

## **MATLAB FUNCTIONS**

### **model\_msk.m**

INFO: Implementation of the MSK model. This function simulates the dynamic response of a tumor to a radiotherapy schedule by tracking cell populations across the three specific oxygenation compartments defined in the MSK model.

#### INPUTS:

- *schedule*: treatment schedule doses, 2xn matrix, where n is the number of fraction. The first row contains the doses per fraction, and the second row containing the treatment delivery time (h) of each fraction.
- *params*: parameters of the MSK model

#### OUTPUTS:

- *t\_array*: an array of specific time points recorded during the simulation
- *N\_v\_hist*: an array with total number of viable surviving cells at each time point in *t\_array*
- *D\_hist*: an array recording the cumulative radiation dose delivered at each time point in *t\_array*

### **calculate\_EQD2\_msk.m**

INFO: This function calculates the equivalent dose in 2 Gy fractions (EQD2) for various radiotherapy schedules. It first simulates a standard reference schedule (2 Gy/fraction every 24 hours) using the `model_msk.m` function to construct a baseline spline interpolant, which maps the logarithm of surviving tumor cells to the accumulated dose. Then, it evaluates each user-provided schedule, calculates its final surviving cell count, and uses the baseline interpolant to find the mathematically equivalent dose had the treatment been delivered in standard 2 Gy fractions.

#### INPUT:

- *doses*: an array where each element represents the dose per fraction for a specific treatment schedule.
- *schedules*: cell array where each cell contains a 1D vector of administration times (in hours) corresponding to a specific treatment schedule.
- *params*: an array of 11 radiobiological parameters required by the MSK model.

#### OUTPUT:

- *EQD2\_hist\_array*: a 1D array containing the calculated final EQD2 values for each corresponding schedule provided in the input.

### **optimise\_tcp\_logistic\_reox.m**

INFO: Implementation of a Simulated Annealing optimization algorithm to find the best-fitting parameters for a logistic Tumor Control Probability (TCP) model using a maximum likelihood method.

#### INPUT:

- *A*: cell array containing the experimental data.

- *par0*: starting point for the model parameters.
- *ind\_opt*: indices of the specific parameters that we want to optimize (some will stay fixed).
- *Constraint*: a 2x13 matrix with the lower and upper bounds for each parameter.
- *cell\_spline* & *v\_k*: pre-computed spline functions to approximate binomial probabilities (in the case of large patient cohorts).
- *runs*: the number of cooling steps and the number of iterations per temperature step ([1000, 1000] typically).
- *T0* & *dT*: initial temperature and the cooling rate

OUTPUT:

- *par\_best*: best-fitting parameters.
- *cost\_best*: minimum cost of the objective function.
- *EQD2\_best*: EQD2 values for each schedule calculated using the best-fitting parameters.

## **MATLAB WORKSPACES**

**best\_fits.mat**

INFO: workspace containing the results of the best fits for LR and IR

Variables:

- **A\_IR**: experimental data for Intermediate Risk patients. Each of the 6 columns contains: dose per fraction; number of fractions; overall treatment time (days); number of patients; vector with the treatment delivery times of each fraction (hors)
- **A\_LR**: as above Low Risk patients
- **cell\_spline\_IR** & **V\_K\_IR**: pre-computed spline functions to approximate binomial probabilities for large\_patients cohorts in A\_IR
- **cell\_spline\_LR** & **V\_K\_LR**: pre-computed spline functions to approximate binomial probabilities for large\_patients cohorts in A\_LR
- **constraint\_IR\_Zharinov**: matrix with the lower and upper bounds for each parameter for IR dataset
- **constraint\_LR\_Zharinov**: matrix with the lower and upper bounds for each parameter for LR dataset
- **cost\_IR\_optimo**: minimum cost achieved for IR dataset
- **cost\_LR\_optimo**: minimum cost achieved for LR dataset
- **EQD2\_IR\_optimo**: EQD2 values for each schedule calculated using the best-fitting parameters for IR.
- **EQD2\_LR\_optimo**: EQD2 values for each schedule calculated using the best-fitting parameters for LR.
- **indice\_optimizar**: indices of the specific parameters that we want to optimize (some will stay fixed). In our case [1, 2, 7, 9, 10, 12] which corresponds to [D50, gamma50, km, alpha/beta, OER\_I, f\_pro]
- **par\_IR\_optimo**: best-fitting parameters for LR.
- **par\_LR\_optimo**: best-fitting parameters for IR.

## **ic.mat**

INFO: workspace containing the results of the calculation of confidence intervals using the profile likelihood methodology

Variables:

- **coste\_LR/IR\_parameter:** vector with the minimum costs found for the parameter values found in `valor_LR/IR_parameter`.
- **valor\_LR/IR\_parameter:** vector with the fixed values of that parameter used to obtain the confidence intervals
- **ic\_LR/IR\_parameter:** vectors with the confidence interval results for each parameter both for LR and IR datasets -> [lower limit of 95% confidence interval, optimal value, upper limit of 95% confidence interval]. Obtained through interpolation of the values reported in the above variables.

## **kcross.mat**

INFO: workspace containing the results of the k-cross validation

Variables:

- **kcross\_results\_IR/kcross\_results\_LR:** matlab structure containing the results for the 50 kcross validations for IR and LR. Fields saved for each validation are:
  - `idx_train`: index of IR experimental points used for training
  - `params`: optimal parameters found
  - `coste_training`: minimum cost value obtained for the training subdataset
  - `p_value_training`: p-value obtained from the  $\chi^2$  test for the training subdataset
  - `coste_validacion`: cost value obtained evaluating the optimal parameters (*params*) in the validation subdataset
  - `p_value_validacion`: p-value obtained from the  $\chi^2$  test for the validation subdataset