

$$g = \begin{bmatrix} 1 & (e_E \cdot e_B) & (e_E \cdot e_k) & 0 \\ (e_E \cdot e_B) & 1 & (e_B \cdot e_k) & 0 \\ (e_E \cdot e_k) & (e_B \cdot e_k) & 1 & 0 \\ 0 & 0 & 0 & -1 \end{bmatrix}$$

$$X = x_E \mathbf{e}_E + x_B \mathbf{e}_B + x_k \mathbf{e}_k + t \mathbf{e}_t$$

$$K = k \mathbf{e}_k + \omega \mathbf{e}_t$$

$$K \cdot X = (e_B \cdot e_k) k x_B + (e_E \cdot e_k) k x_E - \omega t + k x_k$$

$$F = (e_B \cdot e_k) B e^{i((e_B \cdot e_k) k x_B + (e_E \cdot e_k) k x_E - \omega t + k x_k)} \mathbf{e}_E \wedge \mathbf{e}_B - B e^{i((e_B \cdot e_k) k x_B + (e_E \cdot e_k) k x_E - \omega t + k x_k)} \mathbf{e}_E \wedge \mathbf{e}_k + E e^{i((e_B \cdot e_k) k x_B + (e_E \cdot e_k) k x_E - \omega t + k x_k)} \mathbf{e}_E \wedge \mathbf{e}_t + (e_E \cdot e_B) B e^{i((e_B \cdot e_k) k x_B + (e_E \cdot e_k) k x_E - \omega t + k x_k)} \mathbf{e}_B \wedge \mathbf{e}_k$$

$$\text{Substituting } e_E \cdot e_B = e_E \cdot e_k = e_B \cdot e_k = 0$$

$$g = \begin{bmatrix} 1 & (e_E \cdot e_B) & (e_E \cdot e_k) & 0 \\ (e_E \cdot e_B) & 1 & (e_B \cdot e_k) & 0 \\ (e_E \cdot e_k) & (e_B \cdot e_k) & 1 & 0 \\ 0 & 0 & 0 & -1 \end{bmatrix}$$

$$X = x_E \mathbf{e}_E + x_B \mathbf{e}_B + x_k \mathbf{e}_k + t \mathbf{e}_t$$

$$K = k \mathbf{e}_k + \omega \mathbf{e}_t$$

$$K \cdot X = (e_B \cdot e_k) k x_B + (e_E \cdot e_k) k x_E - \omega t + k x_k$$

$$\text{Substituting } e_E \cdot e_B = e_E \cdot e_k = e_B \cdot e_k = 0$$