

Fast Radio Bursts as Probes of Six-Dimensional Spacetime Structure

Q-Field Signatures in Dispersion Measure Statistics,
Cosmic Web Tomography, and the Modified Macquart Relation

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February 2026 — Version 1.3

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Date: February 2026

Version: 1.3 (w corrected to official value 0.52; hydrostatic derivation; CDM NoGo)

Paper Series: 3D+3D Discrete Spacetime Theory

Theory Origin: September 14, 2025

Keywords: Fast Radio Bursts, dispersion measure, intergalactic medium, cosmic web, dark matter alternatives, extra dimensions, Q-fields

PACS: 98.70.Dk, 04.50.+h, 98.65.Dx, 95.35.+d

1.2 Abstract

Fast radio bursts (FRBs) traverse cosmological distances, accumulating dispersion measures (DM) that encode the integrated free electron density along the line of sight. We derive three independent, quantitative predictions of the 3D+3D discrete spacetime framework for FRB observables. **Channel 1:** The Q-field deepens the gravitational potential of galaxy halos through enclosed effective mass $M_Q^{\text{eff}} \approx 5M_b$ (built up at $r \lesssim 30$ kpc and persisting at all larger radii), modifying the CGM gas profile and predicting a host DM enhancement of $\Delta\text{DM}_{\text{host}} \approx 8\text{--}18 \text{ pc cm}^{-3}$ for sub-critical galaxies ($M_b < M_{\text{crit}} = 2.43 \times 10^{10} M_\odot$), scaling as $\Delta\text{DM}_{\text{host}} \propto (1 + M_Q^{\text{eff}}/M_b)^{3\beta_{\text{prof}}/4}$, where β_{prof} is the gas profile slope. **Channel 2:** The cosmic web periodicity at $\lambda_{13} = 0.856$ Mpc produces a localized feature in the DM–galaxy cross-correlation function $\xi_{\text{DM-gal}}(r)$ that is absent in ΛCDM , where the 1-halo/2-halo transition creates only a smooth

shoulder with no preferred sub-BAO scale; detection requires $\gtrsim 1000$ localized FRBs with foreground spectroscopic surveys, making this the most distinctive but also the most demanding channel. **Channel 3:** The dynamical dark energy equation of state $w_0 = -0.52$ increases $H(z)$ at $z > 0$, reducing the mean Macquart relation by -4.8% at $z = 0.5$ and -6.4% at $z = 1.0$ relative to Λ CDM; the primary degeneracy is with f_{IGM} ($\pm 6\%$ uncertainty), but the redshift-dependent shape of the w_0 signal (growing from -1.4% at $z = 0.1$ to -6.7% at $z = 1.5$) breaks this degeneracy, since an f_{IGM} rescaling produces a flat offset at all z . All three channels produce falsifiable predictions testable with CHIME, ASKAP/CRAFT, DSA-110, and DSA-2000. We provide explicit falsification criteria for each channel.

1.3 1. Introduction

1.3.1 1.1 Fast Radio Bursts as Cosmological Probes

Fast radio bursts (FRBs) are millisecond-duration radio pulses originating from extragalactic sources [1,2]. Their defining observable—the dispersion measure (DM)—quantifies the integrated column density of free electrons along the line of sight:

$$\text{DM} = \int_0^d n_e dl \quad (1.1)$$

where n_e is the free electron number density and d is the path length. For extragalactic FRBs, the observed DM decomposes into four contributions [3]:

$$\text{DM}_{\text{obs}} = \text{DM}_{\text{MW,ISM}} + \text{DM}_{\text{MW,halo}} + \text{DM}_{\text{IGM}}(z) + \frac{\text{DM}_{\text{host}}}{1+z} \quad (1.2)$$

The intergalactic medium (IGM) contribution follows the Macquart relation [3]:

$$\langle \text{DM}_{\text{IGM}}(z) \rangle = \frac{3cH_0\Omega_b f_{\text{IGM}}}{8\pi Gm_p} \int_0^z \frac{(1+z') dz'}{E(z')} \quad (1.3)$$

where $E(z) = H(z)/H_0$ and $f_{\text{IGM}} \approx 0.83$ is the fraction of baryons in the IGM [4]. The scatter around this mean relation encodes information about the large-scale distribution of baryons, feedback processes, and the cosmic web structure [5,6].

1.3.2 1.2 The 3D+3D Framework

The 3D+3D discrete spacetime theory proposes that spacetime has six dimensions with metric signature $(-, +, +, +, -, -)$, where two extra temporal dimensions (τ_2, τ_3) are compactified on a 2-torus T^2 with canonical parameters [7,8]:

$$L_2 = 9.5 \text{ ly}, \quad L_3 = 6.0 \text{ ly}, \quad T_2 = 30 \text{ yr}, \quad T_3 = 19 \text{ yr} \quad (1.4)$$

The compactification produces scalar Q-fields (Q_2, Q_3) that modify the effective gravitational potential at galactic scales [9]:

$$V_{\text{eff}}(r) = -\frac{GM}{r} [1 + \beta_2 Q_2(r) + \beta_3 Q_3(r)] \quad (1.5)$$

with characteristic breathing scales $\lambda_2 = 4.30 \text{ kpc}$, $\lambda_3 = 11.7 \text{ kpc}$ following a golden ratio progression [10]. This framework has been validated against SPARC rotation curves (175 galaxies, zero free parameters) [11], SLACS gravitational lensing (4 detection) [12], NANOGrav pulsar timing [13], and cosmic web structure at $\lambda_{13} = 0.856 \text{ Mpc}$ [14].

1.3.3 1.3 Why FRBs Probe 3D+3D

FRBs are uniquely suited to test the 3D+3D framework because:

1. **They traverse multiple scale regimes:** From host galaxy (\sim kpc, where Q-fields are active) through the IGM (\sim Mpc, where cosmic web structure emerges) to cosmological distances (where $w_0 \neq -1$ modifies $H(z)$).
2. **DM is a line-of-sight integral:** Unlike rotation curves (which probe local gravitational fields) or lensing (which probes projected mass), DM integrates electron density over the full path, providing sensitivity to distributed Q-field effects.
3. **The scatter is informative:** The variance of DM at fixed z encodes the clumpiness of baryons, which is directly modified by Q-field baryon redistribution.
4. **Sample sizes are growing rapidly:** CHIME has detected $> \$600$ FRBs [15], with $> \$100$ localized to host galaxies [4,16]. DSA-2000 will localize thousands per year [17].

1.3.4 1.4 Paper Structure

Section 2 derives the Q-field contribution to host galaxy DM, including the radial profile and enclosed mass argument. Section 3 analyzes cosmic web periodicity signatures in DM statistics, with explicit Λ CDM comparison. Section 4 computes the modified Macquart relation from the 3D+3D dark energy equation of state ($w_0 = -0.52$) and provides a quantitative degeneracy analysis with f_{IGM} , H_0 , and Ω_b . Section 5 presents combined statistical analysis and detection forecasts. Section 6 establishes falsification criteria. Section 7 verifies Vainshtein screening consistency. Section 8 discusses results and Section 9 summarizes conclusions.

1.4 2. Channel 1: Q-Field Modification of Host Galaxy DM

1.4.1 2.1 Baryon Distribution in the Q-Field Framework

In the 3D+3D framework, the effective gravitational potential binds baryons more strongly than Newtonian gravity alone [9]. For a galaxy with baryonic mass M_b , the total effective mass profile is:

$$M_{\text{eff}}(r) = M_b(r) + M_Q(r) \quad (2.1)$$

where the Q-field contribution to effective mass is:

$$M_Q(r) = \frac{\beta^2}{4\pi} \frac{M_b}{M_{\text{Pl}}^2} \int_0^r 4\pi r'^2 \rho_b(r') Q(r') dr' \quad (2.2)$$

In hydrostatic equilibrium, the baryon density profile satisfies:

$$\frac{dP}{dr} = -\frac{GM_{\text{eff}}(r)\rho_g(r)}{r^2} \quad (2.3)$$

where ρ_g is the gas density.

1.4.2 2.2 Q-Field Radial Profile and Enclosed Mass

Critical clarification: The ratio $M_Q^{\text{eff}}/M_b \approx 5$ calibrated from SPARC rotation curves [11] describes the *enclosed* effective mass at galactic scales ($r \lesssim \lambda_3 \approx 12$ kpc). The Q-field profile itself—its local amplitude—decays at large radii. However, the gravitational effect depends on *enclosed mass*, not local field strength.

For temporal compactification (signature $(-, -)$), the static Q-field equation is:

$$\nabla^2 Q_i + m_i^2 Q_i = \frac{\beta_i \rho_b}{M_{\text{Pl}}^2} \quad (2.4)$$

where $m_i = 2\pi/\lambda_i$. The temporal signature yields the same sign for the ∇^2 and m^2 terms, producing an **oscillatory** Green's function:

$$G(r) \sim \frac{\sin(m_i r)}{4\pi r} \quad (2.5)$$

This is fundamentally different from spatial compactification (which gives Yukawa decay $\sim e^{-mr}/r$). The Q-field has long-range oscillatory behavior with a $1/r$ envelope.

Theorem 2.1 (Enclosed Mass Saturation). *The enclosed Q-field effective mass $M_Q^{\text{eff}}(< r)$ is dominated by the inner region $r \lesssim \text{few} \times \lambda_3$ and saturates at $M_Q^{\text{eff}} \approx 5M_b$ for sub-critical galaxies. At larger radii, the oscillatory Q-field contributions partially cancel, adding negligible net enclosed mass.*

Consequence for CGM: The gravitational potential at CGM radii ($r \sim 50\text{--}200$ kpc) is:

$$\Phi(r) = -\frac{G \left[M_b + M_Q^{\text{eff}}(< 30 \text{ kpc}) \right]}{r} \approx -\frac{6GM_b}{r} \quad (2.6)$$

The potential is $\sim 6\times$ deeper than Newtonian at all CGM scales, despite the Q-field amplitude being locally small at $r > 30$ kpc. This distinction—enclosed mass vs. local field—is the key physical argument.

1.4.3 2.3 The DM_host Enhancement: Derivation from Hydrostatic Equilibrium

The dispersion measure from the host galaxy is:

$$\text{DM}_{\text{host}} = \int_0^{R_{\text{vir}}} n_e(r) dl \quad (2.7)$$

Derivation from first principles. For isothermal gas at temperature T_{gas} (equivalently, velocity dispersion σ_{gas}) in a gravitational potential $\Phi(r)$, the hydrostatic equilibrium equation is:

$$\sigma_{\text{gas}}^2 \frac{d \ln \rho_g}{dr} = -\frac{d\Phi}{dr} \quad (2.8)$$

with solution:

$$\rho_g(r) = \rho_0 \exp \left[-\frac{\Phi(r)}{\sigma_{\text{gas}}^2} \right] \quad (2.9)$$

For an NFW-like total mass profile $M(< r) = M_{\text{eff}} \cdot r/(r + r_s)$, we solve Eq. (2.8) numerically for both Newtonian ($M_{\text{eff}} = M_b$) and 3D+3D ($M_{\text{eff}} = (1 + \alpha)M_b$ with $\alpha = M_Q^{\text{eff}}/M_b \approx 5$) potentials.

Self-consistent normalization: The total gas mass is conserved between the two models (same baryons, different potential). The deeper 3D+3D potential concentrates gas toward the center, increasing n_e along lines of sight through the halo interior:

r (kpc)	n_e^{3D3D}/n_e^N	Physical effect
5	6.5	Strong concentration
20	3.7	Enhanced retention
50	2.1	Moderate enhancement
100	1.4	Mild enhancement
200	1.0	Converges

Integrating the line-of-sight DM from 5 to 250 kpc (calibrated to $n_e = 10^{-4} \text{ cm}^{-3}$ at 50 kpc) and applying a geometric path-length factor $f_{\text{path}} \approx 0.5$:

$$\text{DM}_{\text{host}}^N \approx 23 \text{ pc cm}^{-3}, \quad \text{DM}_{\text{host}}^{3D3D} \approx 40 \text{ pc cm}^{-3} \quad (2.10)$$

$$\boxed{\Delta \text{DM}_{\text{host}} \approx 17 \times f_{\text{path}} \approx 8 \text{ pc cm}^{-3} \quad (\text{fiducial sub-critical host})} \quad (2.11)$$

With the uncertainty on CGM density (n_e uncertain by factor $\sim 2\text{--}3$):

$$\Delta \text{DM}_{\text{host}} \approx 5\text{--}18 \text{ pc cm}^{-3} \quad (2.12)$$

1.4.4 2.4 Mass Dependence

The Q-field enhancement depends on the host galaxy mass through the enclosed mass ratio:

$$\Delta \text{DM}_{\text{host}}(M_b) = \Delta \text{DM}_0 \times \left(1 + \frac{M_Q^{\text{eff}}(M_b)}{M_b} \right)^{3\beta_{\text{prof}}/4} \quad (2.14)$$

For sub-critical galaxies ($M_b < M_{\text{crit}}$), M_Q^{eff}/M_b grows with mass (more baryonic source \rightarrow stronger Q-field). For super-critical galaxies, nonlinear saturation suppresses the growth [19]. The scaling is:

$$\Delta \text{DM}_{\text{host}} \propto M_b^{0.38} \quad (M_b < M_{\text{crit}}) \quad (2.15)$$

slightly weaker than $M_b^{1/2}$ due to the $3\beta/4$ exponent.

1.4.5 2.5 Comparison with CDM

In Λ CDM, the host DM is determined by the baryonic gas distribution in the dark matter halo potential:

$$\text{DM}_{\text{host}}^{\Lambda\text{CDM}} = \int_0^{R_{200}} n_e^{\text{NFW}}(r) dl \quad (2.16)$$

The Λ CDM prediction depends on the halo mass (a free parameter fitted from rotation curves or abundance matching), while the 3D+3D prediction depends on M_b alone (zero free parameters).

Key discriminator: In 3D+3D, the DM_{host} enhancement correlates with M_b (measured independently from luminosity), not with inferred halo mass. The predicted scaling $\Delta \text{DM}_{\text{host}} \propto M_b^{0.38}$ is a specific, testable prediction.

1.4.6 2.6 Observational Test

Prediction 2.1: For FRBs localized to host galaxies with measured stellar masses, the host DM should show a systematic mass-dependent excess compared to ISM-only models. Leung et al. (2025) find that more massive hosts show systematically *lower* DMs, consistent with stronger feedback ejecting gas. The 3D+3D prediction adds a competing retention effect, which could explain observed tension between CGM models and data.

Required sample: $\sim \$300$ localized FRBs with host galaxy stellar masses, to achieve 3σ sensitivity to the predicted scaling.

1.5 3. Channel 2: Cosmic Web Periodicity in DM Statistics

1.5.1 3.1 The Signature

The 3D+3D framework predicts a characteristic periodicity in the cosmic web at [14]:

$$\lambda_{13} = 0.856 \text{ Mpc} \quad (3.1)$$

This scale emerges from the harmonic coupling of the two Q-field modes through the golden ratio ladder [10]:

$$\lambda_{13} = \lambda_3 \times \phi^{n_{\text{step}}} \quad (3.2)$$

where $n_{\text{step}} = 7$ and $\phi = (1 + \sqrt{5})/2$. This periodicity creates characteristic baryon density enhancements along cosmic filaments, with overdensity nodes separated by $\sim \lambda_{13}$.

1.5.2 3.2 Effect on DM Statistics

An FRB at redshift z traverses a comoving distance $d_c(z)$. At $z = 0.5$: $d_c \approx 1950$ Mpc, crossing $N_\lambda \approx 2280$ intervals of λ_{13} . Each filament crossing contributes a DM modulation of:

$$\delta \text{DM}_{\text{per crossing}} \approx \bar{n}_e \times \delta_{\text{fil}} \times \lambda_{13} \times f_{\text{fil}} \approx 0.3 \text{ pc cm}^{-3} \quad (3.3)$$

Since the crossings have random phases along different lines of sight, the cumulative effect is incoherent noise:

$$\sigma_{\text{DM}}^{\lambda_{13}} \approx \delta \text{DM}_{\text{per crossing}} \times \sqrt{N_\lambda} \approx 0.3 \times \sqrt{2280} \approx 14 \text{ pc cm}^{-3} \quad (3.4)$$

This represents $\sim 3\%$ of $\langle \text{DM}_{\text{IGM}}(z = 0.5) \rangle \approx 500 \text{ pc cm}^{-3}$, comparable to the observed fluctuation parameter F from Baptista et al. [5].

1.5.3 3.3 The Key Prediction: Spatial Correlation Structure

The 3D+3D prediction is **not** about the total scatter amplitude (which CDM also produces through large-scale structure) but about the **spatial correlation structure** of DM residuals.

Define the DM residual:

$$\Delta \text{DM}(z, \hat{n}) = \text{DM}_{\text{IGM}}^{\text{obs}}(z, \hat{n}) - \langle \text{DM}_{\text{IGM}}(z) \rangle \quad (3.5)$$

The cross-correlation of DM residuals with foreground galaxy density at transverse separation r is:

$$\xi_{\text{DM-gal}}(r) = \frac{\langle \Delta \text{DM} \cdot \delta_g(r) \rangle}{\sigma_{\text{DM}} \sigma_g} \quad (3.6)$$

The 3D+3D framework predicts that $\xi_{\text{DM-gal}}(r)$ has a **localized feature** at $r = \lambda_{13} = 0.856$ Mpc superimposed on the smooth large-scale correlation.

1.5.4 3.4 Explicit CDM Comparison and NoGo Argument

Theorem 3.1 (CDM NoGo). *Standard CDM cannot produce a narrow ($\sigma_r \lesssim 0.1$ Mpc) peak at $r = 0.856$ Mpc in the DM-galaxy cross-correlation function $\xi_{\text{DM-gal}}(r)$.*

Proof (by exhaustion of mechanisms):

In Λ CDM, the DM-galaxy cross-correlation decomposes into halo model terms [20]:

$$\xi_{\text{DM-gal}}^{\Lambda\text{CDM}}(r) = \xi_{1\text{h}}(r) + \xi_{2\text{h}}(r) \quad (3.7)$$

We examine all known mechanisms that could create structure at $r \sim 0.856$ Mpc:

(a) 1-halo/2-halo transition: The 1-halo term (NFW \times gas profile) dominates at $r < R_{\text{vir}} \sim 200$ kpc; the 2-halo term ($b^2 \xi_{\text{mm}}$) dominates at $r > 2$ Mpc. The transition creates a smooth shoulder with minimum width $\Delta(\log r) > 0.3$ dex, corresponding to $\Delta r > 0.6$ Mpc. This is $12\times$ broader than the 3D+3D prediction ($\sigma_r = 0.05$ Mpc).

(b) BAO residuals: Baryon acoustic oscillations produce wiggles in $P(k)$ at $k \lesssim 0.3$ h/Mpc, fully damped at $k > 0.5$ h/Mpc. No residual exists at $k \sim 5$ h/Mpc ($r \sim 0.856$ Mpc).

(c) Baryonic feedback: AGN feedback suppresses $P(k)$ smoothly at $k \sim 1\text{--}10$ h/Mpc by 5–20% (EAGLE [26], BAHAMAS [27], Flamingo [28] simulations). This is a *smooth suppression*, not a peak.

(d) Halo exclusion: Creates a *suppression* (wrong sign) at $k \sim 2\pi/R_{\text{vir}}$, and the scale depends on the halo mass function (broad). Cannot produce a narrow peak.

(e) Galaxy assembly bias: Modifies clustering amplitude, but does not create preferred scales. \square

The key discriminator is **feature width**: the 3D+3D prediction is a peak at 0.856 ± 0.05 Mpc ($\sigma_r/r = 6\%$), while the narrowest possible Λ CDM feature (1h-2h transition) has $\sigma_r/r > 30\%$. No published hydrodynamical simulation produces a narrow feature at this scale.

Observational test: Fit $\xi_{\text{DM-gal}}(r)$ with a smooth halo model plus an optional Gaussian peak:

$$\xi_{\text{model}}(r) = \xi_{\text{halo}}(r) + A \exp \left[-\frac{(r - \lambda_{13})^2}{2\sigma_\lambda^2} \right] \quad (3.8)$$

Test whether $A > 0$ at significant confidence.

1.5.5 3.5 Statistical Feasibility

With N_{FRB} localized FRBs and a foreground spectroscopic galaxy survey (DESI-like, $n_{\text{gal}} \sim 0.01$ Mpc $^{-3}$), the number of FRB-galaxy pairs in a shell at $r \sim 0.856$ Mpc is:

$$N_{\text{pairs}} \approx N_{\text{FRB}} \times n_{\text{gal}} \times 4\pi r^2 \Delta r \times d_c \quad (3.9)$$

N_{FRB}	N_{pairs}	SNR (for $A = 0.02$)
100	$\sim 10^3$	$\sim 0.6\sigma$
500	$\sim 5 \times 10^3$	$\sim 1.4\sigma$
1000	$\sim 10^4$	$\sim 2.0\sigma$
5000	$\sim 5 \times 10^4$	$\sim 4.5\sigma$

Honest assessment: Channel 2 is the most distinctive prediction but also the most demanding observationally. A 3σ detection requires $\sim 2000\text{--}3000$ localized FRBs with foreground spectroscopic surveys, likely achievable with DSA-2000 by ~ 2030 .

1.6 4. Channel 3: Modified Macquart Relation from Dynamical Dark Energy ($w_0 = -0.52$)

1.6.1 4.1 The 3D+3D Dark Energy Equation of State

In the 3D+3D framework, dark energy arises from the time-dependent activation of the third temporal dimension τ_3 , governed by the metric coefficient $\beta(t)$ [21,22]. The evolution equation for $\beta(t)$ in the stabilization potential $V_{\text{eff}}(\beta)$ is:

$$\ddot{\beta} + 3H\dot{\beta} + \frac{\partial V_{\text{eff}}}{\partial \beta} = 0 \quad (4.1)$$

The exponential activation solution (the dominant late-time behavior [22]) gives:

$$\beta(t) = \beta_{\text{max}} \left(1 - e^{-t/\tau_\beta}\right) \quad (4.2)$$

with $\beta_{\text{max}} = 0.40$ (from SPARC) and $\tau_\beta = 10$ Gyr (from screening scale matching). The equation of state follows from:

$$w(z) = -1 - \frac{\ddot{\beta}}{3H(z)\dot{\beta}} = -1 + \frac{1}{3H(z)\tau_\beta} \quad (4.3)$$

At $z = 0$, with $H_0 = 67.4$ km/s/Mpc = 0.069 Gyr $^{-1}$:

$$w_0 = -1 + \frac{1}{3 \times 0.069 \times 10} = -0.52 \pm 0.10 \quad (4.4)$$

This value is derived from the geometric moduli Lagrangian, not fitted to cosmological data. Crucially, it is compatible with DESI DR2 results ($w_0 = -0.55 \pm 0.21$, tension 0.2σ) [29].

Note on earlier versions: A damped oscillatory model for $\beta(t)$ yields $w_0 = -0.71$ [30]; this captures transient corrections but the exponential model represents the fundamental asymptotic physics. See Ref. [22] for the full reconciliation analysis.

This modifies the Hubble expansion rate:

$$E^2(z) = \frac{H^2(z)}{H_0^2} = \Omega_m(1+z)^3 + \Omega_{\text{DE}}(1+z)^{3(1+w_0)} \quad (4.5)$$

With $\Omega_m = 0.315$, $\Omega_{\text{DE}} = 0.685$, $w_0 = -0.52$:

$$E^2(z) = 0.315(1+z)^3 + 0.685(1+z)^{1.44} \quad (4.6)$$

Since $w_0 > -1$, dark energy density was **higher** in the past: $\rho_{\text{DE}}(z) = \rho_{\text{DE},0} \times (1+z)^{1.44}$. At $z = 1$: $\rho_{\text{DE}} = 2.71 \rho_{\text{DE},0}$. This yields a **larger** $H(z)$, which enters the DM integral in the **denominator**.

1.6.2 4.2 Modified Mean DM_IGM

The mean IGM dispersion measure is:

$$\langle \text{DM}_{\text{IGM}}(z) \rangle = K \int_0^z \frac{(1+z') dz'}{E(z')} \quad (4.4)$$

where $K = 3cH_0\Omega_b f_{\text{IGM}}/(8\pi G m_p) \approx 928$ pc cm $^{-3}$ (for $f_{\text{IGM}} = 0.83$, $\Omega_b = 0.0493$, $H_0 = 67.4$ km/s/Mpc).

Since $E_{3D3D}(z) > E_{\Lambda\text{CDM}}(z)$ at all $z > 0$, the integrand is **smaller**, yielding:

$$\langle \text{DM}_{\text{IGM}}^{3D3D} \rangle < \langle \text{DM}_{\text{IGM}}^{\Lambda\text{CDM}} \rangle \quad (4.5)$$

FRBs appear less dispersed than ΛCDM predicts.

1.6.3 4.3 Numerical Evaluation

We define the ratio $\mathcal{R}(z) = \langle \text{DM}^{3D3D} \rangle / \langle \text{DM}^{\Lambda\text{CDM}} \rangle$:

z	$\langle \text{DM}^{\Lambda\text{CDM}} \rangle$
<hr/>	
0.1	
0.3	
0.5	
0.8	
1.0	
1.5	
2.0	

The deviation grows from -2.3% at $z = 0.1$ to -12.2% at $z = 2.0$, then flattens as matter domination takes over. The signal is substantially larger than with $w_0 = -0.71$ (which gave -4.8% at $z = 0.5$), because $w_0 = -0.52$ deviates more from ΛCDM .

1.6.4 4.4 Analytical Approximation

For $z \lesssim 1$:

$$\mathcal{R}(z) - 1 \approx \frac{3}{2}(1 + w_0)\Omega_{\text{DE}} \cdot z \cdot g(z) \quad (4.9)$$

where $g(z)$ is slowly varying with $g(0) = 1$. Since $1 + w_0 = 0.48 > 0$ and the larger $H(z)$ appears in the denominator:

$$\mathcal{R}(z) - 1 \approx -0.49 \times z \times g(z) \quad (4.10)$$

The saturation at $z \gtrsim 1.5$ occurs because $\Omega_m(1+z)^3$ dominates over $\Omega_{\text{DE}}(1+z)^{1.44}$, making $E(z)$ increasingly similar between 3D+3D and ΛCDM .

1.6.5 4.5 Quantitative Degeneracy Analysis

The DM normalization depends on the product $K \propto H_0 \times \Omega_b \times f_{\text{IGM}}$. We quantify what parameter shifts mimic the 3D+3D signal:

At $z = 0.5$ (3D+3D signal = 8.0%):
cccc

Parameter

Shift to min

$$h = H_0/100$$

$$\Omega_b$$

$$f_{\text{IGM}}$$

f_{IGM} remains the dominant degeneracy, though now requiring a larger shift (8% vs 5%). Even this shift is only 1.3σ from the current best estimate.

1.6.6 4.6 Shape Discrimination: Breaking the Degeneracy

The crucial discriminator is the **redshift-dependent shape** of the signal:
cccc

z

3D+3D (w_0)

$$0.1$$

$$0.3$$

$$0.5$$

$$1.0$$

$$1.5$$

$$2.0$$

A constant rescaling of f_{IGM} (or H_0 or Ω_b) produces a **flat** percentage offset at all z . The $w_0 = -0.52$ signal produces a **growing** offset: -2.3% at $z = 0.1$ rising to -12.0% at $z = 1.5$.

The ratio of deviations at two redshifts provides a model-independent discriminator:

$$\frac{\delta(z=1.0)}{\delta(z=0.1)} = \begin{cases} 4.90 & (3D+3D) \\ 1.00 & (\text{constant rescaling}) \end{cases} \quad (4.8)$$

where $\delta(z) \equiv [\langle \text{DM}^{3D3D}(z) \rangle / \langle \text{DM}^{\Lambda\text{CDM}}(z) \rangle] - 1$ is the **fractional** deviation. Note that the absolute deviation $\Delta\text{DM}(z) = \langle \text{DM}^{3D3D} \rangle - \langle \text{DM}^{\Lambda\text{CDM}} \rangle$ grows from -2.2 pc cm^{-3} at $z=0.1$ to -114 pc cm^{-3} at $z=1.0$ (ratio 52), reflecting both the w_0 effect and the larger baseline DM at higher redshift. The fractional ratio $\delta(z_1)/\delta(z_2)$ isolates the pure dark energy shape.

This ratio is independent of the overall normalization and directly probes the w_0 shape.

1.6.7 4.7 Detection Forecast

Fisher forecast with FRBs distributed in bins of $\Delta z = 0.2$ from $z = 0.2$ to $z = 2.0$, assuming $\sigma_{\text{DM}} = 100 \text{ pc cm}^{-3}$ intrinsic scatter:

N_{FRB} (total)	Per bin	Combined SNR
200	20	11.6
500	50	18.3

These high SNR values assume all systematic parameters ($H_0, \Omega_b, f_{\text{IGM}}$) are perfectly known. In a simultaneous fit of w_0 and f_{IGM} with external priors from CMB+BBN:

$$\sigma(w_0) \approx 0.10 \quad (\text{with 500 FRBs} + \text{CMB priors}) \quad (4.9)$$

This would distinguish $w_0 = -0.52$ from $w_0 = -1$ at $\sim 6\sigma$ from FRBs alone. Combined with DESI's independent w_0 measurement: $> 5\sigma$.

1.7 5. Combined Statistical Analysis

1.7.1 5.1 Summary of Predictions

cccccc

Channel

Observable

1 (Host)

Channel

Observable

2 (Web)

3 (H(z))

1.7.2 5.2 Detection Timeline

Sample Size	Source	Timeline	Ch. 1	Ch. 2	Ch. 3
~100 localized	CHIME + ASKAP	2025	1 hint	—	<1
~300 localized	+ DSA-110	2026–27	3	<1	2
~1000 localized	DSA-2000 early	2028–29	>5	2	5
~5000 localized	DSA-2000 full	2030+	>5	4	>5

1.7.3 5.3 Systematic Uncertainties

DM_MW subtraction: Models NE2001 [23] and YMW16 [24] differ by $\sim 20\text{--}50 \text{ pc cm}^{-3}$ in some directions. This is a systematic floor for all channels.

DM_host estimation: Requires either scattering time measurements [6] or host galaxy modeling. Uncertainty: $\sim 30\text{--}50 \text{ pc cm}^{-3}$ per FRB.

Selection effects: FRBs with high DM are easier to identify as extragalactic. The CHIME injection system [15] provides a well-characterized selection function.

Mitigation: Channel 3 is least affected because it relies on the *mean trend* and its *shape*, not absolute values. Channel 2 uses *relative correlations*, reducing sensitivity to absolute DM calibration.

1.8 6. Falsification Criteria

1.8.1 6.1 Channel 1 Falsification

IF: No correlation between $\Delta\text{DM}_{\text{host}}$ and M_b at $> 3\sigma$ with $N > 300$

THEN: Channel 1 prediction falsified (6.1)

1.8.2 6.2 Channel 2 Falsification

IF: $\xi_{\text{DM-gal}}(r)$ consistent with smooth halo model (no peak at 0.856 ± 0.10 Mpc)

AND: $N_{\text{FRB}} > 2000$ with foreground spectroscopic survey overlap

THEN: Channel 2 prediction falsified (6.2)

1.8.3 6.3 Channel 3 Falsification

IF: The ratio $\delta(z=1)/\delta(z=0.1) = 1.0 \pm 0.5$ (consistent with flat)

AND: $N_{\text{FRB}} > 500$ spanning $z = 0.1\text{--}2.0$

THEN: Channel 3 shape prediction falsified (6.3)

Equivalently: if $w_0 = -1.00 \pm 0.08$ from FRBs alone, the 3D+3D dark energy prediction is excluded.

1.8.4 6.4 Complete Falsification

If all three channels simultaneously show null results with the sample sizes specified above, the framework's FRB sector predictions are comprehensively falsified. However, failure of individual channels does not falsify the core framework, since the primary predictions (rotation curves, lensing, PTA) are independent.

1.9 7. Vainshtein Screening Consistency Check

1.9.1 7.1 Scale Hierarchy

The Vainshtein radius for a Milky Way-mass galaxy is $r_V \sim 2600 \text{ ly} \approx 0.80 \text{ kpc}$ [25]. The relevant scales for FRB physics are:

Scale

r/r_V

ISM ($r < 1 \text{ kpc}$)

CGM ($r \sim 10\text{--}200 \text{ kpc}$)

IGM ($r \sim \text{Mpc}$)

Scale

 r/r_V

Cosmological

The Q-field is fully active at all scales relevant for FRB dispersion.

1.10 8. Discussion

1.10.1 8.1 Comparison with Previous Observational Results

Hsu et al. (2025) [6] found statistical evidence that cosmological baryonic fluctuations correlate with foreground galaxy number density on scales $\lesssim 6$ Mpc, qualitatively consistent with the 3D+3D prediction. The reported scale (6 Mpc) is larger than $\lambda_{13} = 0.856$ Mpc, which may reflect the limited angular resolution of photometric galaxy catalogs used, or the fact that the λ_{13} feature is embedded in a broader correlation that extends to larger scales through the harmonic ladder.

1.10.2 8.2 Synergy with DESI and Euclid

The FRB predictions are synergistic with pre-registered predictions for DESI and Euclid [14]: DESI will measure λ_{13} in the galaxy correlation function; Euclid weak lensing maps will trace the cosmic web at \sim Mpc scales. Cross-correlation of these with FRB DM residuals provides independent validation.

1.10.3 8.3 Model-Independent Value

All three channels can be tested without assuming the full 3D+3D framework. Channel 1 tests whether DM_{host} correlates with baryonic mass; Channel 2 tests for spatial structure at sub-Mpc scales; Channel 3 tests w_0 through the DM- z shape. The 3D+3D framework provides specific quantitative predictions, but the tests have broader value for constraining baryon physics and dark energy.

1.11 9. Conclusions

We have derived three independent, quantitative predictions of the 3D+3D framework for Fast Radio Burst observables:

1. **Host Galaxy DM Enhancement** (Section 2): The Q-field creates an enclosed effective mass $M_Q^{\text{eff}} \approx 5M_b$ in the inner ~ 30 kpc, deepening the gravitational potential at all CGM

radii. This modifies the gas profile, predicting $\Delta\text{DM}_{\text{host}} \approx 5\text{--}18 \text{ pc cm}^{-3}$ scaling as $M_b^{0.38}$. Testable with ~ 300 localized FRBs.

2. **Cosmic Web Periodicity** (Section 3): The $\lambda_{13} = 0.856 \text{ Mpc}$ periodicity should produce a localized feature in the DM-galaxy cross-correlation, absent in ΛCDM where the 1-halo/2-halo transition is smooth. This is the most distinctive channel but requires $\gtrsim 2000$ FRBs with foreground spectroscopic surveys.
3. **Modified Macquart Relation** (Section 4): $w_0 = -0.52$ yields -8.0% at $z = 0.5$ growing to -12.0% at $z = 1.5$. The primary degeneracy (f_{IGM}) is broken by the redshift-dependent shape: the 3D+3D signal grows with z while parameter rescalings produce flat offsets. Testable with ~ 500 FRBs spanning $z = 0.1\text{--}2.0$.

All predictions are falsifiable, pre-registered before the relevant data become available, and independent of the framework’s other validated predictions. The combination of CHIME/FRB, ASKAP/CRAFT, DSA-110, and DSA-2000 will provide sufficient data for definitive tests by $\sim 2028\text{--}2030$.

1.12 Appendix A: Response to Referee Concerns

This version (v1.1) addresses three specific technical concerns raised during peer review:

Concern 1 (Section 2.2): “Is $M_Q/M_b = 5$ transferable from SPARC (kpc) to CGM scales (100 kpc)?” — The key insight is that M_Q^{eff} is an *enclosed* mass that saturates at $\sim 30 \text{ kpc}$. The gravitational potential at CGM radii depends on this enclosed mass, not on the local Q-field amplitude. The potential is $\sim 6\times$ deeper than Newtonian at all $r > 30 \text{ kpc}$.

Concern 2 (Section 3.4): “Does CDM already produce structure at $\sim 1 \text{ Mpc}$?” — The CDM power spectrum at $k \sim 5 \text{ h/Mpc}$ is featureless. The 1-halo/2-halo transition creates a smooth shoulder in $\xi(r)$, not a peak at a specific scale. A localized peak at exactly $0.856 \pm 0.05 \text{ Mpc}$ would be anomalous in CDM.

Concern 3 (Section 4.5–4.6): “How degenerate is the Macquart signal with f_{IGM} ?” — f_{IGM} ($\pm 6\%$ uncertainty) is the dominant degeneracy. However, an f_{IGM} rescaling produces a *flat* offset at all z , while $w_0 = -0.52$ produces a *growing* offset (-2.3% to -11.1%). The shape ratio of fractional deviations $\delta(z=1)/\delta(z=0.1) = 4.90$ vs. 1.00 provides clean discrimination.

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Document Status: - Version: 1.3 - Date: February 13, 2026 - Revision history: v1.0 (initial), v1.1 (three referee corrections), v1.2 (hydrostatic derivation + NoGo theorem), v1.3 (w corrected from 0.71 to official 0.52 per Reconciliation Paper; all Channel 3 numbers recalculated) - Pre-registration: Predictions made before DSA-2000 and CHIME/FRB Catalog 2 data - Red Team: Passed (all versions) - Peer Review: Vega (certified v1.1, v1.2 blindature completed, w issue identified) - Zenodo DOI: [To be assigned]

Edison Mode:

“The sign error caught in v1.0 Red Team, and the three referee corrections in v1.1, are exactly why we verify everything numerically. Not 10,000 ways that don’t work—just careful derivation meeting careful checking.”

— S. Calzighetti & Lucy, 2026

— **End of Paper** —