

1 **Title:** Does phenology explain plant-pollinator interactions at different latitudes? An assessment of its  
2 explanatory power in plant-hoverfly networks in French calcareous grasslands

3 **Authors:** Natasha de Manincor<sup>1\*</sup>, Nina Hautekeete<sup>1</sup>, Yves Piquot<sup>1</sup>, Bertrand Schatz<sup>2</sup>, Cédric  
4 Vanappelghem<sup>3</sup>, François Massol<sup>1,4</sup>

5 <sup>1</sup>Université de Lille, CNRS, UMR 8198 - Evo-Eco-Paleo, F-59000 Lille, France

6 <sup>2</sup>CEFE, EPHE-PSL, CNRS, University of Montpellier, University of Paul Valéry Montpellier 3, IRD,  
7 Montpellier, France

8 <sup>3</sup>Conservatoire d'espaces naturels Nord et du Pas-de-Calais, 160 rue Achille Fanié - ZA de la Haye,  
9 62190 LILLERS

10 <sup>4</sup>Univ. Lille, CNRS, Inserm, CHU Lille, Institut Pasteur de Lille, U1019 - UMR 8204 - CIIL - Center for  
11 Infection and Immunity of Lille, F-59000 Lille, France

12

13 E-mail addresses and ORCID numbers:

14 Natasha de Manincor: [natasha.de-manincor@univ-lille.fr](mailto:natasha.de-manincor@univ-lille.fr), 0000-0001-9696-125X

15 Nina Hautekeete: [nina.hautekeete@univ-lille.fr](mailto:nina.hautekeete@univ-lille.fr), 0000-0002-6071-5601

16 Yves Piquot: [yves.piquot@univ-lille.fr](mailto:yves.piquot@univ-lille.fr), 0000-0001-9977-8936

17 Bertrand Schatz: [bertrand.schatz@cefe.cnrs.fr](mailto:bertrand.schatz@cefe.cnrs.fr), 0000-0003-0135-8154

18 Cédric Vanappelghem: [cedric.vanappelghem@espaces-naturels.fr](mailto:cedric.vanappelghem@espaces-naturels.fr)

19 François Massol: [francois.massol@univ-lille.fr](mailto:francois.massol@univ-lille.fr), 0000-0002-4098-955X

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24 \*Corresponding author information: Natasha de Manincor, e-mail: [natasha.de-manincor@univ-lille.fr](mailto:natasha.de-manincor@univ-lille.fr),

25 phone: +330362268530

26 **Author contributions**

27 NDM and FM conceived the project, formulated and implemented the model. NDM conducted the  
28 analysis and prepared the manuscript. FM supervised the analysis and edited the manuscript. NH, YP,  
29 CV and BS contributed substantially to all later versions. NDM, NH, YP and BS conducted the fieldwork  
30 and provided the data. CV identified the hoverflies.

31 **Data accessibility**

32 The data supporting the results are archived on Zenodo (DOI: [10.5281/zenodo.2542845](https://doi.org/10.5281/zenodo.2542845)).

33

34 **Abstract**

35 For plant-pollinator interactions to occur, the flowering of plants and the flying period of pollinators  
36 (*i.e.* their phenologies) have to overlap. Yet, few models make use of this principle to predict  
37 interactions and fewer still are able to compare interaction networks of different sizes. Here, we  
38 tackled both challenges using Bayesian Structural Equation Models (SEM), incorporating the effect of  
39 phenology overlap in six plant-hoverfly networks. Insect and plant abundances were strong  
40 determinants of the number of visits, while phenology overlap alone was not sufficient, but  
41 significantly improved model fit. Phenology overlap was a stronger determinant of plant-pollinator  
42 interactions in sites where the average overlap was longer and network compartmentalization was  
43 weaker, *i.e.* at higher latitudes. Our approach highlights the advantages of using Bayesian SEMs to  
44 compare interaction networks of different sizes along environmental gradients and articulates the  
45 various steps needed to do so.

46

## 47 INTRODUCTION

48 Understanding how phenology determines species interactions is a central question in the case of  
49 mutualistic networks. In plant-pollinator networks, phenology shapes their temporal and spatial limits,  
50 thus defining the area and the period along the season in which interactions preferably occur (Olesen  
51 *et al.* 2011; Ogilvie & Forrest 2017). Since plant and pollinator phenologies are not equally affected by  
52 changes in environmental cues, partial or total phenological mismatches can occur as a result of  
53 environmental changes such as climate change (Parmesan 2007; Rafferty 2017). Phenological  
54 advances indeed increase at higher latitudes, as a response to the acceleration of warming  
55 temperature along the same gradient (Post *et al.* 2018), increase phenological mismatch, and have the  
56 potential to threaten the synchrony needed for effective pollination (Hutchings *et al.* 2018). Such  
57 environmental changes can thus drastically alter pollinator interactions through modified temporal  
58 overlap between pollinators and their floral resources leading, in extreme cases, to local extinctions  
59 (Memmott *et al.* 2007) and the ensuing absence of the partner species at the location and/or time at  
60 which the interaction should have taken place (Willmer 2012; Miller-Struttmann *et al.* 2015; Rafferty  
61 *et al.* 2015; Hutchings *et al.* 2018).

62 Because phenological match is crucial to plant-pollinator interactions, and thus ultimately to  
63 pollinators' fitness, pollinators have to adapt to phenological shifts either through interaction with  
64 other plant species (Rafferty *et al.* 2015) or through changes of their own phenology (Bartomeus *et al.*  
65 2011). Phenology can then influence dynamical network properties, such as the stability and the  
66 coexistence of species, through changes in network topology (Encinas-Viso *et al.* 2012). Moreover,  
67 phenology predictably affects network compartmentalization as different phenophases likely  
68 correspond to different compartments when networks are considered on an annual scale (Martín  
69 González *et al.* 2012).

70 Despite considerable theoretical advances, there are few models available to predict the probability  
71 of interaction in plant-pollinator networks (Staniczenko *et al.* 2017; Cirtwill *et al.* 2019) and fewer still

72 able to make comparisons between networks. Due to their complexity and variation among years  
73 (Chacoff *et al.* 2017), most studies of mutualistic networks have focused on predicting and comparing  
74 classic network metrics (nestedness, connectance, modularity, etc.) which are all influenced by  
75 network size, *i.e.* the number of plant and insect species (Fortuna *et al.* 2010; Staniczenko *et al.* 2013;  
76 Poisot & Gravel 2014; Astegiano *et al.* 2015). Moreover, few studies have compared interaction  
77 networks along environmental gradients (Devoto *et al.* 2005; Schleuning *et al.* 2012; Sebastián-  
78 González *et al.* 2015; Pellissier *et al.* 2017). In order to compare networks of different sizes, a better  
79 alternative is to switch from network-derived metrics to the comparison of the probability of  
80 interaction given by regression models, which can consider multiple factors and latent variables and  
81 assume that the sampled data are just part of a larger unobserved dataset (Grace *et al.* 2010).

82 Calcareous grasslands are characterized by highly diverse plant communities with a high proportion of  
83 entomophilous species (Baude *et al.* 2016), thus they are a convenient model for such studies. Most  
84 plant-insect pollinator networks involve bee species (Anthophila), but recent studies have also pointed  
85 out the importance of hoverflies (Diptera: Syrphidae), which pollinate a large spectrum of wild  
86 flowering species (Klecka *et al.* 2018a) and crops (Jauker & Wolters 2008; Rader *et al.* 2011). They  
87 usually behave opportunistically, *i.e.* from being pollen generalists to specialists, only limited by  
88 morphological constraints (Iler *et al.* 2013; Klecka *et al.* 2018a; Lucas *et al.* 2018). Indeed, their  
89 generalist behaviour, at the species level, could be the result of individually specialized diets, since  
90 most pollen retrieved on hoverfly individuals usually comes from a single plant taxon (Lucas *et al.* 2018)  
91 and depends on flower availability and phenology (Cowgill *et al.* 1993; Colley & Luna 2000; Lucas *et al.*  
92 2018). Moreover, some hoverflies have preferences regarding plant colour, morphology and  
93 inflorescence height (Branquart & Hemptinne 2000; Colley & Luna 2000; Lunau 2014; Klecka *et al.*  
94 2018b, a).

95 Here we study the consequences of environmental gradients on plant-pollinator interactions, focusing  
96 on how phenology overlap affects interactions between plants and insects in six calcareous grassland

97 sites distributed along a latitudinal gradient. We obtained plant and insect phenologies, abundances,  
98 and interactions in all sites from April to October 2016. We modelled plant-pollinator interaction  
99 networks following a Bayesian Structural Equation Modelling approach (SEM) using latent variables,  
100 *i.e.* unobserved variables (Grace *et al.* 2010). SEM is a multivariate technique used to test several  
101 hypotheses in ecological studies. SEM analysis involves cause-effect equations to evaluate multiple  
102 causal relationship (Grace 2006; Eisenhauer *et al.* 2015) using observed and latent variables to explain  
103 some other observed variables (Grace 2006). SEM can be used to choose among competing models  
104 (Grace & Bollen 2008). Thus, SEM are well suited for studying the complexity of ecological networks.  
105 To test whether phenology affects network compartmentalization, we looked for species subgroups  
106 using a latent block model (LBM) which is among the best clustering methods for weighted networks  
107 (Leger *et al.* 2015).

108 The comparison of 16 SEMs and the analysis of LBMs of sampled networks evinced that phenology  
109 overlap is an important determinant of plant-pollinator interactions, but is less informative than  
110 species abundances and performs heterogeneously among sites. Our results suggest that the use of  
111 SEMs to compare networks of different sizes along an environmental gradient is an innovative  
112 approach which can help understand the structure of plant-pollinator networks.

## 113 **MATERIALS AND METHODS**

### 114 Study sites

115 We sampled plant and hoverfly species in six areas (Fig. S1) of 1 hectare each in different French  
116 regions: two sites in Hauts-de-France (Les Larris de Grouches-Luchuel, thereafter noted LAR,  
117 50°11'22.5"N 2°22'02.9"E and Regional natural reserve Riez de Noeux les Auxi, noted R, 50°14'51.85"N  
118 2°12'05.56"E, in départements Pas-de-Calais and Somme), two sites in Normandie (Château Gaillard –  
119 le Bois Dumont, noted CG, 49°14'7.782"N 1°24'16.445"E and les Falaises d'Orival, noted FAL,  
120 49°04'40.08"N 1°33'07.254"E, départements: Eure and Seine Maritime) and two sites in Occitanie  
121 (Fourches, noted F, 43°56'07.00"N 3°30'46.1"E and Bois de Fontaret, noted BF, 43°55'17.71"N

122 3°30'06.06"E, département: Gard). The six sites are included in the European NATURA 2000 network, a  
123 network of preserved areas designated to protect a number of habitats and species representative of  
124 European biodiversity. The four sites in Hauts-de-France and Normandie are managed by the  
125 Conservatoire d'espaces naturels of Normandie, Picardie and Nord – Pas-de-Calais and the sites in  
126 Occitanie by the CPIE Causses méridionaux. We sampled each site once a month from April to October  
127 2016, except for the site of Riez that was sampled from May to October.

#### 128 Plant-hoverfly observations and sampling

129 To collect information at the community level, in each site and at each session we realized: (i) a botanic  
130 inventory of the flowering species, recorded their abundances and the total flower covering in the area  
131 and (ii) a pollinator sampling using a hand net along a variable transect walk.

132 Flowering plants were identified at the species level. We recorded the abundances of all flowering  
133 species. At first, we estimated the total percentage of surface covered by all flowering species in the  
134 selected area. We then estimated the relative abundance of each flowering species. We used Braun-  
135 Blanquet coefficients of abundance-dominance, ranked from i to 5 (most abundant coefficient class)  
136 (Van Der Maarel 1975, 1979; Mucina *et al.* 2000), to rank flowering species. We converted the  
137 coefficients to percentage intervals and then in mean values of percentage cover classes (Table S1):  
138 coefficient **5** = 75-100%, coeff **4** = 50-75%, coeff **3**=25-50%, coeff **2** = 10-25%, coeff **1** = 1-10%, coeff **+**  
139 = few individuals less than < 1%, coeff **i** = 1 individual. All inventories were realized by the same  
140 surveyors to avoid biases.

141 Pollinator observations were performed by the same team of 3-5 persons each day. The surveyors  
142 walked slowly around any potential attractive resource patch included in the selected 1-hectare area  
143 for 4h each day. We split the sampling period into 2 hours in the morning (about 10-12h) and 2 hours  
144 in the afternoon (about 14-16h) to cover the daily variability of both pollinator (bees and hoverflies,  
145 which are more active in the morning than in the afternoon; D'Amen *et al.* 2013) and flower  
146 communities. Sampling took place when we had suitable weather conditions for pollinators (following

147 Westphal *et al.* 2008). We sampled all flower-visiting insects and we recorded observed interactions.  
148 All sampled insects were immediately put individually in a killing vial with ethyl acetate and were later  
149 prepared and pinned in the laboratory and identified at the species level by expert taxonomists. Even  
150 if we collected both bees and hoverflies, in this study we focus on hoverflies only (since at the moment  
151 of the study bees were not identified at the species level yet). Overall, we sampled for 41 days,  
152 equivalent to about 164 hours in the field (all the surveyors collected at the same time). For all analyses  
153 described here, we only used the list of visited herbaceous plant species and hoverflies which were  
154 found visiting a plant. Despite their rarity and even if hoverflies are known to prefer open flowers  
155 (Branquart & Hemptinne 2000), we also considered the interactions between hoverflies and plant  
156 species of the Fabaceae family because we observed in the field that they visited Fabaceae species  
157 that were already opened by other insects, *e.g.* by large bee species, such as *Eucera* sp. (de Manincor,  
158 personal observation).

#### 159 Plant – hoverfly networks

160 For each site, we constructed an interaction network consisting of all pairs of interacting plant and  
161 insect species, pooling data from all months. A pair of species ( $i,j$ ) was connected with intensity  $v_{ij}$  when  
162 we recorded  $v_{ij}$  visits of insect species  $i$  on plant species  $j$  in the site. We calculated the network  
163 specialization index,  $H2'$  (Blüthgen *et al.* 2006) using the `H2fun` function implemented in the  
164 `bipartite` package (Dormann *et al.* 2009; R Core Team 2018). We obtained the  $d$ -value (Kullback-  
165 Leibler divergence between the interactions of the focal species and the interactions predicted by the  
166 weight of potential partner species in the overall network) and the  $d_{max}$ -value (maximum  $d$ -value  
167 theoretically possible given the observed number of interactions in the network) using the `dfun`  
168 function in the `bipartite` package (Dormann *et al.* 2009). We did not use the  $d'$  values provided by  
169 this package as they sometimes yielded spurious results based on the computation of the minimal  $d$   
170 value (*e.g.* reporting low  $d'$  for species with only one partner in the network). We then manually

171 calculated the standardized specialization index  $d'$  (Blüthgen *et al.* 2006) for each plant and insect  
172 species as the ratio of the  $d$ -value to its corresponding  $d_{max}$ -value.

173 We calculated the modularity of the network and the associated partition of species into modules  
174 using the `cluster_leading_eigen` method for modularity optimization implemented in the  
175 `igraph` package (Csardi & Nepusz 2006; Newman 2006). Modularity optimization can help identify  
176 strong, simple divisions of a network into relatively independent sub-networks by looking for highly  
177 interconnected sub-networks. However, modules are not meant to inform about more subtle  
178 groupings among the species, *e.g.* particular avoidance of interactions between insects of group A and  
179 plants of group 1. In order to detect such groups, we implemented latent block models (LBM) using  
180 the `BM_poisson` method for Poisson probability distribution implemented in the `blockmodels`  
181 package (Leger *et al.* 2015). Blocks are calculated separately for the two groups (insect and plant) based  
182 on the number of visits (*i.e.* a weighted network). The algorithm finds the best divisions of insects and  
183 plants through fitting one Poisson parameter in each block of the visit matrix, thus essentially  
184 maximizing the ICL (Integrated Completed Likelihood; Biernacki *et al.* 2000; Daudin *et al.* 2008). The  
185 LBM script is given in Supplementary Information (Appendix S3). All analyses were performed in R  
186 version 3.3.3 (R Core Team 2018).

#### 187 Plant and hoverfly abundances and phenology overlap

188 We calculated plant abundance using information about the abundance-dominance recorded in the  
189 field following the methodology of Braun-Blanquet presented above. We transformed the coefficients  
190 of abundance in percentages (Table S1): we used the mean of the percentage corresponding to each  
191 class. We then calculated the relative abundance ( $A_P$ ) of each flowering plant species as the ratio of  
192 the focal species cumulated abundance to total flower abundance during its flowering season. For  
193 hoverflies, we used the recorded number of visiting individuals (total abundance) and their presence  
194 (recorded months) along the season to calculate their average abundance during months when they  
195 were present ( $A_H$ ).

196 We refer to plant phenology as their flowering period and insect phenology as the flying period. We  
197 considered only flowering plants which had been visited by pollinators. For the pollinators, we  
198 considered only hoverflies which were found in interaction. To build the species phenology tables for  
199 both plants and hoverflies, we merged the information provided by two sources of data (field data and  
200 the literature): we used the observed phenology of both plants and insects during the field session as  
201 the only source of information for plants (plants visited by insects and plants found in the botanic  
202 inventory in the site at that date), and we complemented the hoverfly phenology with information  
203 provided by the Syrph the Net Database (Speight *et al.* 2016). We then built the phenology overlap  
204 (PO) matrix based on the species phenology tables by calculating the number of phenologically active  
205 months that are shared by each pair of insect and plant species along the season.

#### 206 Bayesian Structural Equation Modelling (SEM)

207 SEM is a confirmatory technique that involves cause-effect equations to evaluate multivariate  
208 hypotheses in ecological networks (Grace 2006). The primary interest of SEM analyses lies in its ability  
209 to compare different causal models between the same sets of explanatory and explained variables.  
210 Another important feature of SEM is that they can relate data through latent variables, *i.e.* variables  
211 which are not measured in the model and which represent underlying causes or effects, coupled with  
212 observed variables (Grace 2006; Grace *et al.* 2010). SEM can now be assessed using Bayesian  
213 approaches and parameters estimated using MCMC (Markov Chain Monte Carlo)(Grace *et al.* 2010;  
214 Fan *et al.* 2016).

215 In our study, we modelled hoverfly-plant interaction networks using a SEM approach (Fig. 1) with latent  
216 variables linking the number of visits per plant-pollinator species pair to abundance and phenology  
217 overlap (PO) data through a first latent table representing probabilities of interactions, another latent  
218 table representing the possible interactions between plant and pollinators (as a realization of the  
219 aforementioned interaction probability matrix), and a third latent table yielding the expected number  
220 of visits per plant-pollinator species pair (*i.e.* the intensity of interactions). We used the term latent

221 tables to describe latent variables organized as insect x plant tables, such as the expected number of  
222 visit matrix.

223 In this model, we considered that PO had an effect on possible interactions ( $I_{ij}$ ) and the number of visits  
224 ( $\lambda_{ij}$ ) – a longer overlap is intuitively expected to drive a higher probability of interaction and a larger  
225 number of visits. Interaction probabilities were also assumed to depend on two random effects (plant  
226 and insect species identities,  $E_i$  and  $E_j$ ), to represent heterogeneity of species degrees (*i.e.* the number  
227 of links) in the network. We modelled the possibility of interaction  $I_{ij}$  between insect species  $i$  and plant  
228 species  $j$  (*i.e.*  $I_{ij} = 1$  when species  $i$  and  $j$  can interact) as a Bernoulli random variable of probability  $\mu_{ij}$   
229 given by:

$$230 \quad \text{logit}(\mu_{ij}) = \mu_0 + \mu_{PO}PO_{ij} + E_i + E_j$$

231 where logit is the usual logistic transformation ( $\log(x/(1-x))$ ),  $\mu_0$  is the intercept of this relation,  $\mu_{PO}$  is  
232 the coefficient measuring the effect of PO, and  $E_i$  and  $E_j$  are the random effects associated with insect  
233 species  $i$  and plant species  $j$  respectively.

234 The number of visits  $V_{ij}$  was assumed to depend on plant and hoverfly abundances, as more abundant  
235 species are expected to be more often sampled (and thus more often recorded “in interaction”). Please  
236 note that we only linked abundances to the number of visits,  $V_{ij}$ , and not to the possibility of interaction  
237  $I_{ij}$ , because the aim of the latter latent table is to capture “forbidden links”, while detectability and  
238 sampling effects are supposed to be captured by the statistical model of the number of interactions.  
239 We integrated species abundances as predictor variables in order to assess the effect of PO on the  
240 number of visits on top of a “null model” that already includes sensible drivers of the numbers of visits,  
241 such as species abundances.  $V_{ij}$  was modelled as a Poisson random variable to allow for sampling  
242 variability, with a conditional mean  $\lambda_{ij}$  (the intensity of visits that can occur) given by:

$$243 \quad \log(\lambda_{ij}) = \lambda_0 + \lambda_H A_{H,i} + \lambda_P A_{P,j} + \lambda_{PO} \log(1 + PO_{ij})$$

244 where  $\lambda_0$  is the intercept of this relation,  $\lambda_H$  is the coefficient measuring the effect of hoverfly  
245 abundance  $A_H$ ,  $\lambda_P$  is that of plant abundance  $A_P$ , and  $\lambda_{PO}$  is the coefficient of the effect of PO.

246 Possible interactions ( $I_{ij}$ ) and the intensity of visits ( $\lambda_{ij}$ ) are multiplied to obtain the unconditional mean  
247 number of recorded visits, *i.e.*  $V_{ij}$  is then obtained as a Poisson draw of mean  $I_{ij} \lambda_{ij}$ .

248 Overall we estimated four main parameters: the effect of phenology overlap on the probability of  
249 interaction ( $PO \rightarrow I_{ij}, \mu_{PO}$ ), the effect of phenology overlap on the intensity of interactions ( $PO \rightarrow \lambda_{ij},$   
250  $\lambda_{PO}$ ), the effect of plant abundance on the intensity of interactions ( $A_P \rightarrow \lambda_{ij}$ , coefficient  $\lambda_P$ ) and the  
251 effect of insect (hoverflies) abundance on the intensity of interactions ( $A_H \rightarrow \lambda_{ij}, \lambda_H$ ).

252 We used the `jags` function (R2jags package), which provides an interface from R to the JAGS library  
253 for Bayesian data analysis, to estimate model parameters. JAGS (Plummer 2003) uses a Markov Chain  
254 Monte Carlo algorithm to generate samples from the posterior distribution of the parameters. We ran  
255 two Markov chains with  $10^6$  iterations per chain to check for model convergence. The code of the  
256 model is given in Supplementary Material (Appendix S1 and S2).

### 257 Model and parameter comparison

258 We estimated the 16 models that included all combinations of 0 and 4 of the above-mentioned effects  
259 to understand which effects were more likely to play a role in the structuring of the network. The  
260 goodness-of-fit of these models were compared using the leave-one-out cross-validation criterion  
261 (LOO) calculated using the R package `loo` using Pareto smoothed importance sampling for regularizing  
262 importance weights (Vehtari *et al.* 2017). The LOO criterion is a fully Bayesian method to compare  
263 models of different complexities and to estimate prediction accuracy using the log-likelihood  
264 evaluated at the posterior simulations of the parameter values (Vehtari *et al.* 2017). Models can thus  
265 be ranked according to their LOO scores, with the best model being the one with the lowest LOO value.  
266 The LOO criterion is analogous to the classic Akaike and Bayesian Information Criteria, which are used  
267 to compare frequentist models, but can instead be applied to Bayesian models, without suffering the

268 instability issues of the Deviance Information Criterion which used to be the main information criterion  
269 for Bayesian models (Vehtari *et al.* 2017). To rank the models, we then calculated the  $\Delta LOO$  (noted  $\Delta_i$ )  
270 as  $\Delta_i = LOO_i - LOO_{min}$  (following Burnham & Anderson 2004), where  $LOO_{min}$  is the minimum of the  $LOO_i$   
271 values among the 16 models. We used  $\Delta_i$  to obtain model weights  $\omega_i$ , following the Akaike weight  
272 methodology (Burnham & Anderson 2002):

$$273 \quad \omega_i = \frac{e^{-\Delta_i/2}}{\sum e^{-\Delta_i/2}}$$

274 We then summed weights ( $w_H$ ) over all models that incorporated a given focal parameter to ascertain  
275 the plausibility of the effect associated to this parameter. We used this sum to evaluate the null  
276 hypothesis ( $H_0$ ) that a given factor has no effect on the plant-pollinator interactions by comparing the  
277 sum of weights to null expectations, based on the fact that each tested effect is incorporated in exactly  
278 half of the tested models. The effect is considered *plausible* when  $w_H > 0.5$ , *implausible* otherwise,  
279 *likely* when  $w_H > 0.73$ , and *unlikely* when it corresponds to a value of 0.27 or lower, following Massol  
280 *et al.* (2007).

### 281 Predictive power analysis

282 We tested the predictive power of the models we built by making predictions for the  $I_{ij}$  table and  
283 checking their validity using a binarized version of the visit table  $V_{ij}$ . Predictions were obtained by  
284 defining a threshold on interaction probability  $\mu_{ij}$ : values found above the threshold were predicted as  
285 occurring interactions, values below the threshold as no interaction. The threshold probability value  
286 was found by maximizing the sum of model specificity and sensitivity. We computed accuracy statistics  
287 (sensitivity, specificity, omission rate, area under the ROC curve [AUC]) in two situations: (i) when  
288 predicting data for the site that was used to build the model (self-validation; e.g. predicting interaction  
289 data in the site of Riez based on the model developed for this site) and (ii) when predicting data for  
290 the other site from the same region (cross-validation; e.g. predicting data for the LAR site based on the  
291 model for the R site). We performed these analyses using the `SDMTools` package in R. We only used

292 the set of best models (LOO < 4) found for each site to predict the interactions in the other site through  
293 a multimodel averaging approach. We obtained the threshold probability using `optim.tresh`  
294 function with option `max.sensitivity+specificity`.

## 295 **RESULTS**

### 296 Plant-hoverfly networks and phenology overlap

297 At the end of the field campaign we had collected 1584 hoverflies and recorded 1668 interactions  
298 between 76 hoverfly species and 117 plant species overall (Table 1). The number of sampled hoverfly  
299 and plant species varied between sites and among regions. In Normandie we generally sampled a  
300 higher number of hoverflies than in the other two regions (Table 1) and the maximum number of visits  
301 recorded in the site of FAL was 47 (between *Helophilus pendulus* and *Scabiosa columbaria*, Fig. S3) and  
302 in the site of CG was 22 (between *Eristalis tenax* and *S. columbaria* and between *Sphaerophoria scripta*  
303 and *Leontodon hispidus*, Fig. 3). We observed the highest diversity of both plants and hoverflies in  
304 Occitanie and the lowest diversity of hoverflies in Hauts-de-France. Despite the high species diversity  
305 in Occitanie, the total number of interactions recorded in these sites (BF and F) is not the highest  
306 recorded in the field (Table 1): the maximum number of visits in the site of BF was 10 (between  
307 *Sphaerophoria scripta* and *Helichrysum stoechas*, Fig. S2) and 12 in the site of F (between *Syrphus ribesii*  
308 and *Bellis perennis*, Fig. 2). In the two southern sites we also recorded the lowest connectance values  
309 (BF: 0.07 and F: 0.08) of all six sites, with the highest connectance observed in the site of R (R 0.16; LAR  
310 0.13; CG 0.13; FAL 0.12). The maximum number of visits recorded in the site of LAR was 12 (between  
311 *Syrphus ribesii* and *L. hispidus*, Fig. S4) and in the site of R was 17 (between *Syrretta pipiens* and *Asperula*  
312 *cynanchica*, Fig. S5).

313 In spite of differences in diversity and the number of interactions, the overall level of specialization (H2  
314 index) did not show a high variation among the 6 networks (range: 0.32 – 0.37). However, we found  
315 that the sites in Occitanie (BF and F) had a higher average degree of specialization ( $d'$ ) for both insect  
316 (BF 0.63 and F 0.57) and plant species (BF 0.58 and F 0.48). The sites in Occitanie also had a higher

317 modularity (BF 0.51 and F 0.48) than the ones in Normandie (CG 0.34 and FAL 0.23) and Hauts-de-  
318 France (LAR 0.37 and R 0.34; Table 1). Given that these statistics only compare 6 sites, none of these  
319 assessments can be properly statistically tested, but the importance of the differences among sites is  
320 highly suggestive of a difference in average specialization and modularity. We found that plant  
321 phenology is generally shorter in all sites than that of hoverflies (Table 1). The phenology overlap was  
322 shorter in Occitanie (BF and F) than in the other sites (Table 1).

323 Illustrations of the block clustering provided by the LBM analysis (Latent Block Model) are shown in  
324 Fig. 2 and 3 in the main text and in Fig. S2 to S5 in Supplementary Information. We found different  
325 numbers of blocks in plants and hoverflies among sites: the BF site had 2 insect blocks and 2 plant  
326 blocks (Fig. S2); the F site had 4 of both (Fig. 2); the CG and R sites had 3 blocks for the plants and 4  
327 blocks for the insects in (Fig. 3 and S5); the FAL site had 4 plant blocks and 3 insect blocks (Fig. S3); the  
328 LAR site had 3 blocks for the plants and 2 for the insects (Fig. S4).

### 329 Model ranking and comparison of parameters in each site

330 For each site we compared the 16 models using the LOO criterion (Table 2,  $\Delta\text{LOO}$  values). We found  
331 that models 1, 2 and 4 had consistently better goodness-of-fit than the others. The model  
332 incorporating all effects except the effect of phenological overlap on the probability of interaction  
333 (Model 4:  $\lambda_{ij} \sim A_H + A_P + \text{PO}$ , Table 2) was the best model in the sites of CG, FAL and LAR. In the two  
334 southern sites (BF and F), we found that the model incorporating all effects except that of phenological  
335 overlap on the intensity of visits (Model 1:  $\lambda_{ij} \sim A_H + A_P / I_{ij} \sim \text{PO}$ , Table 2), was the best one. The model  
336 incorporating all effects (Model 0:  $\lambda_{ij} \sim A_H + A_P + \text{PO} / I_{ij} \sim \text{PO}$ , Table 2) was found as the best one only in  
337 the site of R, but was a suitable model ( $\Delta\text{LOO} < 4$ ) in all the other sites (Table 2). We also compared the  
338 sum of model weights of the four parameters among sites (Table 2, Effects weight). We found that the  
339 effect of insect abundance on the intensity of interaction ( $A_H \rightarrow \lambda_{ij}$ ) is always likely (*i.e.* the sum of their  
340 weights is always higher than 0.73, Table 2) and of large effect size in all sites (standardised coefficient  
341 higher than 1, Fig. 4). Likewise, we found that the effect of plant abundance on the intensity of

342 interaction ( $A_p \rightarrow \lambda_{ij}$ ) was always likely and had large effect size in most part of sites, except in the site  
343 of F ( $w_H = 0.59$ , Table 2; standardised coefficient = 0.67, Fig. 4). The effects of phenological overlap on  
344 the probability of interaction ( $PO \rightarrow I_{ij}$ ) and the intensity of visits ( $PO \rightarrow \lambda_{ij}$ ), however, had variable  
345 plausibility among sites. The effect of phenological overlap on the probability of interaction was *likely*  
346 only in half of the sites (Table 2 and Fig. 4). The effect of phenological overlap on the intensity of visits  
347 was *not plausible* only in the two southern sites (BF and F) and *plausible* in the other four sites (LAR, R  
348 CG and FAL, Table 2 and Fig. 4). In all sites, the standardised coefficients of PO effects were always less  
349 than 1, thus showing a low effect size of phenology on interaction probability and intensity (Fig. 4).

350 When assessing the predictive power of the best models, we observed that the sensitivity and  
351 specificity values, both for the self-validation and the cross-validation, were higher than 0.5 (Table S2),  
352 which means that the interactions predicted by the models are better than predicted by chance. While  
353 area under the curve (AUC) values were all higher than 0.75 for self-validation, cross-validation tests  
354 yielded intermediate values (AUC between 0.62 and 0.73), reflecting the fact that abundances and  
355 phenology are certainly not sufficient to make accurate predictions on the occurrence of plant-  
356 pollinator interactions.

## 357 **DISCUSSION**

358 Latitude affects the seasonality, with advancing species phenologies at higher latitudes, and thus, can  
359 be a limiting factor for the phenological coupling of interacting species (Post *et al.* 2018). In this study  
360 we explored the effect of phenology overlap on a large network of species interactions in calcareous  
361 grasslands and how this effect could vary along a latitudinal gradient in France using empirical data on  
362 six plant-hoverfly networks. We identified plants and insects at the species level to build detailed  
363 interaction networks and hence avoid spurious generalisation levels. In order to better understand the  
364 determinants of variation in species interactions in space and time, we used the latitudinal gradient to  
365 consider variations linked to environmental cues and the entire flowering period to allow for seasonal  
366 variation (Valverde *et al.* 2016; Pellissier *et al.* 2017). One of the main problems of comparing networks

367 along gradients is the dependence of network metrics on network size (Staniczenko *et al.* 2013;  
368 Astegiano *et al.* 2015; Tylianakis & Morris 2017). In this study, to avoid the problem of comparing  
369 networks with different dimensions, we decided to focus on the determinants of the probability of  
370 interaction and the number of visits, rather than the overall structure. We employed Bayesian  
371 Structural Equation Models (SEM) which is an emergent approach increasingly used to investigate  
372 complex networks of relationship in ecological studies (Grace *et al.* 2010; Eisenhauer *et al.* 2015; Fan  
373 *et al.* 2016; Theodorou *et al.* 2017). In our study we used SEM to link the numbers of visits to phenology  
374 overlap (PO) and species abundance through latent probabilities of species interaction and expected  
375 numbers of visits per plant-pollinator species pair. We tested different models with variable numbers  
376 of effects and compared them in each site. In our models, we used species abundances to construct a  
377 sensible null model to test whether phenology overlap could help explain the probability and intensity  
378 of interactions when the effects of species abundances are already taken into account. In all sites, we  
379 found that models that included both PO and abundances had always better goodness-of-fit than  
380 models that included only abundances. Abundances indeed provided a sensible null model since the  
381 goodness-of-fit of models that did not include abundances were always quite worse than the ones  
382 which did.

383

384 We also found that in all sites the most important factor affecting pollinator visits was insect  
385 abundance (Table 2). Likewise, we found that plant abundance was also a very important effect in most  
386 sites, except in the site of F (Table 2). Since insect abundances are given by visitation data, it is not  
387 surprising that the intensity of interactions positively depends on these abundances. Species  
388 abundance often explain the linkage level in pollination network studies (Olesen *et al.* 2008; Bartomeus  
389 *et al.* 2016; Chacoff *et al.* 2017; Pellissier *et al.* 2017) but it is often associated with the length of the  
390 phenology to better assess the general properties of the interaction network (Vázquez *et al.* 2009;  
391 Olito & Fox 2015). In accordance with this verbal prediction, we indeed found that the best models

392 incorporated the effect of PO on either the probability or the intensity of interactions (Table 2), and  
393 the model that only considered species abundance (model 5 in Table 2) was not the best one in any  
394 site. Phenology overlap generally cannot predict the probability of interaction on its own (Encinas-Viso  
395 *et al.* 2012; CaraDonna *et al.* 2017). Our findings do agree with this general predicament since no site  
396 favoured a model that only incorporated PO effects and because these effects always display lower  
397 effect sizes than the other variables. However, our objective was not to compare the effect of  
398 phenology overlap to that of species abundance – for such an endeavour, one would need estimates  
399 of species abundances independent of visitation data. Because models which consider the effect of PO  
400 on the intensity and/or probability of interactions are the best models for all sites evinces a clear effect  
401 of PO. In our model, the effect of PO on the probability of interaction and the expected number of  
402 visits also vary along the latitudinal gradient (Fig. 4). In general, we observed that southern sites (BF  
403 and F) showed shorter plant phenology and phenology overlap (PO) than the other four sites (Table  
404 1). In these sites, plant species richness is higher and fewer visits were sampled, probably because the  
405 presence of specialist species with short phenophases may increase the number of forbidden or  
406 undetected links (Olesen *et al.* 2011; Martín González *et al.* 2012). Conversely, in sites where plant  
407 phenology is longer, PO is longer too, as observed in Normandie and Hauts-de-France (CG, FAL, LAR  
408 and R, Table 1). Moreover, when plant richness and specialization are lower, a higher number of visits  
409 can be observed (Table 1) because generalist species could interact without constraints. Indeed, in  
410 Normandie and Hauts-de-France we found that the effect of phenology overlap on the intensity of  
411 visits was always likely ( $PO \rightarrow \lambda_{ij}$ , Table 2) and we observed higher numbers of interactions in the first  
412 two/three blocks of insects and plants which also corresponded to blocks with longer PO (Fig. 3, S3, S4  
413 and S5). A higher phenological overlap is expected to drive a higher probability of interactions and a  
414 larger number of visits (Olesen *et al.* 2011). In Occitanie, we did not find any effect of PO on the number  
415 of visits because the more densely visited blocks do not correspond to those with longer phenology  
416 overlap. Plant phenology can therefore drive the probability and the intensity of interactions in  
417 networks in which plant phenology is shorter, thus suggesting that hoverflies may undergo selection

418 for behavioural flexibility in order to maintain synchrony with their foraging resources (Iler *et al.* 2013;  
419 Ogilvie & Forrest 2017).

420 We also found that modularity decreased along the latitudinal gradient, with richer sites (BF and F)  
421 displaying higher modularity (as in Sebastián-González *et al.* 2015) but also the lower connectance. In  
422 the two southern sites, higher modularity could be related to shorter phenologies and higher  
423 proportions of non-overlapping sets of species, which induce some form of temporal short-term  
424 specialisation (Lucas *et al.* 2018). However, modularity also seems to be influenced by species  
425 abundances and degrees (Schleuning *et al.* 2014), and is expected to increase with link specificity  
426 (Morente-López *et al.* 2018). Indeed, in these sites, species blocks match species degrees (Fig. 2 and  
427 S2), with generalist and specialist species forming separate blocks among both plants and insects  
428 (Martín González *et al.* 2012). With lower modularity and more generalist species, we expect a stronger  
429 relationship between phenology and the intensity of interactions because interactions are less  
430 influenced by insect preferences and more by seasonal rhythm and flower availability (Dormann *et al.*  
431 2017). Thus, different phenophases might correspond to different compartments (Martín González *et*  
432 *al.* 2012; Morente-López *et al.* 2018), as observed in CG, FAL, LAR and R where higher overlap  
433 corresponded to higher numbers of observed visits. Although phenology improved model fit (Table 2),  
434 its effect size was modest (Fig. 4), which suggests that other types of data such as traits and phylogenies  
435 might help predict specific interactions. In our study, we did not consider competition among studied  
436 insect species or with other group of insects, such as bees which were present in all sites. Different  
437 types of pollinators with different abundances could have context-dependent effects on network  
438 topology (Valverde *et al.* 2016). Moreover, in our study we only considered as “true absence” of the  
439 interaction the lack of phenological coupling between species (*i.e.* plant and hoverfly species which are  
440 not present at the same moment along the season cannot interact). We did not consider “false  
441 absences”, *i.e.* missing links, since not all the potential links among species are recorded in the field  
442 (Olesen *et al.* 2011) which may introduce bias in the estimation of the probability of interactions  
443 (Bartomeus *et al.* 2016; Cirtwill *et al.* 2019).

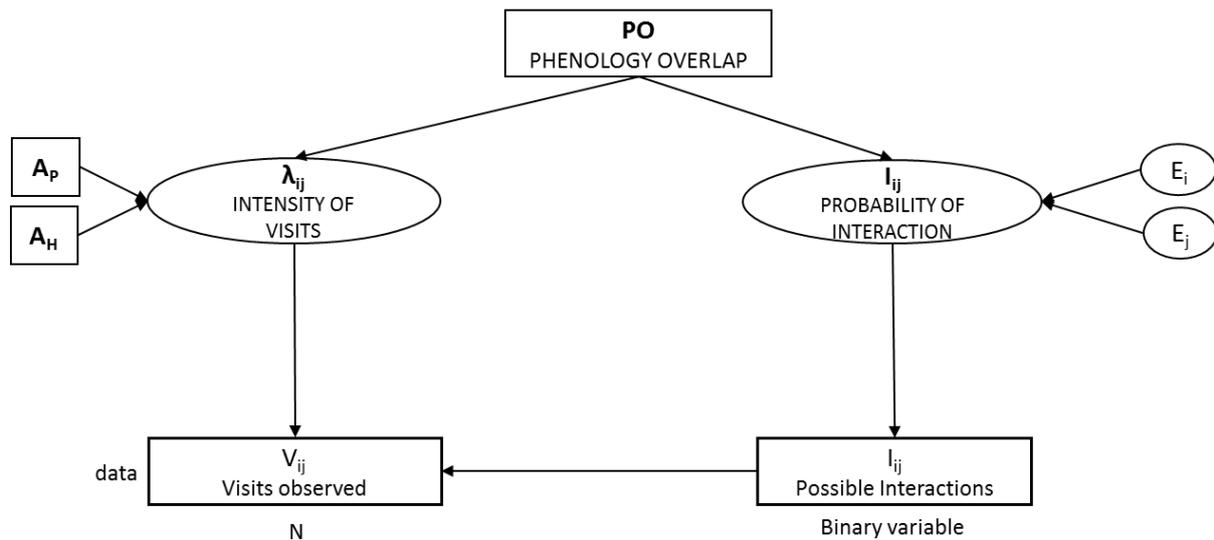
444 To conclude, plant phenology here drives the duration of the phenology overlap between plant and  
445 hoverflies, which in turn influences either the probability of interaction or the expected number of  
446 visits, as well as network compartmentalization. Longer phenologies correspond to less constrained  
447 interactions (lower modularity), shorter phenologies to more constrained interactions (higher  
448 modularity), which in turn restrict the number of visits. Phenology overlap alone was not sufficient to  
449 explain interactions, as suggested elsewhere (CaraDonna *et al.* 2017). Plant and insect abundances  
450 played a substantial role to explain the number of visits (as in Chacoff *et al.* 2017) since abundances  
451 may affect partner choice (Trøjelsgaard *et al.* 2015). Our results, and the ability of the method used  
452 here to compare different effects on interaction patterns, suggest that the use of Bayesian SEM to  
453 compare networks of different sizes is a valuable tool which can help understand plant-pollinator  
454 networks (Eisenhauer *et al.* 2015). The use of latent variables can help predict the probability of  
455 interaction and the expected number of visits while avoiding circularity – the introduction of plant and  
456 insect specific random effects played the role of an implicit “degree” effect. Our results demonstrate  
457 the importance of considering differences in plant and insect phenologies to better predict their  
458 interactions in pollination networks at different latitudes. The use of morphological traits (*e.g.* tongue  
459 length, inter-tegular distance, ...) together with species richness and phylogenies, on top of variables  
460 already used, might improve the modelling of interactions and could help better understand some  
461 forbidden or missing links in richer communities or considering other pollinators (*e.g.* wild bees).

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468 Regional Economical Development for their financial support.

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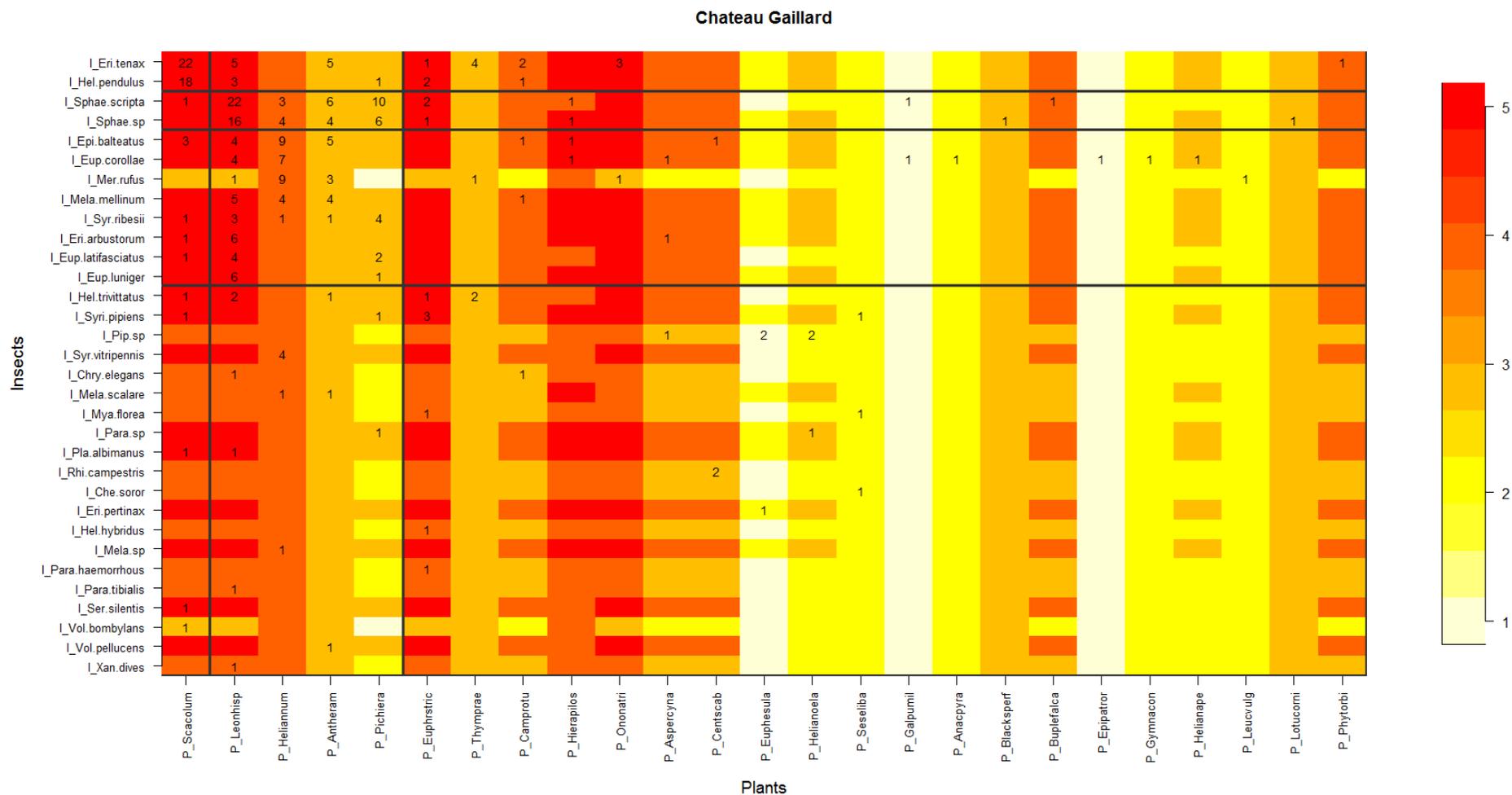
471

472 Figure 1. Summary diagram of the SEM model. We estimated 4 effects: the effect of plant abundance  
 473 ( $A_P \rightarrow \lambda_{ij}$ , coefficient  $\lambda_P$ ), the effect of insect (hoverflies) abundance on the intensity of visits ( $A_H \rightarrow$   
 474  $\lambda_{ij}$ ,  $\lambda_H$ ), the effect of phenology overlap on the intensity of visits ( $PO \rightarrow \lambda_{ij}$ ,  $\lambda_{PO}$ ) and the effect of  
 475 phenology overlap on the probability of interaction ( $PO \rightarrow I_{ij}$ ,  $\mu_{PO}$ ). The phenology overlap ( $PO$ ) is the  
 476 number of phenologically active months that are shared by each pair of insect and plant species along  
 477 the season. The intensity of visits ( $\lambda_{ij}$ ) and the probability of interaction are latent variables in the  
 478 model. Effect-i and effect-p are random effects calculated by the model which represent the insect  
 479 and plant species identities. The  $I_{ij}$  (Possible interactions) is a binary variable and the  $V_{ij}$  (visits  
 480 observed) follow a Poisson distribution with an expected value given when the probability of  
 481 interaction is predicted as “true”. Rectangles represent observed variables while ovals represent  
 482 unobserved influences.

483

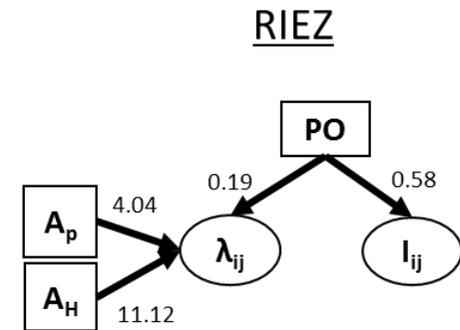
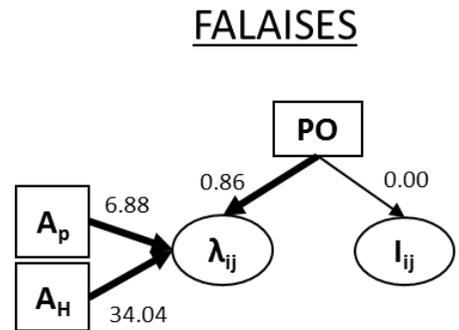
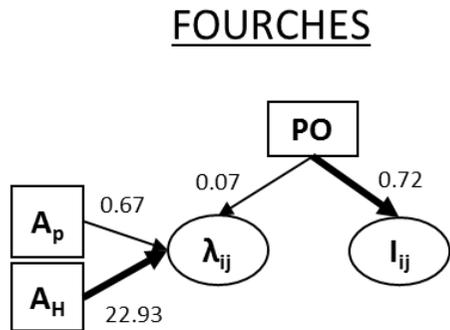
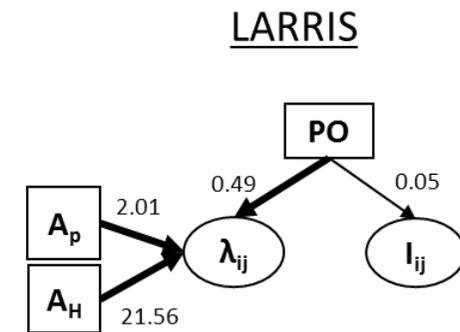
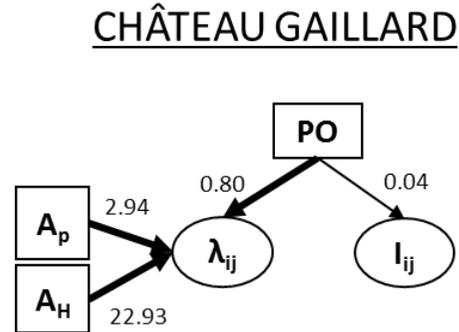
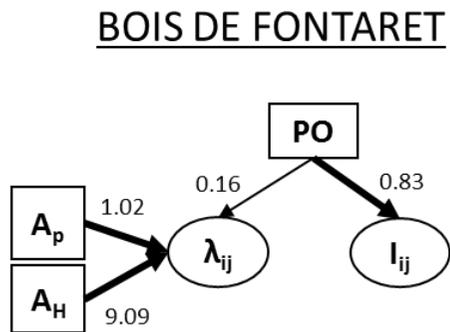


490 Figure 3. Block clustering provided by LBM in the site of Chateau Gaillard (CG, Normandie) overlaid on a heatmap of species phenology overlap. Insect species  
 491 are displayed in rows and plant species in columns, following their degree (number of partners). The blocks of insects and the blocks of plants are separated  
 492 by solid black lines. Colours correspond to the number of months that are shared by each pair of plant and insect species (PO, phenology overlap), with higher  
 493 PO corresponding to darker colours. Numbers are the number of visits observed in the field for a given plant-insect pair.



494

495 Figure 4. Summary diagram of the best models in all sites. The thickness of the arrows is scaled to Akaike weights (thin ER < 0.73; thick ER > 0.73, cf. Table 2).  
 496 Standardised coefficients of the model average (computed based on the Akaike weighted model average) are reported next to the arrows. PO is the phenology  
 497 overlap,  $I_{ij}$  is the probability of interaction,  $\lambda_{ij}$  is the intensity of visits,  $A_H$  and  $A_p$  are the hoverflies and plant abundances respectively.



498

499

500 Table 1. Summary table of results obtained in each site (Bois de Fontaret [BF] and Fourches [F] in Occitanie, Château Gaillard [CG] and Falaises [FAL] in  
501 Normandie, Larris [LAR] and Riez [R] in Hauts-de-France).  $H_2'$  and  $d'$  indices refer to specialization indices described by Blüthgen *et al.* (2006) and  
502 implemented in the R package `bipartite` (Dormann *et al.* 2009). The modularity score was obtained using the `leading-eigenvector` method  
503 described by Newman (2006) and implemented in the `igraph` package (Csardi & Nepusz 2006). LBM refers to latent block modelling as implemented in the  
504 R package `blockmodels` (Leger *et al.* 2015).

505

Site	Region	Collected data				Specialization index			Species phenology			Modularity analysis	LBM	
		Sampled insects	Insect species	Plant species	Recorded Interactions	$H_2'$ index	$d'$ Insects (average + sd)	$d'$ Plants (average + sd)	Insect (average + sd)	Plant (average + sd)	Phenology overlap (PO) (average + sd)	modularity score	blocks I	blocks P
<b>BF</b>	Occitanie	197	40	43	198	0.37	0.63 ± 0.17	0.58 ± 0.17	5.25 ± 1.51	2.14 ± 1.04	1.77 ± 1.03	0.53	2	2
<b>F</b>	Occitanie	223	36	49	286	0.33	0.57 ± 0.18	0.48 ± 0.19	5.61 ± 1.54	2.08 ± 1.13	1.78 ± 1.14	0.48	4	4
<b>CG</b>	Normandie	295	32	25	297	0.34	0.40 ± 0.21	0.47 ± 0.18	6.03 ± 1.00	3.28 ± 1.24	3.02 ± 1.17	0.34	4	3
<b>FAL</b>	Normandie	363	34	30	374	0.32	0.40 ± 0.18	0.41 ± 0.18	6.06 ± 1.13	3.57 ± 1.59	3.23 ± 1.51	0.23	3	4
<b>LAR</b>	Hauts-de-France	220	24	33	220	0.36	0.48 ± 0.19	0.45 ± 0.15	6.38 ± 0.82	3.18 ± 1.38	2.99 ± 1.36	0.37	2	3
<b>R</b>	Hauts-de-France	286	22	29	293	0.32	0.39 ± 0.16	0.40 ± 0.16	5.55 ± 0.74	3.38 ± 1.47	3.11 ± 1.45	0.34	4	3
<b>Total</b>		<b>1584</b>	<b>76</b>	<b>117</b>	<b>1668</b>									

506

507 Table 2. (i) Comparison of SEM models using the leave-one-out cross-validation criterion (LOO); (ii)  
508 evidence ratios (ER) of model effects in each site. (i) Models are ranked depending on the number of  
509 parameters used (from 0 to 4). The best models are the ones with  $\Delta\text{LOO}=0$  (underlined and bold  
510 values). The other suitable models are the ones with  $\Delta\text{LOO} < 4$  (underlined and italic values).  $\lambda_{ij}$  is the  
511 intensity of visits,  $I_{ij}$  is the probability of interaction,  $A_H$  is the insect abundance,  $A_P$  is the plant  
512 abundance and PO is the phenology overlap. (ii) We compared 4 model effects:  $\text{PO} \rightarrow I_{ij}$ , effect of the  
513 phenology overlap on the probability of interaction;  $\text{PO} \rightarrow \lambda_{ij}$ , effect of the phenology overlap on the  
514 intensity of visits;  $A_H \rightarrow \lambda_{ij}$  and  $A_P \rightarrow \lambda_{ij}$  effects of the hoverflies and plant abundances on the intensity  
515 of interaction. The  $w_H$  limits for unlikelihood is 0.27, plausibility 0.5 and likelihood 0.73. Underlined  
516 and bold values represent the likely hypothesis only.

		Sites					
		BF	F	CG	FAL	LAR	R
Model	Nb of parameters	$\Delta\text{LOO values}$					
0	$\lambda_{ij} \sim A_H + A_P + \text{PO} / I_{ij} \sim \text{PO}$	<u>2.98</u>	<u>2.04</u>	<u>3.54</u>	<u>2.54</u>	<u>2.86</u>	<b>0.00</b>
1	$\lambda_{ij} \sim A_H + A_P / I_{ij} \sim \text{PO}$	<b>0.00</b>	<b>0.00</b>	36.75	64.04	10.37	<u>2.90</u>
2	$\lambda_{ij} \sim A_P + \text{PO} / I_{ij} \sim \text{PO}$	8.66	78.23	106.46	184.02	44.60	17.00
3	$\lambda_{ij} \sim A_H + \text{PO} / I_{ij} \sim \text{PO}$	6.63	<u>1.71</u>	8.09	73.62	11.24	11.42
4	$\lambda_{ij} \sim A_H + A_P + \text{PO}$	<u>2.86</u>	8.06	<b>0.00</b>	<b>0.00</b>	<b>0.00</b>	<u>2.24</u>
5	$\lambda_{ij} \sim \text{PO} / I_{ij} \sim \text{PO}$	14.69	73.20	109.85	223.86	55.67	23.09
6	$\lambda_{ij} \sim A_H / I_{ij} \sim \text{PO}$	<u>1.45</u>	<u>1.31</u>	33.53	119.04	27.23	19.76
7	$\lambda_{ij} \sim A_P / I_{ij} \sim \text{PO}$	9.84	72.16	156.61	256.04	47.99	21.53
8	$\lambda_{ij} \sim A_H + \text{PO}$	11.49	8.18	5.25	71.97	10.28	13.80
9	$\lambda_{ij} \sim A_P + \text{PO}$	10.71	88.67	103.46	182.14	44.36	17.94
10	$\lambda_{ij} \sim A_H + A_P$	24.36	14.04	36.10	66.82	10.51	4.26
11	$I_{ij} \sim \text{PO}$	11.78	68.52	154.26	272.98	64.12	32.39
12	$\lambda_{ij} \sim \text{PO}$	19.99	86.20	108.46	219.66	54.64	25.73
13	$\lambda_{ij} \sim A_H$	25.58	14.41	36.12	123.30	28.27	22.78
14	$\lambda_{ij} \sim A_P$	32.99	87.70	157.74	256.39	48.82	22.87
15	-	34.39	83.89	155.68	274.80	64.78	33.52
Model effects		Effects weight ( $w_H$ )					
	$\text{PO} \rightarrow I_{ij}$	<b>0.88</b>	<b>0.98</b>	0.15	0.22	0.20	<b>0.74</b>
	$\text{PO} \rightarrow \lambda_{ij}$	0.26	0.35	<b>1.00</b>	<b>1.00</b>	<b>0.99</b>	<b>0.79</b>
	$A_H \rightarrow \lambda_{ij}$	<b>0.99</b>	<b>1.00</b>	<b>1.00</b>	<b>1.00</b>	<b>1.00</b>	<b>1.00</b>
	$A_P \rightarrow \lambda_{ij}$	<b>0.74</b>	0.59	<b>0.93</b>	<b>1.00</b>	<b>0.99</b>	<b>1.00</b>

517

518

519 **Supporting Information**

520 The following Supporting Information is available for this article:

521 Appendix S1. Model code.

522 Appendix S2. Model script for the 16 models.

523 Appendix S3. Script modularity and latent block model analysis (LBM).

524 Figure S1. Sites location in France.

525 Figure S2. Block clustering provided by LBM in the site of Bois de Fontaret (BF, Occitanie), overlaid on  
526 a heatmap of species phenology overlap.

527 Figure S3. Block clustering provided by LBM in the site of Falaises (FAL, Normandie), overlaid on a  
528 heatmap of species phenology overlap.

529 Figure S4. Block clustering provided by LBM in the site of Larris (LAR, Hauts-de-France), overlaid on a  
530 heatmap of species phenology overlap.

531 Figure S5. Block clustering provided by LBM in the site of Riez (R, Hauts-de-France), overlaid on a  
532 heatmap of species phenology overlap.

533 Table S1. Table of transformed plant abundances.

534

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696

697

## Supplementary Information

698 Does phenology explain plant-pollinator interactions at different latitudes? An assessment of its  
699 explanatory power in plant-hoverfly networks in French calcareous grasslands

700 N. de Manincor<sup>1\*</sup>, N. Hautekeete<sup>1</sup>, Y. Piquot<sup>1</sup>, B. Schatz<sup>2</sup>, C. Vanappelghem<sup>3</sup>, F. Massol<sup>1,4</sup>

701 <sup>1</sup> Université de Lille, CNRS, UMR 8198 - Evo-Eco-Paleo, 59000 Lille, France

702 <sup>2</sup> CEFE, EPHE-PSL, CNRS, University of Montpellier, University of Paul Valéry Montpellier 3, IRD,  
703 Montpellier, France

704 <sup>3</sup> Conservatoire d'espaces naturels Nord et du Pas-de-Calais, 160 rue Achille Faniens - ZA de la Haye,  
705 62190 LILLERS

706 <sup>4</sup> Univ. Lille, CNRS, Inserm, CHU Lille, Institut Pasteur de Lille, U1019 - UMR 8204 - CIIL - Center for  
707 Infection and Immunity of Lille, F-59000 Lille, France

708

709 Natasha de Manincor ORCID: 0000-0001-9696-125X

710 Nina Hautekeete ORCID: 0000-0002-6071-5601

711 Yves Piquot ORCID: 0000-0001-9977-8936

712 Bertrand Schatz ORCID: 0000-0003-0135-8154

713 François Massol ORCID: 0000-0002-4098-955X

714

715 \*Corresponding author

716

717 E-mail addresses: [natasha.de-manincor@univ-lille.fr](mailto:natasha.de-manincor@univ-lille.fr), [francois.massol@univ-lille.fr](mailto:francois.massol@univ-lille.fr),  
718 [nina.hautekeete@univ-lille.fr](mailto:nina.hautekeete@univ-lille.fr), [yves.piquot@univ-lille.fr](mailto:yves.piquot@univ-lille.fr), [Bertrand.SCHATZ@cefe.cnrs.fr](mailto:Bertrand.SCHATZ@cefe.cnrs.fr),  
719 [cedric.vanappelghem@espaces-naturels.fr](mailto:cedric.vanappelghem@espaces-naturels.fr)

720 **Appendix S1: Model Code**

721 The model code (in JAGS language) given in this supplementary material refers to the “model Z0” which  
722 considers all four parameters (model effects, Table 2 in the main text). Overall, we estimated 16  
723 models that included between 0 and 4 of the above-mentioned effects. To create the code for these  
724 other models, parameters should be removed following the order in the Tab. 2. The four parameters  
725 tested in the model are: (i) alpha: effect of the phenology overlap (cooc) on the probability of  
726 interaction; (ii) epsilon: effect of the phenology overlap on the intensity of visits; (iii) gamma: effect of  
727 the insect abundances (ab\_I) on the intensity of visits; and (iv) delta: effect of the plant abundances  
728 (ab\_P) on the intensity of visits.

---

729

730 model

731 {

732 for( i in 1 : dim1 ) {

733 for( p in 1 : dim2 ) {

734 inter[i , p] ~ dbern(mu[i , p])

735 logit(mu[i , p]) <- beta + alpha\*cooc[i , p] + effet\_I[i] + effet\_P[p]

736 lambda[i,p] <- exp(theta[i,p])

737 theta[i,p] <- theta0 + gamma\*ab\_I[i] + delta\*ab\_P[p] + epsilon\*log(1+cooc[i,p])

738 visit[i,p] ~ dpois( inter[i,p]\*lambda[i,p] )

739 loglik[i,p] <- log(ifelse(visit[i,p]==0,1-mu[i,p]+mu[i , p]\*dpois(visit[i,p],lambda[i,p]),mu[i ,

740 p]\*dpois(visit[i,p],lambda[i,p])))

741 }

742 }

743

744 for( i in 1 : dim1 ) {

745 effet\_I[i] ~ dnorm( 0.0,tau\_I)

```
746 }
747
748 for( p in 1 : dim2 ) {
749     effet_P[p] ~ dnorm( 0.0,tau_P)
750 }
751
752     tau_I ~ dexp( 10)
753     tau_P ~ dexp( 10)
754     alpha ~ dnorm(0,0.01)
755     beta ~ dnorm(0,0.01)
756     theta0 ~ dnorm(0,0.01)
757     gamma ~ dnorm(0,0.01)
758     delta ~ dnorm(0,0.01)
759     epsilon ~ dnorm(0,0.01)
760 }
761
```

762 **Appendix 2: Model script for the 16 models – LOO values**

763 The following generic script was applied to all the study sites using all 16 models. The script is separated  
764 in three blocks which communicate among them: the script options, the model definitions and the  
765 execution (model inference). We defined three options to set (i) the name of the directory (-d), (ii) the  
766 site (-s) and (iii) the type of model (-m).

767 We used, as an example, the information for the site of Bois de Fontaret (BF).

768 Exemple: Rscript (name) "script-SEMLOO\_generique.R" "-d o-BFs-2016" "-s BFs"

769 In order to calculate the standardised coefficients for each parameters used, at the end of the third  
770 block, we added the functions to get the parameter values for each site and each model.

771 ##### BLOCK 1 – SCRIPT OPTION #####

772 library(optparse)

773 option\_list = list(

774     make\_option(c("-d", "--dir"), type="character", default=NULL, help="directory",

775     metavar="character"),

776     make\_option(c("-s", "--site"), type="character", default=NULL, help="site name",

777     metavar="character"),

778     make\_option(c("-m", "--modele"), type="character", default="all", help="modele name",

779     metavar="character"))

780 opt\_parser = OptionParser(option\_list=option\_list);

781 opt = parse\_args(opt\_parser);

782 site<-opt\$site

783 dossier<-opt\$dir

784 ##### Librairies #####

785 library(bipartite)

786 library(vegan)

787 library(igraph)

```

788 library(magrittr)
789 library(dummies)
790 library(MuMIn)
791 library(rjags)
792 library(boot)
793 library(R2jags)
794 library(coda)
795 library(lattice)
796 library(ggplot2)
797 library(loo)
798 library(matrixStats)
799 ##### Function to record the LOO values #####
800 write_values<-function(x, f, app)
801 {
802     write.table(x, append=app, file=f, sep="\t", row.names=T, col.names=T, quote=F)
803 }
804 ##### BLOCK 2 – MODEL FUNCTIONS #####
805 #Model function and model initialization: one function for each model from model Z15, with 0
806 parameters, to Z00 with all the parameters#
807 ### MODEL Z015
808 mZ015<-function(){
809     init.funZ015 <-function(){
810         list("tau_I" = rexp(1,10), "tau_P" = rexp(1,10), "beta" = rnorm(1,0,1), "theta0" =
811 rnorm(1,0,1), "effet_I"=rnorm(dim1,0,1),"effet_P"=rnorm(dim2,0,1), "inter"=inter0)
812     }

```

```

813     mod.Z015<-jags(inits=init.funZ015,model.file = "modelZ015_code.txt",data =
814 list("visit","dim1","dim2"),parameters.to.save =
815 c("mu","effet_I","effet_P","tau_I","tau_P","beta","theta0", "loglik"),n.chains = 1, n.iter=1000000,
816 n.burnin = 250000, n.thin = 250)
817     mod.Z015.mcmc<-as.mcmc(mod.Z015)
818     mZ015<-mod.Z015$BUGSoutput$sims.list
819     mZ015.deviance<-mZ015$deviance
820     mZ015.loglik<-mZ015$loglik
821     dimSEM<-dim(mZ015.loglik)[1]
822     list.mZ015<-sapply(1:dimSEM,function(x) matrix(mZ015.loglik[x,,],nrow=dim1*dim2))
823     list.tmZ015<-(t(list.mZ015))
824     mZ015.loo<-loo(list.tmZ015)
825     loo_file<-paste(dossier, "/", site, "_Z015_loo.txt", sep="")
826     write_values("mZ015", app=F, loo_file)
827     mZ015_loo_pointwise<-mZ015.loo$pointwise
828     mZ015_loo_pareto_k<-mZ015.loo$pareto_k
829     mZ015.loo$pareto_k<-NULL
830     mZ015.loo$pointwise<-NULL
831     write_values(as.matrix(mZ015.loo), app=T, loo_file)
832     save.image(paste(dossier, "/", site, "_Z015.RData", sep=""))
833 }
834 ### MODEL Z014
835 mZ014<-function(){
836     init.funZ014 <-function(){
837         list("tau_I" = rexp(1,10), "tau_P" = rexp(1,10), "beta" = rnorm(1,0,1), "delta" = rnorm(1,0,1),
838 "theta0" = rnorm(1,0,1), "effet_I"=rnorm(dim1,0,1),"effet_P"=rnorm(dim2,0,1), "inter"=inter0)

```

```

839     }
840     mod.Z014<<-jags(inits=init.funZ014,model.file = "modelZ014_code.txt",data =
841 list("visit","ab_P","dim1","dim2"),parameters.to.save =
842 c("mu","effet_I","effet_P","tau_I","tau_P","delta","beta","theta0","loglik"),n.chains = 1,
843 n.iter=1000000, n.burnin = 250000, n.thin = 250)
844     mod.Z014.mcmc<-as.mcmc(mod.Z014)
845     mZ014<-mod.Z014$BUGSoutput$sims.list
846     mZ014.deviance<-mZ014$deviance
847     mZ014.loglik<-mZ014$loglik
848     dimSEM<-dim(mZ014.loglik)[1]
849     list.mZ014<-sapply(1:dimSEM,function(x) matrix(mZ014.loglik[x,,],nrow=dim1*dim2))
850     list.tmZ014<-(t(list.mZ014))
851     mZ014.loo<-loo(list.tmZ014)
852     mZ014.loo
853     loo_file<-paste(dossier, "/", site, "_Z014_loo.txt", sep="")
854     write_values("mZ014", app=T, loo_file)
855     mZ014_loo_pointwise<-mZ014.loo$pointwise
856     mZ014_loo_pareto_k<-mZ014.loo$pareto_k
857     mZ014.loo$pareto_k<-NULL
858     mZ014.loo$pointwise<-NULL
859     write_values(as.matrix(mZ014.loo), app=T, loo_file)
860     save.image(paste(dossier, "/", site, "_Z014.RData", sep=""))
861 }
862 ### MODEL Z013
863 mZ013<-function(){
864     init.funZ013 <-function(){

```

```

865     list("tau_I" = rexp(1,10), "tau_P" = rexp(1,10), "beta" = rnorm(1,0,1), "gamma" =
866     rnorm(1,0,1), "theta0" = rnorm(1,0,1), "effet_I"=rnorm(dim1,0,1),"effet_P"=rnorm(dim2,0,1),
867     "inter"=inter0)
868     }
869     mod.Z013<<-jags(inits=init.funZ013,model.file = "modelZ013_code.txt",data =
870     list("visit","ab_I","dim1","dim2"),parameters.to.save =
871     c("mu","effet_I","effet_P","tau_I","tau_P","gamma","beta","theta0","loglik"),n.chains = 1,
872     n.iter=1000000, n.burnin = 250000, n.thin = 250)
873     mod.Z013.mcmc<-as.mcmc(mod.Z013)
874     mZ013<-mod.Z013$BUGSoutput$sims.list
875     mZ013.deviance<-mZ013$deviance
876     mZ013.loglik<-mZ013$loglik
877     dimSEM<-dim(mZ013.loglik)[1]
878     list.mZ013<-sapply(1:dimSEM,function(x) matrix(mZ013.loglik[x,,],nrow=dim1*dim2))
879     list.tmZ013<-(t(list.mZ013))
880     mZ013.loo<-loo(list.tmZ013)
881     mZ013.loo
882     loo_file<-paste(dossier, "/", site, "_Z013_loo.txt", sep="")
883     write_values("mZ013", app=T, loo_file)
884     mZ013_loo_pointwise<-mZ013.loo$pointwise
885     mZ013_loo_pareto_k<-mZ013.loo$pareto_k
886     mZ013.loo$pareto_k<-NULL
887     mZ013.loo$pointwise<-NULL
888     write_values(as.matrix(mZ013.loo), app=T, loo_file)
889     save.image(paste(dossier, "/", site, "_Z013.RData", sep=""))
890 }

```

```

891   ### MODEL Z012
892   mZ012<-function(){
893       init.funZ012 <-function(){
894           list("tau_I" = rexp(1,10), "tau_P" = rexp(1,10), "beta" = rnorm(1,0,1), "theta0" =
895   rnorm(1,0,1), "epsilon" = rnorm(1,0,1), "effet_I"=rnorm(dim1,0,1),"effet_P"=rnorm(dim2,0,1),
896   "inter"=inter0)
897       }
898       mod.Z012<<-jags(inits=init.funZ012,model.file = "modelZ012_code.txt",data =
899   list("cooc","visit","dim1","dim2"),parameters.to.save =
900   c("mu","effet_I","effet_P","tau_I","tau_P","beta","theta0","epsilon","loglik"),n.chains = 1,
901   n.iter=1000000, n.burnin = 250000, n.thin = 250)
902       mod.Z012.mcmc<-as.mcmc(mod.Z012)
903       mZ012<-mod.Z012$BUGSoutput$sims.list
904       mZ012.deviance<-mZ012$deviance
905       mZ012.loglik<-mZ012$loglik
906       dimSEM<-dim(mZ012.loglik)[1]
907       list.mZ012<-sapply(1:dimSEM,function(x) matrix(mZ012.loglik[x,,],nrow=dim1*dim2))
908       list.tmZ012<-(t(list.mZ012))
909       mZ012.loo<-loo(list.tmZ012)
910       mZ012.loo
911       loo_file<-paste(dossier, "/", site, "_Z012_loo.txt", sep="")
912       write_values("mZ012", app=T, loo_file)
913       mZ012_loo_pointwise<-mZ012.loo$pointwise
914       mZ012_loo_pareto_k<-mZ012.loo$pareto_k
915       mZ012.loo$pareto_k<-NULL
916       mZ012.loo$pointwise<-NULL

```

```

917     write_values(as.matrix(mZ012.loo), app=T, loo_file)
918     save.image(paste(dossier, "/", site, "_Z012.RData", sep=""))
919 }
920 ### MODEL Z011
921 mZ011<-function(){
922     init.funZ011 <-function(){
923         list("tau_I" = rexp(1,10), "tau_P" = rexp(1,10), "alpha" = 0.1,"beta" = rnorm(1,0,1), "theta0"
924 = rnorm(1,0,1), "effet_I"=rnorm(dim1,0,1),"effet_P"=rnorm(dim2,0,1), "inter"=inter0)
925     }
926     mod.Z011<<-jags(inits=init.funZ011,model.file = "modelZ011_code.txt",data =
927 list("cooc","visit","dim1","dim2"),parameters.to.save =
928 c("mu","effet_I","effet_P","tau_I","tau_P","alpha","beta","theta0","loglik"),n.chains = 1,
929 n.iter=1000000, n.burnin = 250000, n.thin = 250)
930     mod.Z011.mcmc<-as.mcmc(mod.Z011)
931     mZ011<-mod.Z011$BUGSoutput$sims.list
932     mZ011.deviance<-mZ011$deviance
933     mZ011.loglik<-mZ011$loglik
934     dimSEM<-dim(mZ011.loglik)[1]
935     list.mZ011<-sapply(1:dimSEM,function(x) matrix(mZ011.loglik[x,,],nrow=dim1*dim2))
936     list.tmZ011<-(t(list.mZ011))
937     mZ011.loo<-loo(list.tmZ011)
938     mZ011.loo
939     loo_file<-paste(dossier, "/", site, "_Z011_loo.txt", sep="")
940     write_values("mZ011", app=T, loo_file)
941     mZ011_loo_pointwise<-mZ011.loo$pointwise
942     mZ011_loo_pareto_k<-mZ011.loo$pareto_k

```

```

943     mZ011.loo$pareto_k<-NULL
944     mZ011.loo$pointwise<-NULL
945     write_values(as.matrix(mZ011.loo), app=T, loo_file)
946     save.image(paste(dossier, "/", site, "_Z011.RData", sep=""))
947 }
948 ### MODEL Z010
949 mZ010<-function(){
950     init.funZ010 <-function(){
951         list("tau_I" = rexp(1,10), "tau_P" = rexp(1,10), "beta" = rnorm(1,0,1), "gamma" =
952 rnorm(1,0,1), "delta" = rnorm(1,0,1), "theta0" = rnorm(1,0,1),
953 "effet_I"=rnorm(dim1,0,1),"effet_P"=rnorm(dim2,0,1), "inter"=inter0)
954     }
955     mod.Z010<<-jags(inits=init.funZ010,model.file = "modelZ010_code.txt",data =
956 list("visit","ab_I","ab_P","dim1","dim2"),parameters.to.save =
957 c("mu","effet_I","effet_P","tau_I","tau_P","gamma","delta","beta","theta0","loglik"),n.chains = 1,
958 n.iter=1000000, n.burnin = 250000, n.thin = 250)
959     mod.Z010.mcmc<-as.mcmc(mod.Z010)
960     mZ010<-mod.Z010$BUGSoutput$sims.list
961     mZ010.deviance<-mZ010$deviance
962     mZ010.loglik<-mZ010$loglik
963     dimSEM<-dim(mZ010.loglik)[1]
964     list.mZ010<-sapply(1:dimSEM,function(x) matrix(mZ010.loglik[x,,],nrow=dim1*dim2))
965     list.tmZ010<-(t(list.mZ010))
966     mZ010.loo<-loo(list.tmZ010)
967     mZ010.loo
968     loo_file<-paste(dossier, "/", site, "_Z010_loo.txt", sep="")

```

```

969     write_values("mZ010", app=T, loo_file)
970     mZ010_loo_pointwise<-mZ010.loo$pointwise
971     mZ010_loo_pareto_k<-mZ010.loo$pareto_k
972     mZ010.loo$pareto_k<-NULL
973     mZ010.loo$pointwise<-NULL
974     write_values(as.matrix(mZ010.loo), app=T, loo_file)
975     save.image(paste(dossier, "/", site, "_Z010.RData", sep=""))
976 }
977 ### MODEL Z09
978 mZ09<-function(){
979     init.funZ09 <-function(){
980         list("tau_I" = rexp(1,10), "tau_P" = rexp(1,10), "beta" = rnorm(1,0,1), "delta" = rnorm(1,0,1),
981 "theta0" = rnorm(1,0,1), "epsilon" = rnorm(1,0,1),
982 "effet_I"=rnorm(dim1,0,1),"effet_P"=rnorm(dim2,0,1), "inter"=inter0)
983     }
984     mod.Z09<<-jags(inits=init.funZ09,model.file = "modelZ09_code.txt",data =
985 list("cooc","visit","ab_P","dim1","dim2"),parameters.to.save =
986 c("mu","effet_I","effet_P","tau_I","tau_P","delta","beta","theta0","epsilon","loglik"),n.chains = 1,
987 n.iter=1000000, n.burnin = 250000, n.thin = 250)
988     mod.Z09.mcmc<-as.mcmc(mod.Z09)
989     mZ09<-mod.Z09$BUGSoutput$sims.list
990     mZ09.deviance<-mZ09$deviance
991     mZ09.loglik<-mZ09$loglik
992     dimSEM<-dim(mZ09.loglik)[1]
993     list.mZ09<-sapply(1:dimSEM,function(x) matrix(mZ09.loglik[x,,],nrow=dim1*dim2))
994     list.tmZ09<-(t(list.mZ09))

```

```

995     mZ09.loo<-loo(list.tmZ09)
996     mZ09.loo
997     loo_file<-paste(dossier, "/", site, "_Z09_loo.txt", sep="")
998     write_values("mZ09", app=T, loo_file)
999     mZ09_loo_pointwise<-mZ09.loo$pointwise
1000    mZ09_loo_pareto_k<-mZ09.loo$pareto_k
1001    mZ09.loo$pareto_k<-NULL
1002    mZ09.loo$pointwise<-NULL
1003    write_values(as.matrix(mZ09.loo), app=T, loo_file)
1004    save.image(paste(dossier, "/", site, "_Z09.RData", sep=""))
1005  }
1006  ### MODEL Z08
1007  mZ08<-function(){
1008    init.funZ08 <-function(){
1009      list("tau_I" = rexp(1,10), "tau_P" = rexp(1,10), "beta" = rnorm(1,0,1), "gamma" =
1010  rnorm(1,0,1), "theta0" = rnorm(1,0,1), "epsilon" = rnorm(1,0,1),
1011  "effet_I"=rnorm(dim1,0,1),"effet_P"=rnorm(dim2,0,1), "inter"=inter0)
1012    }
1013    mod.Z08<<-jags(inits=init.funZ08,model.file = "modelZ08_code.txt",data =
1014  list("cooc","visit","ab_I","dim1","dim2"),parameters.to.save =
1015  c("mu","effet_I","effet_P","tau_I","tau_P","gamma","beta","theta0","epsilon","loglik"),n.chains = 1,
1016  n.iter=1000000, n.burnin = 250000, n.thin = 250)
1017    mod.Z08.mcmc<-as.mcmc(mod.Z08)
1018    mZ08<-mod.Z08$BUGSoutput$sims.list
1019    mZ08.deviance<-mZ08$deviance
1020    mZ08.loglik<-mZ08$loglik

```

```

1021     dimSEM<-dim(mZ08.loglik)[1]
1022     list.mZ08<-sapply(1:dimSEM,function(x) matrix(mZ08.loglik[x,,],nrow=dim1*dim2))
1023     list.tmZ08<-(t(list.mZ08))
1024     mZ08.loo<-loo(list.tmZ08)
1025     mZ08.loo
1026     loo_file<-paste(dossier, "/", site, "_Z08_loo.txt", sep="")
1027     write_values("mZ08", app=T, loo_file)
1028     mZ08_loo_pointwise<-mZ08.loo$pointwise
1029     mZ08_loo_pareto_k<-mZ08.loo$pareto_k
1030     mZ08.loo$pareto_k<-NULL
1031     mZ08.loo$pointwise<-NULL
1032     write_values(as.matrix(mZ08.loo), app=T, loo_file)
1033     save.image(paste(dossier, "/", site, "_Z08.RData", sep=""))
1034 }
1035 ### MODEL Z07
1036 mZ07<-function(){
1037     init.funZ07 <-function(){
1038         list("tau_I" = rexp(1,10), "tau_P" = rexp(1,10), "alpha" = 0.1,"beta" = rnorm(1,0,1), "delta" =
1039         rnorm(1,0,1), "theta0" = rnorm(1,0,1), "effet_I"=rnorm(dim1,0,1),"effet_P"=rnorm(dim2,0,1),
1040         "inter"=inter0)
1041     }
1042     mod.Z07<<-jags(inits=init.funZ07,model.file = "modelZ07_code.txt",data =
1043     list("cooc","visit","ab_P","dim1","dim2"),parameters.to.save =
1044     c("mu","effet_I","effet_P","tau_I","tau_P","alpha","delta","beta","theta0","loglik"),n.chains = 1,
1045     n.iter=1000000, n.burnin = 250000, n.thin = 250)
1046     mod.Z07.mcmc<-as.mcmc(mod.Z07)

```

```

1047     mZ07<-mod.Z07$BUGSoutput$sims.list
1048     mZ07.deviance<-mZ07$deviance
1049     mZ07.loglik<-mZ07$loglik
1050     dimSEM<-dim(mZ07.loglik)[1]
1051     list.mZ07<-sapply(1:dimSEM,function(x) matrix(mZ07.loglik[x,,],nrow=dim1*dim2))
1052     list.tmZ07<-(t(list.mZ07))
1053     mZ07.loo<-loo(list.tmZ07)
1054     mZ07.loo
1055     loo_file<-paste(dossier, "/", site, "_Z07_loo.txt", sep="")
1056     write_values("mZ07", app=T, loo_file)
1057     mZ07_loo_pointwise<-mZ07.loo$pointwise
1058     mZ07_loo_pareto_k<-mZ07.loo$pareto_k
1059     mZ07.loo$pareto_k<-NULL
1060     mZ07.loo$pointwise<-NULL
1061     write_values(as.matrix(mZ07.loo), app=T, loo_file)
1062     save.image(paste(dossier, "/", site, "_Z07.RData", sep=""))
1063 }
1064 ### MODEL Z06
1065 mZ06<-function(){
1066     init.funZ06 <-function(){
1067         list("tau_I" = rexp(1,10), "tau_P" = rexp(1,10), "alpha" = 0.1, "beta" = rnorm(1,0,1), "gamma"
1068 = rnorm(1,0,1), "theta0" = rnorm(1,0,1), "effet_I"=rnorm(dim1,0,1),"effet_P"=rnorm(dim2,0,1),
1069 "inter"=inter0)
1070     }
1071     mod.Z06<<-jags(inits=init.funZ06,model.file = "modelZ06_code.txt",data =
1072 list("cooc","visit","ab_I","dim1","dim2"),parameters.to.save =

```

```

1073 c("mu","effet_I","effet_P","tau_I","tau_P","alpha","gamma","beta","theta0","loglik"),n.chains = 1,
1074 n.iter=1000000, n.burnin = 250000, n.thin = 250)
1075     mod.Z06.mcmc<-as.mcmc(mod.Z06)
1076     mZ06<-mod.Z06$BUGSoutput$sims.list
1077     mZ06.deviance<-mZ06$deviance
1078     mZ06.loglik<-mZ06$loglik
1079     dimSEM<-dim(mZ06.loglik)[1]
1080     list.mZ06<-sapply(1:dimSEM,function(x) matrix(mZ06.loglik[x,,],nrow=dim1*dim2))
1081     list.tmZ06<-(t(list.mZ06))
1082     mZ06.loo<-loo(list.tmZ06)
1083     mZ06.loo
1084     loo_file<-paste(dossier, "/", site, "_Z06_loo.txt", sep="")
1085     write_values("mZ06", app=T, loo_file)
1086     mZ06_loo_pointwise<-mZ06.loo$pointwise
1087     mZ06_loo_pareto_k<-mZ06.loo$pareto_k
1088     mZ06.loo$pareto_k<-NULL
1089     mZ06.loo$pointwise<-NULL
1090     write_values(as.matrix(mZ06.loo), app=T, loo_file)
1091     save.image(paste(dossier, "/", site, "_Z06.RData", sep=""))
1092 }
1093 ### MODEL Z05
1094 mZ05<-function(){
1095     init.funZ05 <-function(){
1096         list("tau_I" = rexp(1,10), "tau_P" = rexp(1,10), "alpha" = 0.1,"beta" = rnorm(1,0,1), "theta0"
1097 = rnorm(1,0,1), "epsilon" = rnorm(1,0,1), "effet_I"=rnorm(dim1,0,1),"effet_P"=rnorm(dim2,0,1),
1098 "inter"=inter0)

```

```

1099     }
1100     mod.Z05<-jags(inits=init.funZ05,model.file = "modelZ05_code.txt",data =
1101 list("cooc","visit","dim1","dim2"),parameters.to.save =
1102 c("mu","effet_I","effet_P","tau_I","tau_P","alpha","beta","theta0","epsilon","loglik"),n.chains = 1,
1103 n.iter=1000000, n.burnin = 250000, n.thin = 250)
1104     mod.Z05.mcmc<-as.mcmc(mod.Z05)
1105     mZ05<-mod.Z05$BUGSoutput$sims.list
1106     mZ05.deviance<-mZ05$deviance
1107     mZ05.loglik<-mZ05$loglik
1108     dimSEM<-dim(mZ05.loglik)[1]
1109     list.mZ05<-sapply(1:dimSEM,function(x) matrix(mZ05.loglik[x,,],nrow=dim1*dim2))
1110     list.tmZ05<-(t(list.mZ05))
1111     mZ05.loo<-loo(list.tmZ05)
1112     mZ05.loo
1113     loo_file<-paste(dossier, "/", site, "_Z05_loo.txt", sep="")
1114     write_values("mZ05", app=T, loo_file)
1115     mZ05_loo_pointwise<-mZ05.loo$pointwise
1116     mZ05_loo_pareto_k<-mZ05.loo$pareto_k
1117     mZ05.loo$pareto_k<-NULL
1118     mZ05.loo$pointwise<-NULL
1119     write_values(as.matrix(mZ05.loo), app=T, loo_file)
1120     save.image(paste(dossier, "/", site, "_Z05.RData", sep=""))
1121 }
1122 ### MODEL Z04
1123 mZ04<-function(){
1124     init.funZ04 <-function(){

```

```

1125     list("tau_I" = rexp(1,10), "tau_P" = rexp(1,10), "beta" = rnorm(1,0,1), "gamma" =
1126 rnorm(1,0,1), "delta" = rnorm(1,0,1), "theta0" = rnorm(1,0,1), "epsilon" = rnorm(1,0,1),
1127 "effet_I"=rnorm(dim1,0,1),"effet_P"=rnorm(dim2,0,1), "inter"=inter0)
1128     }
1129     mod.Z04<-jags(inits=init.funZ04,model.file = "modelZ04_code.txt",data =
1130 list("cooc","visit","ab_I","ab_P","dim1","dim2"),parameters.to.save =
1131 c("mu","effet_I","effet_P","tau_I","tau_P","gamma","delta","beta","theta0","epsilon","loglik"),n.chai
1132 ns = 1, n.iter=1000000, n.burnin = 250000, n.thin = 250)
1133     mod.Z04.mcmc<-as.mcmc(mod.Z04)
1134     mZ04<-mod.Z04$BUGSoutput$sims.list
1135     mZ04.deviance<-mZ04$deviance
1136     mZ04.loglik<-mZ04$loglik
1137     dimSEM<-dim(mZ04.loglik)[1]
1138     list.mZ04<-sapply(1:dimSEM,function(x) matrix(mZ04.loglik[x,,],nrow=dim1*dim2))
1139     list.tmZ04<-t(list.mZ04)
1140     mZ04.loo<-loo(list.tmZ04)
1141     mZ04.loo
1142     loo_file<-paste(dossier, "/", site, "_Z04_loo.txt", sep="")
1143     write_values("mZ04", app=T, loo_file)
1144     mZ04_loo_pointwise<-mZ04.loo$pointwise
1145     mZ04_loo_pareto_k<-mZ04.loo$pareto_k
1146     mZ04.loo$pareto_k<-NULL
1147     mZ04.loo$pointwise<-NULL
1148     write_values(as.matrix(mZ04.loo), app=T, loo_file)
1149     save.image(paste(dossier, "/", site, "_Z04.RData", sep=""))
1150 }

```

```

1151   ### MODEL Z03
1152   mZ03<-function(){
1153       init.funZ03 <-function(){
1154           list("tau_I" = rexp(1,10), "tau_P" = rexp(1,10), "alpha" = 0.1,"beta" = rnorm(1,0,1), "gamma"
1155   = rnorm(1,0,1), "theta0" = rnorm(1,0,1), "epsilon" = rnorm(1,0,1),
1156   "effet_I"=rnorm(dim1,0,1),"effet_P"=rnorm(dim2,0,1), "inter"=inter0)
1157       }
1158       mod.Z03<<-jags(inits=init.funZ03,model.file = "modelZ03_code.txt",data =
1159   list("cooc","visit","ab_I","dim1","dim2"),parameters.to.save =
1160   c("mu","effet_I","effet_P","tau_I","tau_P","alpha","gamma","beta","theta0","epsilon","loglik"),n.cha
1161   ins = 1, n.iter=1000000, n.burnin = 250000, n.thin = 250)
1162       mod.Z03.mcmc<-as.mcmc(mod.Z03)
1163       mZ03<-mod.Z03$BUGSoutput$sims.list
1164       mZ03.deviance<-mZ03$deviance
1165       mZ03.loglik<-mZ03$loglik
1166       dimSEM<-dim(mZ03.loglik)[1]
1167       list.mZ03<-sapply(1:dimSEM,function(x) matrix(mZ03.loglik[x,,],nrow=dim1*dim2))
1168       list.tmZ03<-(t(list.mZ03))
1169       mZ03.loo<-loo(list.tmZ03)
1170       mZ03.loo
1171       loo_file<-paste(dossier, "/", site, "_Z03_loo.txt", sep="")
1172       write_values("mZ03", app=T, loo_file)
1173       mZ03_loo_pointwise<-mZ03.loo$pointwise
1174       mZ03_loo_pareto_k<-mZ03.loo$pareto_k
1175       mZ03.loo$pareto_k<-NULL
1176       mZ03.loo$pointwise<-NULL

```

```

1177     write_values(as.matrix(mZ03.loo), app=T, loo_file)
1178     save.image(paste(dossier, "/", site, "_Z03.RData", sep=""))
1179 }
1180 ### MODEL Z02
1181 mZ02<-function(){
1182     init.funZ02 <-function(){
1183         list("tau_I" = rexp(1,10), "tau_P" = rexp(1,10), "alpha" = 0.1, "beta" = rnorm(1,0,1), "delta" =
1184 rnorm(1,0,1), "theta0" = rnorm(1,0,1), "epsilon" = rnorm(1,0,1),
1185 "effet_I"=rnorm(dim1,0,1),"effet_P"=rnorm(dim2,0,1), "inter"=inter0)
1186     }
1187     mod.Z02<<-jags(inits=init.funZ02,model.file = "modelZ02_code.txt",data =
1188 list("cooc","visit","ab_P","dim1","dim2"),parameters.to.save =
1189 c("mu","effet_I","effet_P","tau_I","tau_P","alpha","delta","beta","theta0","epsilon","loglik"),n.chain
1190 s = 1, n.iter=1000000, n.burnin = 250000, n.thin = 250)
1191     mod.Z02.mcmc<-as.mcmc(mod.Z02)
1192     mZ02<-mod.Z02$BUGSoutput$sims.list
1193     mZ02.deviance<-mZ02$deviance
1194     mZ02.loglik<-mZ02$loglik
1195     dimSEM<-dim(mZ02.loglik)[1]
1196     list.mZ02<-sapply(1:dimSEM,function(x) matrix(mZ02.loglik[x,,],nrow=dim1*dim2))
1197     list.tmZ02<-(t(list.mZ02))
1198     mZ02.loo<-loo(list.tmZ02)
1199     mZ02.loo
1200     loo_file<-paste(dossier, "/", site, "_Z02_loo.txt", sep="")
1201     write_values("mZ02", app=T, loo_file)
1202     mZ02_loo_pointwise<-mZ02.loo$pointwise

```

```

1203     mZ02_loo_pareto_k<-mZ02.loo$pareto_k
1204     mZ02.loo$pareto_k<-NULL
1205     mZ02.loo$pointwise<-NULL
1206     write_values(as.matrix(mZ02.loo), app=T, loo_file)
1207     save.image(paste(dossier, "/", site, "_Z02.RData", sep=""))
1208 }
1209 ### MODEL Z01
1210 mZ01<-function(){
1211     init.funZ01 <-function(){
1212         list("tau_I" = rexp(1,10), "tau_P" = rexp(1,10), "alpha" = 0.1, "beta" = rnorm(1,0,1), "gamma"
1213 = rnorm(1,0,1), "delta" = rnorm(1,0,1), "theta0" = rnorm(1,0,1),
1214 "effet_I"=rnorm(dim1,0,1),"effet_P"=rnorm(dim2,0,1), "inter"=inter0)
1215     }
1216     mod.Z01<<-jags(inits=init.funZ01,model.file = "modelZ01_code.txt",data =
1217 list("cooc","visit","ab_I","ab_P", "dim1", "dim2"),parameters.to.save =
1218 c("mu","effet_I","effet_P","tau_I","tau_P","alpha","gamma","delta","beta","theta0","loglik"),n.chain
1219 s = 1, n.iter=1000000, n.burnin = 250000, n.thin = 250)
1220     mod.Z01.mcmc<-as.mcmc(mod.Z01)
1221     mZ01<-mod.Z01$BUGSoutput$sims.list
1222     mZ01.deviance<-mZ01$deviance
1223     mZ01.loglik<-mZ01$loglik
1224     dimSEM<-dim(mZ01.loglik)[1]
1225     list.mZ01<-sapply(1:dimSEM,function(x) matrix(mZ01.loglik[x,,],nrow=dim1*dim2))
1226     list.tmZ01<-(t(list.mZ01))
1227     mZ01.loo<-loo(list.tmZ01)
1228     mZ01.loo

```

```

1229     loo_file<-paste(dossier, "/", site, "_Z01_loo.txt", sep="")
1230     write_values("mZ01", app=T, loo_file)
1231     mZ01_loo_pointwise<-mZ01.loo$pointwise
1232     mZ01_loo_pareto_k<-mZ01.loo$pareto_k
1233     mZ01.loo$pareto_k<-NULL
1234     mZ01.loo$pointwise<-NULL
1235     write_values(as.matrix(mZ01.loo), app=T, loo_file)
1236     save.image(paste(dossier, "/", site, "_Z01.RData", sep=""))
1237 }
1238 ### MODEL Z00
1239 mZ00<-function(){
1240     init.funZ00 <-function(){
1241         list("tau_I" = rexp(1,10), "tau_P" = rexp(1,10), "alpha" = 0.1,"beta" = rnorm(1,0,1), "gamma"
1242 = rnorm(1,0,1), "delta" = rnorm(1,0,1), "theta0" = rnorm(1,0,1), "epsilon" = rnorm(1,0,1),
1243 "effet_I"=rnorm(dim1,0,1),"effet_P"=rnorm(dim2,0,1), "inter"=inter0)
1244     }
1245     mod.Z00<<-jags(inits=init.funZ00,model.file = "modelZ00_code.txt",data =
1246 list("cooc","visit","ab_I","ab_P","dim1","dim2"),parameters.to.save =
1247 c("mu","effet_I","effet_P","tau_I","tau_P","alpha","gamma","delta","beta","theta0","epsilon","loglik
1248 "),n.chains = 1, n.iter=1000000, n.burnin = 250000, n.thin = 250)
1249     mod.Z00.mcmc<-as.mcmc(mod.Z00)
1250     mZ00<-mod.Z00$BUGSoutput$sims.list
1251     mZ00.deviance<-mZ00$deviance
1252     mZ00.loglik<-mZ00$loglik
1253     dimSEM<-dim(mZ00.loglik)[1]
1254     list.mZ00<-sapply(1:dimSEM,function(x) matrix(mZ00.loglik[x,,],nrow=dim1*dim2))

```

```

1255     list.tmZ00<-(t(list.mZ00))
1256     mZ00.loo<-loo(list.tmZ00)
1257     mZ00.loo
1258     loo_file<-paste(dossier, "/", site, "_Z00_loo.txt", sep="")
1259     write_values("mZ00", app=T, loo_file)
1260     mZ00_loo_pointwise<-mZ00.loo$pointwise
1261     mZ00_loo_pareto_k<-mZ00.loo$pareto_k
1262     mZ00.loo$pareto_k<-NULL
1263     mZ00.loo$pointwise<-NULL
1264     write_values(as.matrix(mZ00.loo), app=T, loo_file)
1265     save.image(paste(dossier, "/", site, "_Z00.RData", sep=""))
1266 }
1267 ##### end model functions
1268 print("JOB DONE")
1269 #####
1270 ###   Network information (do not change)   ###
1271 #####
1272 #####BLOCK 3 – MODEL EXECUTION #####
1273 #launch_modele<-function(){
1274     ntw<-read.table(paste(dossier, "/", site, "_ntw.txt", sep=""),
1275     sep="\t",header=T,row.names=1)
1276     dim1<-dim(ntw)[1]
1277     dim2<-dim(ntw)[2]
1278     web<-as.matrix(ntw,dim1,dim2)
1279     inter0<-dget(paste(dossier, "/", site, "_web_i.txt", sep=""))
1280     cooc<-dget(paste(dossier, "/", site, "_co.txt", sep=""))

```

```

1281     visit<-read.table(paste(dossier, "/", site, "_ntw.txt", sep=""),sep="\t",header=T)
1282     visit<-as.matrix(visit)
1283     abundancel<-read.table(paste(dossier, "/", site, "_abl.txt", sep=""), sep="\t", header=T)
1284     ab_I <- log(abundancel[,2])
1285     abundanceP<-read.table(paste(dossier, "/", site, "_abP.txt", sep=""), sep="\t", header=T)
1286     ab_P <- log(abundanceP[,2])
1287     if(opt$modele == "all")
1288     {
1289         print("modele: all")
1290         for(i in 0:15)
1291         {
1292             print(paste("COMPUTING MODELE ", i, "\n", sep=""))
1293             mod<-eval(parse(text=paste("mZ0", i, sep="")))
1294             mod()
1295         }
1296     }else{
1297         print(paste("modele: ", opt$modele), sep="")
1298         mod<-eval(parse(text=paste("m", opt$modele, sep="")))      #recupération de la
1299     fonction du modele
1300         mod()
1301     }
1302     ##### end model execution
1303     #launch_modele()
1304
1305
1306     #####PARAMETER VALUES#####

```

```

1307 library(optparse)
1308 option_list = list(
1309     make_option(c("-d", "--dir"), type="character", default=NULL, help="model directory",
1310     metavar="character"),
1311     make_option(c("-s", "--site"), type="character", default=NULL, help="site name",
1312     metavar="character"))
1313 opt_parser = OptionParser(option_list=option_list);
1314 opt = parse_args(opt_parser);
1315 rdata<-list.files(opt$dir, pattern="*_Z015.RData")
1316 load(paste(opt$dir, "/", rdata, sep="")) #chargement du RData qui contient tous les modèles pour un
1317 site donné
1318 print(paste("RData ", rdata, " loaded", sep=""))
1319 for(mod in ls(pattern="mod.Z0*"))
1320 {
1321     print(paste("getting values from ", mod, sep=""))
1322     model<-eval(parse(text=mod))
1323     if(is.null(model$BUGSoutput$mean$alpha)){model$BUGSoutput$mean$alpha<-NA}
1324     if(is.null(model$BUGSoutput$mean$beta)){model$BUGSoutput$mean$beta<-NA}
1325     if(is.null(model$BUGSoutput$mean$delta)){model$BUGSoutput$mean$delta<-NA}
1326     if(is.null(model$BUGSoutput$mean$epsilon)){model$BUGSoutput$mean$epsilon<-NA}
1327     if(is.null(model$BUGSoutput$mean$gamma)){model$BUGSoutput$mean$gamma<-NA}
1328     val<-matrix(c(model$BUGSoutput$mean$alpha, model$BUGSoutput$mean$beta,
1329     model$BUGSoutput$mean$delta, model$BUGSoutput$mean$epsilon,
1330     model$BUGSoutput$mean$gamma), 1, 5, dimnames=list("values", c("alpha", "beta", "delta",
1331     "epsilon", "gamma")))

```

```
1332     write.table(val, file=paste(opt$dir, "/", opt$site, "_", mod, "_values.txt", sep=""), quote=F,  
1333 sep="\t", row.names=F, col.names=T)  
1334 }  
1335
```

1336 **Appendix S3: Modularity and latent block model analysis**

1337 We calculated the modularity of the network using the `cluster_leading_eigen` method for  
1338 modularity optimization implemented in the `igraph` package (Csardi and Nepusz 2006, Newman  
1339 2006). We then performed latent block models (LBM) using the `BM_poisson` method for  
1340 quantitative network data implemented in the `blockmodels` package (Leger et al. 2015). Blocks  
1341 are calculated separately for the two groups (insect and plant) based on the number of visits (*i.e.* a  
1342 weighted network). The algorithm finds the best divisions of insects and plants through fitting one  
1343 Poisson parameter in each block of the visit matrix, thus essentially maximizing the ICL (Integrated  
1344 Completed Likelihood; Biernacki et al. 2000, Daudin et al. 2007).

---

```
1345  
1346 library(bipartite)  
1347 library(vegan)  
1348 library(igraph)  
1349 library(dummies)  
1350 library(blockmodels)  
1351 library(ade4)  
1352 library(fields)  
1353  
1354 #site data (ex: Bois de Fontaret, BFs)  
1355 BFs<-read.table("ntwBFs.txt",header=T,sep="\t")  
1356 webBFs <- as.matrix(BFs)  
1357 ##### Modularity analysis, binary data #####  
1358 BFs.graph.bin<-graph_from_incidence_matrix(webBFs,multiple=F) #binary  
1359 BFs.bin.cle<-cluster_leading_eigen(BFs.graph.bin)  
1360 BFs.bin.cle  
1361 #get phenology overlap matrix
```

```

1362 coBF<-dget("coBFs.txt")
1363 ##### LBM code: LBM analysis following Poisson #####
1364 bmi_BFs<-BM_poisson('LBM', webBFs)
1365 bmi_BFs$estimate()
1366 numi_BFs<-which.max(bmi_BFs$ICL)
1367 densi_BFs<-sum(webBFs)/(nrow(webBFs)*ncol(webBFs))
1368 probi_BFs<-bmi_BFs$model_parameters[[numi_BFs]]$lambda
1369 row.nb.gpi<-nrow(probi_BFs)
1370 col.nb.gpi<-ncol(probi_BFs)
1371 prob.rowi<-bmi_BFs$memberships[[numi_BFs]]$Z1
1372 hh.namei<-rownames(webBFs)
1373 mbrshp.hhi<-apply(prob.rowi,1,which.max)
1374 ls.freq.rowi<-rowSums(webBFs)
1375 res.hhi<-cbind.data.frame(hh.namei=hh.namei, mbrshp.hhi=mbrshp.hhi, freq.hhi=ls.freq.rowi)
1376 res.hh.ordi<-res.hhi[order(res.hhi$freq.hhi),]
1377 cpt=0
1378 for(k in 1: (nrow(res.hh.ordi)-1))
1379 {
1380   if (res.hh.ordi$mbrshp.hhi[k] !=res.hh.ordi$mbrshp.hhi[k+1]) cpt=cpt+1
1381 }
1382 nb.diff.hhi=cpt-(length(levels(as.factor(res.hh.ordi$mbrshp.hhi)))-1)
1383 #write tables
1384 write.table(res.hh.ordi,sep="\t",row.names=FALSE)
1385 prob.coli<-bmi_BFs$memberships[[numi_BFs]]$Z2
1386 sp.namei<-colnames(webBFs)
1387 mbrshp.spi<-apply(prob.coli,1,which.max)

```

```

1388 ls.freq.coli<-colSums(webBFs)
1389 res.spi<-cbind.data.frame(sp.namei=sp.namei, mbrshp.spi=mbrshp.spi, freq.spi=ls.freq.coli)
1390 res.sp.ordi<-res.spi[order(res.spi$freq.spi),]
1391 cpt=0
1392 for (k in 1: (nrow(res.sp.ordi)-1))
1393 {
1394   if(res.sp.ordi$mbrshp.spi[k] !=res.sp.ordi$mbrshp.spi[k+1]) cpt=cpt+1
1395 }
1396 nb.diff.spi=cpt-(length(levels(as.factor(res.sp.ordi$mbrshp.spi)))-1)
1397 res.sp.ord2i=res.spi[order(res.spi$mbrshp.spi),]
1398 write.table(res.sp.ordi,sep="\t",row.names=FALSE)
1399 write.table(probi_BFs,file="_prob_BFs",sep="\t",row.names=FALSE)
1400
1401 ##### Matrix organization #####
1402 par(mfrow=c(1,1))
1403 webBFs2<-webBFs
1404 webBFs[which(webBFs>1)]=1
1405 nb.row=nrow(webBFs)
1406 nb.col=ncol(webBFs)
1407 nds=webBFs
1408 nps=coBF
1409 res.prob=read.table("_prob_BFs",sep="\t",h=TRUE)
1410 ls.ord.col.prob=order(colSums(res.prob),decreasing=TRUE)
1411 ls.ord.row.prob=order(rowSums(res.prob),decreasing=TRUE)
1412 ls.ord.hhi=apply(res.hhi$mbrshp.hhi,function(x) which (x==ls.ord.row.prob))
1413 res.hh.ord2i=res.hhi[order(ls.ord.hhi),]

```

```

1414 row.nb.gpi=length(levels(as.factor(res.hhi$mbrshp.hhi)))
1415 res.hh.ord3i=NULL
1416 for (h in ls.ord.row.prob)
1417 {
1418   part=res.hh.ord2i[res.hh.ord2i$mbrshp.hhi==h,]
1419   part.ord=part[order(part$freq.hhi,decreasing=TRUE),]
1420   res.hh.ord3i=rbind.data.frame(res.hh.ord3i,part.ord)
1421 }
1422 ls.ord.sp=sapply(res.spi$mbrshp.spi,function(x) which (x==ls.ord.col.prob))
1423 res.sp.ord2i=res.spi[order(ls.ord.sp),]
1424 col.nb.gb=length(levels(as.factor(res.spi$mbrshp.spi)))
1425 res.sp.ord3i=NULL
1426 for (h in ls.ord.col.prob)
1427 {
1428   part=res.sp.ord2i[res.sp.ord2i$mbrshp.spi==h,]
1429   part.ord=part[order(part$freq.spi,decreasing=TRUE),]
1430   res.sp.ord3i=rbind.data.frame(res.sp.ord3i,part.ord)
1431 }
1432 nds=nds[as.character(res.hh.ord3i$hh.namei),as.character(res.sp.ord3i$sp.namei)]
1433 nps=nps[as.character(res.hh.ord3i$hh.namei),as.character(res.sp.ord3i$sp.namei)]
1434 webBFs2=webBFs2[as.character(res.hh.ord3i$hh.namei),as.character(res.sp.ord3i$sp.namei)]
1435
1436 ##### Plot matrix with heatcolours and the number of visits #####
1437 visits<-matrix(webBFs2,nrow=dim(webBFs2)[1]*dim(webBFs2)[2],ncol=1)
1438 visits<-visits[which(visits>0)] #without the zeros
1439 coord.function<-function(x,nI,nP){

```

```

1440   c(((x-1)%%nl)+1,((x-1)%/%nl)+1)
1441   }
1442   func.plot.matrix<-function(x,y){
1443     indices<-which(x==1)
1444     min<-min(y)
1445     max<-max(y)
1446     yLabels<-rownames(x)
1447     xLabels<-colnames(x)
1448     title<-c("Bois de Fontaret")
1449     if(is.null(xLabels)){
1450       xLabels<-c(1:ncol(x))
1451     }
1452     if(is.null(yLabels)){
1453       yLabels<-c(1:nrow(x))
1454     }
1455     reverse<-nrow(x):1
1456     yLabels<-yLabels[reverse]
1457     y<-y[reverse,]
1458     image.plot(1:length(xLabels),1:length(yLabels),t(y),col=c("white",heat.colors(12)[12:1]), xlab="",
1459     ylab="",axes=FALSE,zlim=c(min,max))
1460     if(!is.null(title)){
1461       title(ylab="Insects", line=8, cex.lab=1)
1462       title(xlab="Plants", line=6, cex.lab=1.2)
1463       title("Bois de Fontaret")
1464     }
1465     axis(BELOW<-1,at=1:length(xLabels),labels=as.factor(as.character(xLabels)),las =2, cex.axis=0.6)

```

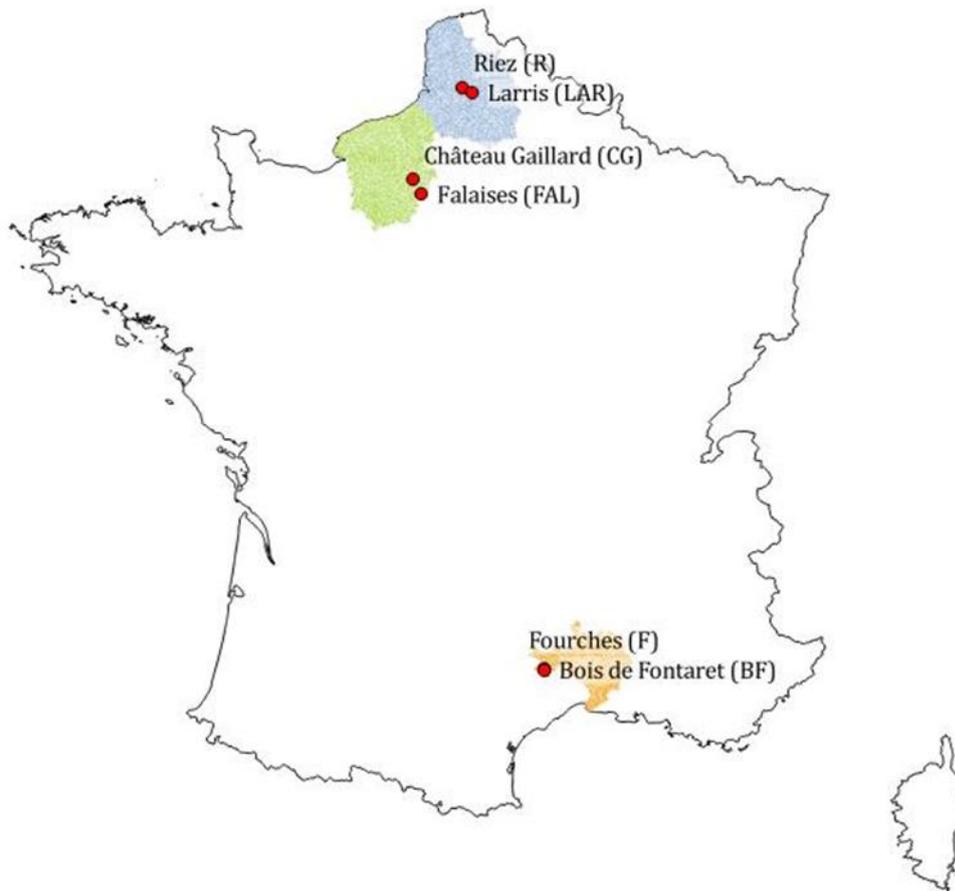
```

1466 axis(LEFT<-2,at=1:length(yLabels), labels=as.factor(as.character(yLabels)),las= 2,cex.axis=0.6)
1467 axis(BELOW<-1,at=1:length(xLabels),labels=rep("",length(xLabels)),las =2,cex.axis=0.6)
1468 axis(LEFT<-2,at=1:length(yLabels),labels=rep("",length(yLabels)),las=2,cex.axis<-0.6)
1469 coo<-t(rbind(sapply(indices,function(xx) coord.function(xx,nrow(x),ncol(x))))))
1470 text(coo[,2],nrow(webBFs)+1-coo[,1],labels=visits, cex=0.6)
1471 }
1472 func.plot.matrix(nds,nps)
1473 ##### Black lines to delimit blocks in the plot #####
1474 if (row.nb.gpi>1)
1475 {
1476 ls.class=as.numeric(as.data.frame(table(res.hh.ord2i$mbrshp.hhi))[ls.ord.row.prob,2])
1477 ls.cum=sum(ls.class)-cumsum(ls.class)
1478 abline(h=ls.cum+0.5,col="grey20", lwd=3)
1479 }
1480 if (col.nb.gpi>1)
1481 {
1482 ls.class=as.numeric(as.data.frame(table(res.sp.ord2i$mbrshp.spi))[ls.ord.col.prob,2])
1483 ls.cum=cumsum(ls.class)
1484 abline(v=ls.cum+0.5,col="grey20", lwd=3)
1485 }

```

1486

## Figures and Tables

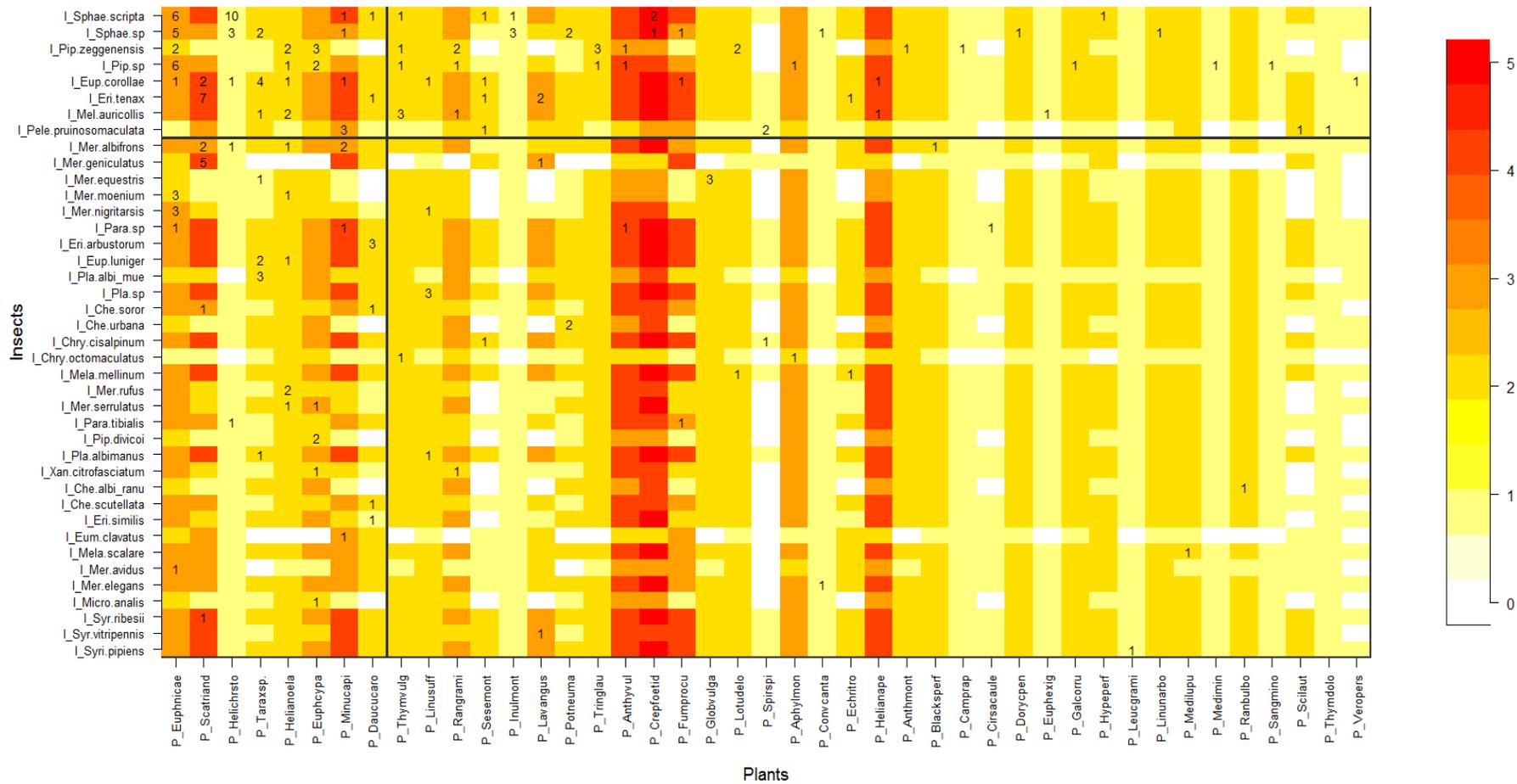


1487

1488 Figure S1. Site location in France: in blue the French départements Pas-de-Calais and Somme (Hauts-  
1489 de-France region), in green the départements Eure and Seine Maritime (Normandie region), in orange  
1490 the département Gard (Occitanie region). The six sites correspond to the red dots.

1491

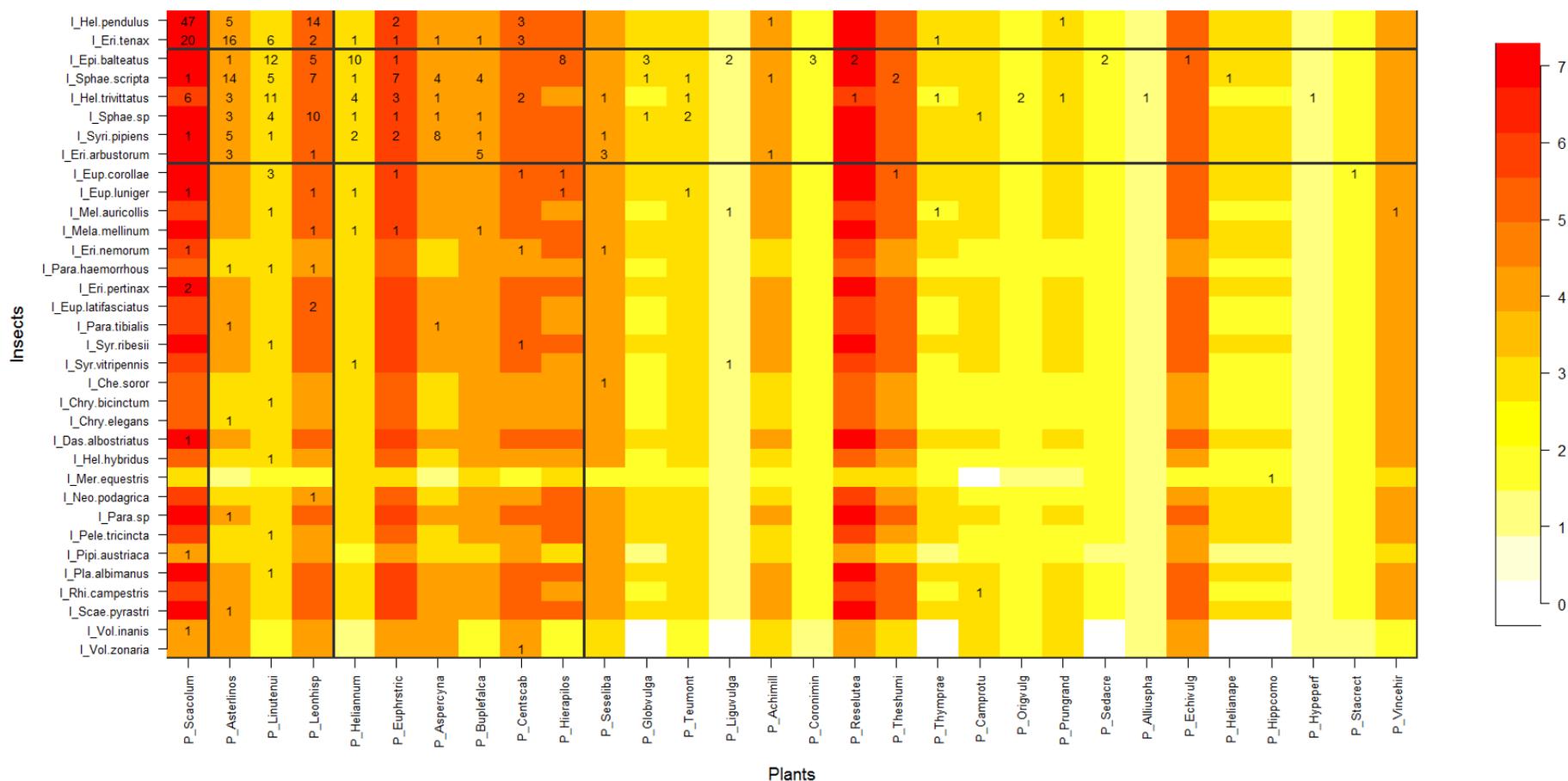
Bois de Fontaret



1492

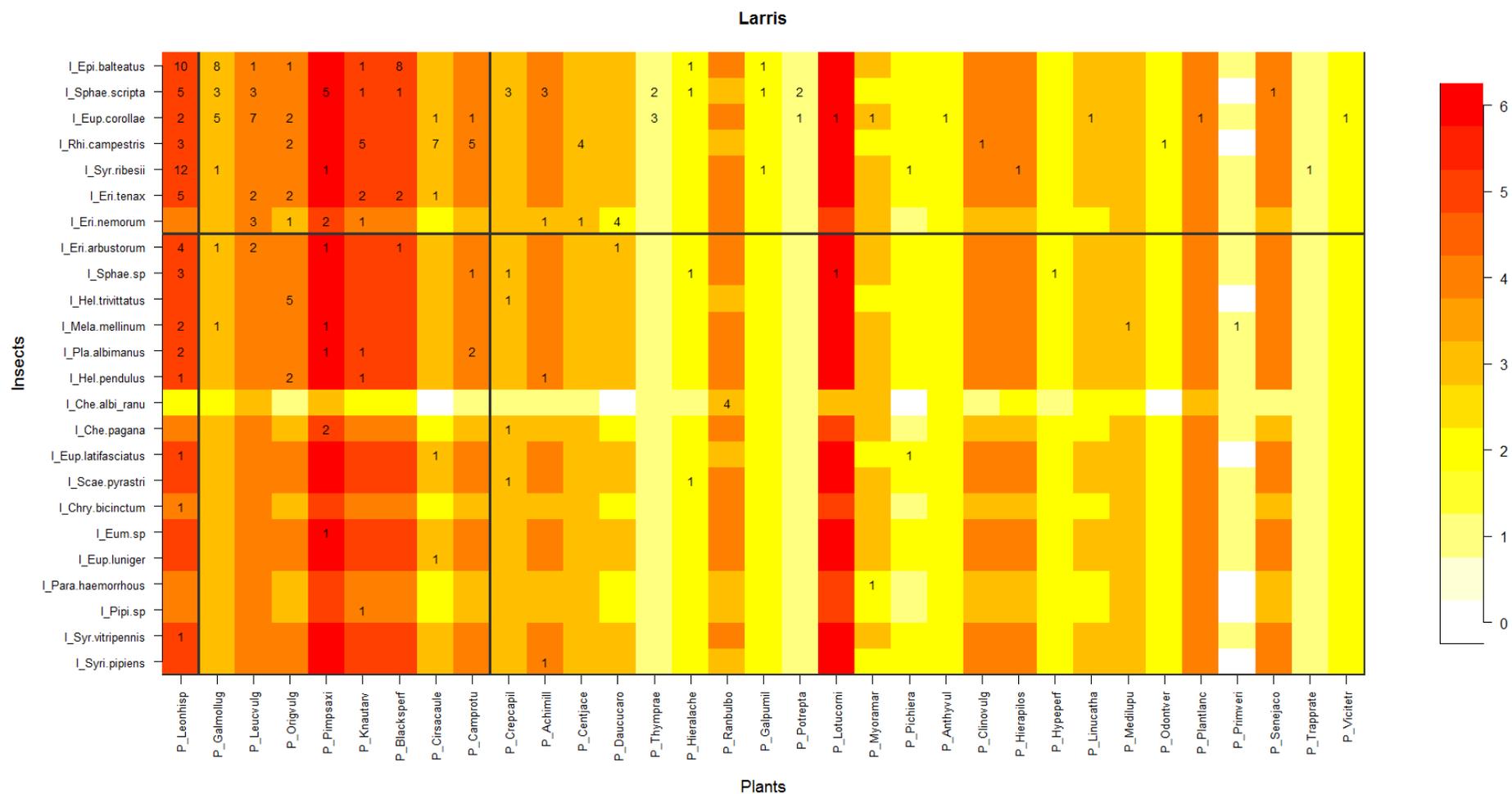
1493 Figure S2. Block clustering provided by LBM in the site of Bois de Fontaret (BF, Occitanie), overlaid on a heatmap of species phenology overlap. Insect species  
 1494 are displayed in rows and plant species in columns, following their degree (number of partners). The blocks of insects and the blocks of plants are separated  
 1495 by solid black lines. Colours correspond to the number of months that are shared by each pair of plant and insect species (PO, phenology overlap), with higher  
 1496 PO corresponding to darker colours. Numbers are the number of visits observed in the field for a given plant-insect pair.

### Falaises



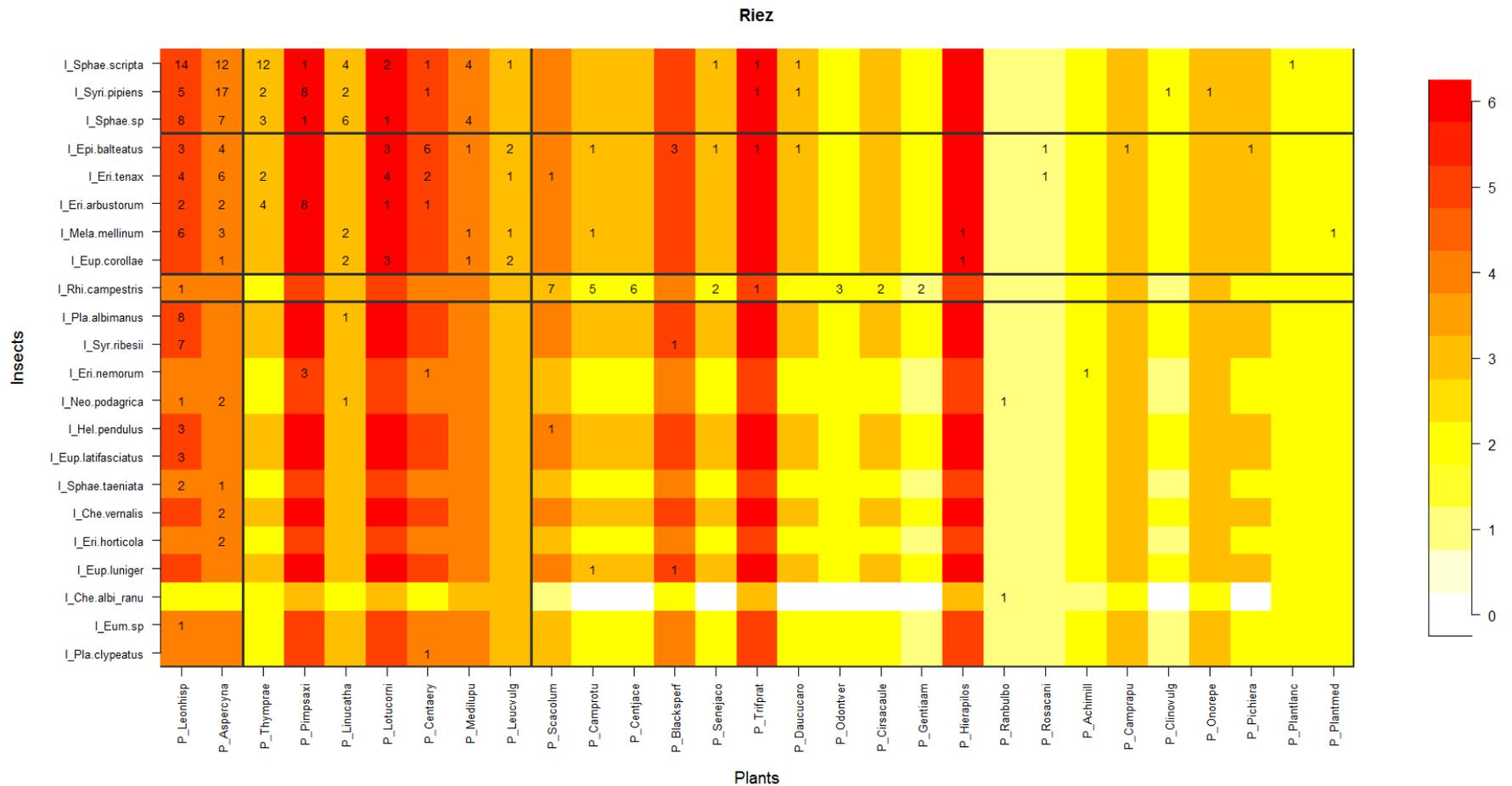
1497

1498 Figure S3. Block clustering provided by LBM in the site of Falaises (FAL, Normandie), overlaid on a heatmap of species phenology overlap. Insect species are  
 1499 displayed in rows and plant species in columns, following their degree (number of partners). The blocks of insects and the blocks of plants are separated by  
 1500 solid black lines. Colours correspond to the number of months that are shared by each pair of plant and insect species (PO, phenology overlap), with higher  
 1501 PO corresponding to darker colours. Numbers are the number of visits observed in the field for a given plant-insect pair.



1502

1503 Figure S4. Block clustering provided by LBM in the site of Larris (LAR, Hauts-de-France), overlaid on a heatmap of species phenology overlap. Insect species  
 1504 are displayed in rows and plant species in columns, following their degree (number of partners). The blocks of insects and the blocks of plants are separated  
 1505 by solid black lines. Colours correspond to the number of months that are shared by each pair of plant and insect species (PO, phenology overlap), with higher  
 1506 PO corresponding to darker colours. Numbers are the number of visits observed in the field for a given plant-insect pair.



1507

1508 Figure S5. Block clustering provided by LBM in the site of Riez (R, Hauts-de-France), overlaid on a heatmap of species phenology overlap. Insect species are  
 1509 displayed in rows and plant species in columns, following their degree (number of partners). The blocks of insects and the blocks of plants are separated by  
 1510 solid black lines. Colours correspond to the number of months that are shared by each pair of plant and insect species (PO, phenology overlap), with higher  
 1511 PO corresponding to darker colours. Numbers are the number of visits observed in the field for a given plant-insect pair.

1512 Table S1. Table of transformed plant abundances. The first column shows the Braun-Blanquet  
1513 coefficients of, the second column, their percentages, and the third column, the transformed  
1514 abundances used as the plant abundances in the model.

Coefficient Braun-Blanquet	Abundance percentage interval	Abundance percentage
<i>i</i>	1 individual	0.1%
<i>+</i>	< 1 %	0.5%
<i>1</i>	1-10 %	5%
<i>2</i>	10-25 %	15%
<i>3</i>	25-50 %	35%
<i>4</i>	50-75 %	65%
<i>5</i>	75-100 %	85%

1515

1516 Table S2. Table of model accuracy. The upper part of the table shows the results of the self-validation: in the region Occitanie the self-validation was tested  
 1517 for the site Bois de Fontaret (BF ~ BF) and the site of Fourches (F ~ F); in the region Normandie for the site of Château Gaillard (CG ~ CG) and the sites of  
 1518 Falaises (FAL ~ FAL) ; and in the region Hauts-de-France for the site of Larris (LAR ~ LAR) and for the site of Riez (R ~ R). The lower part of the table shows the  
 1519 results of the cross-validation only between each site of the same region: in the region Occitanie between Bois de Fontaret et Fourches (BF ~ F and vice versa  
 1520 F ~ BF); in the region Normandie between the site of Château Gaillard and Falaises (CG ~ FAL and vice versa FAL ~ CG); and in the region Hauts-de-France  
 1521 between the site of Larris and Riez (LAR ~ R and vice versa R ~ LAR).

Model type	Region	Sites	Threshold	AUC	Omission rate	Sensitivity	Specificity	Prop correct	Kappa
Self-validation	Occitanie	BF ~ BF	0.15	0.78	0.20	0.80	0.75	0.75	0.22
	Occitanie	F ~ F	0.16	0.78	0.19	0.81	0.74	0.75	0.25
	Normandie	CG ~ CG	0.44	0.75	0.29	0.71	0.79	0.78	0.34
	Normandie	FAL ~ FAL	0.37	0.76	0.16	0.84	0.67	0.69	0.27
	Hauts-de-France	LAR ~ LAR	0.29	0.75	0.16	0.84	0.66	0.69	0.27
	Hauts-de-France	R ~ R	0.27	0.81	0.23	0.77	0.86	0.84	0.53
Cross-validation	Occitanie	BF ~ F	0.15	0.73	0.14	0.86	0.59	0.63	0.20
	Occitanie	F ~ BF	0.16	0.67	0.30	0.70	0.64	0.65	0.17
	Normandie	CG ~ FAL	0.44	0.62	0.45	0.55	0.70	0.67	0.21
	Normandie	FAL ~ CG	0.37	0.68	0.24	0.76	0.60	0.63	0.25
	Hauts-de-France	LAR ~ R	0.29	0.63	0.35	0.65	0.61	0.61	0.17
	Hauts-de-France	R ~ LAR	0.27	0.65	0.42	0.58	0.72	0.69	0.22

1522