} B^{xy}) \mathbf{e}_x \wedge \mathbf{e}_z + (-A^{xy} B^{xz} + A^{xz} B^{xy}) \mathbf{e}_y \wedge \mathbf{e}_z$$