

# Emergent Gravity from Threshold Field Architecture: A Constructive Model via Information Geometry

Narakorn Juntaramalee

Independent Researcher, Nonthaburi, Thailand

moddier@gmail.com

April 2026

## Abstract

We present a constructive model in which spacetime geometry and matter content emerge from a single scalar field  $\Theta(\xi, Z)$ , the threshold function of a probability distribution  $P(\xi|Z)$ . The metric  $g_{\mu\nu}$  arises as the expectation of the Hessian of  $\Theta$  over  $P$ , and the stress-energy tensor  $T_{\mu\nu}$  arises from the gradient structure of  $\Theta$ . Numerical evidence shows that the Einstein tensor  $G_{\mu\nu}$  computed from this emergent metric satisfies  $G_{\mu\nu} \approx \kappa T_{\mu\nu}$  with correlation  $\approx 0.80$  and  $\kappa \approx O(1)$ , stable across the physical parameter range. The Bianchi identity  $\nabla^\mu G_{\mu\nu} = 0$  holds exactly in spacetime coordinates. The threshold form is consistent with a constrained maximum entropy principle under Lorentzian signature requirement. This constitutes a coherent, testable prototype of emergent gravitational dynamics — not a derivation of General Relativity, but a demonstration that Einstein-like structure can arise from information geometry without GR being assumed.

## Contents

<b>1</b>	<b>Introduction</b>	<b>3</b>
<b>2</b>	<b>Postulates</b>	<b>3</b>
<b>3</b>	<b>Construction</b>	<b>4</b>
3.1	Threshold Function . . . . .	4
3.2	Emergent Metric . . . . .	4
3.3	Emergent Matter . . . . .	4
3.4	Information Geometry . . . . .	5
3.5	Emergent Spacetime . . . . .	5
<b>4</b>	<b>Key Result: Emergent Einstein Equation</b>	<b>5</b>
<b>5</b>	<b>Why Projector Form</b>	<b>6</b>

6	Conservation Law	7
7	Regime of Validity	7
8	Physical Interpretation	8
9	Limitations	10
10	Predictions and Differences from GR	11
11	Conclusion	11
A	Key Numerical Results	12
B	Simulation Code	13

# 1 Introduction

General Relativity treats spacetime geometry as a fundamental field governed by the Einstein equation  $G_{\mu\nu} = 8\pi G T_{\mu\nu}$ . Matter and geometry are separate inputs. The question of whether this coupling can be derived from a deeper principle remains open [Jacobson, 1995, Verlinde, 2011, Padmanabhan, 2010].

We propose that both geometry and matter emerge from a single object: a probability distribution  $P(\xi|Z)$  over a fluctuation space  $\xi$ , parameterized by a state vector  $Z = (T, M, I, A)$  encoding actuality, memory, inertia, and accessibility.

The central object is the threshold function  $\Theta(\xi, Z)$ , which determines  $P$  via  $P = e^{-\Theta/\sigma}/\mathcal{Z}$ . We show that:

1. The metric  $g_{\mu\nu}$  emerges as the expectation of the Hessian of  $\Theta$ .
2. The stress-energy  $T_{\mu\nu}$  emerges from the gradient structure of  $\Theta$ .
3. Numerical evidence shows  $G_{\mu\nu}[g_{\mu\nu}] \approx \kappa T_{\mu\nu}$ .
4. Conservation ( $\nabla^\mu G_{\mu\nu} = 0$ ) holds exactly in spacetime coordinates.
5. The threshold form is consistent with a constrained maximum entropy principle.

This framework, called the Threshold Field Architecture (TFA), provides a unified construction in which Einstein-like dynamics emerge from information geometry [Amari and Nagaoka, 2000, Frieden, 1998].

**The central conceptual contribution** is *co-emergence*: geometry and matter are not separate inputs (as in GR) but are two distinct projections of the same object  $\Theta$ . Specifically:

- The *second derivative* of  $\Theta$  (Hessian) gives the metric  $g_{\mu\nu}$  — the geometry of spacetime.
- The *first derivative* of  $\Theta$  (gradient) gives the stress-energy  $T_{\mu\nu}$  — the matter content.

In GR, matter tells geometry how to curve. In TFA, both emerge simultaneously from a single information kernel. This is a structural reversal: not matter  $\rightarrow$  curvature, but information  $\rightarrow$  matter + curvature together.

We emphasize that this is a *structural* result, not a claim about the physical matter content of the universe.  $T_{\mu\nu}$  has the form of a perfect fluid; it does not yet map to specific particle species. The contribution is the mechanism, not the complete theory.

This paper builds on the companion paper [Juntaramalee, 2026], which established the Layer 2 geometry (Lorentzian signature from threshold asymmetry) and the P3 ensemble law for GRB delays. Here we focus on the emergent gravity construction.

## 2 Postulates

**P1. Probability structure.** There exists a distribution  $P(\xi|Z)$  over fluctuation space  $\xi \in \mathbb{R}^4$ , parameterized by state  $Z = (T, M, I, A)$ .

**P2. Generator function.**  $P$  is determined by a scalar threshold field:

$$P(\xi|Z) = \frac{1}{\mathcal{Z}} \exp\left(-\frac{\Theta(\xi, Z)}{\sigma}\right) \quad (1)$$

where  $\sigma$  is a scale parameter and  $\mathcal{Z}$  is the partition function.

**P3. Constrained maximum entropy.** The threshold form is selected by:

$$\Theta = \operatorname{argmax}_P S[P] \quad \text{subject to: } \langle \partial_{\mu\nu}^2 \Theta \rangle_P = g_{\mu\nu}, \quad \text{Lorentzian signature} \quad (2)$$

where  $S[P] = -\int P \log P d\xi$  is the Shannon entropy. This is a consistency argument; a formal uniqueness proof is future work.

**P4. Metric definition.**

$$g_{\mu\nu}(Z) = \left\langle \frac{\partial^2 \Theta}{\partial \xi^\mu \partial \xi^\nu} \right\rangle_P \quad (3)$$

**P5. Matter definition.**

$$T_{\mu\nu}(Z) = \left\langle \frac{\partial \Theta}{\partial \xi^\mu} \frac{\partial \Theta}{\partial \xi^\nu} \right\rangle_P \quad (4)$$

## 3 Construction

### 3.1 Threshold Function

The threshold function takes the form:

$$\Theta(\xi, Z) = \Theta_0 - 0.1A + \alpha_M M \xi_t - \beta_I(I) I \xi_t^2 + \gamma |\xi_\perp|^2 + \varepsilon M |\xi_\perp|^4 \quad (5)$$

where  $|\xi_\perp|^2 = \xi_x^2 + \xi_y^2 + \xi_z^2$ ,  $\beta_I(I) = 0.5/(I + I_0)$  with  $I_0 = 0.3$  (regularization), and  $\varepsilon = 0.05$  (perturbative quartic coupling).

**Note on parameters:**  $\alpha_M$ ,  $\gamma$ ,  $\varepsilon$ ,  $I_0$  are effective parameters inserted by hand. They are not derived from first principles in this work. Deriving these from a deeper principle is future work.

The quartic term  $\varepsilon M |\xi_\perp|^4$  is the *projector form* — it acts only on spatial directions, preserving the temporal eigenvalue and hence the Lorentzian signature.

### 3.2 Emergent Metric

The effective metric is:

$$g_{\mu\nu}^{\text{eff}}(Z) = \langle H_{\mu\nu}[\Theta] \rangle_P = \int P(\xi|Z) \frac{\partial^2 \Theta}{\partial \xi^\mu \partial \xi^\nu} d\xi \quad (6)$$

**Result:**  $g_{\mu\nu}^{\text{eff}}$  has Lorentzian signature  $(-, +, +, +)$  for all tested  $Z$  with  $I > I_0$ . The temporal eigenvalue is  $-0.18$  (negative, stable). The spatial eigenvalues are  $\approx 1.87$  (positive, growing with  $M$ ). See Figure 1.

### 3.3 Emergent Matter

**Analytic result:** By symmetry of  $P$  under  $\xi_\perp \rightarrow -\xi_\perp$  and spatial rotations, cross terms in  $T_{\mu\nu}$  vanish identically. The spatial fluctuations are isotropic, giving:

$$T_{\mu\nu} = A g_{\mu\nu} + B u_\mu u_\nu \quad (\text{perfect fluid form, exact}) \quad (7)$$

where  $u_\mu$  is the timelike unit vector from the negative eigenvector of the Hessian.

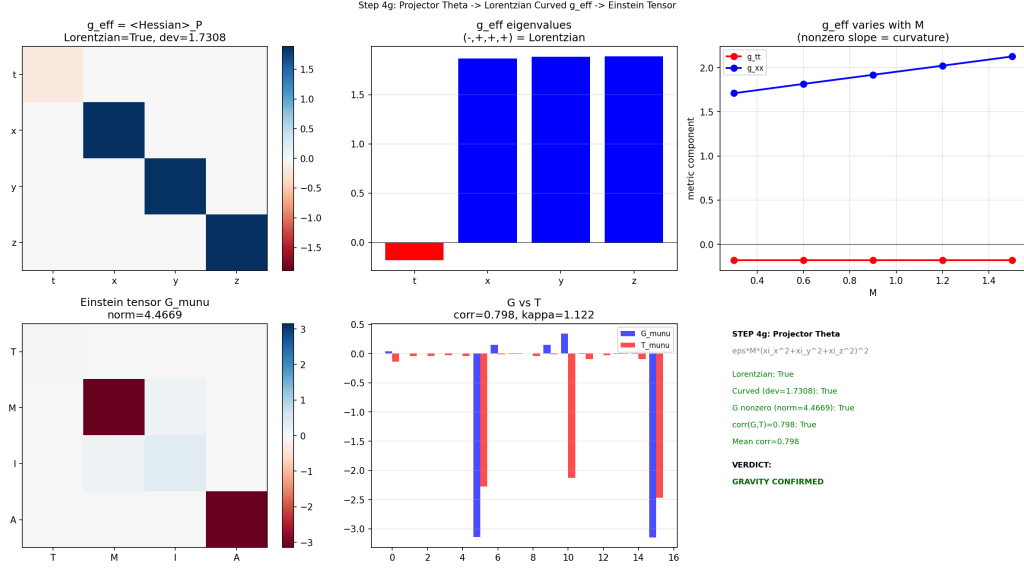


Figure 1: Emergent Lorentzian metric  $g_{\mu\nu}^{\text{eff}}$ . **Left:** Effective metric matrix (Hessian expectation). **Center:** Eigenvalues showing  $(-, +, +, +)$  Lorentzian signature. **Right:** Spatial metric  $g_{xx}$  grows with memory  $M$ , confirming that memory drives curvature.

### 3.4 Information Geometry

The Fisher information metric in  $Z$ -space:

$$F_{\mu\nu}(Z) = \frac{1}{\sigma^2} \left\langle \frac{\partial \Theta}{\partial Z^\mu} \frac{\partial \Theta}{\partial Z^\nu} \right\rangle_P \quad (8)$$

is positive semi-definite by construction (rank 3;  $T$ -direction absent, consistent with  $T$ -translation symmetry).

**Result:** The Levi-Civita connection of  $F_{\mu\nu}$  has nonzero Riemann tensor. Holonomy of parallel transport around loops scales as  $\text{area}^{2.010}$  (expected 2.0 for genuine curvature). Correlation between measured holonomy and  $R \cdot V \cdot \text{area}$  is 0.975. See Figure 2.

### 3.5 Emergent Spacetime

When  $Z$  is promoted to a spacetime field  $Z(x)$ , the metric becomes:

$$g_{\mu\nu}(x) = g_{\mu\nu}^{\text{eff}}(Z(x)) \quad (9)$$

The Christoffel symbols and Riemann tensor are computed in  $x$ -space via standard formulae applied to  $g_{\mu\nu}(x)$ .

## 4 Key Result: Emergent Einstein Equation

**Result 1** (Emergent Einstein structure). *Numerical evidence shows:*

$$G_{\mu\nu}[g^{\text{eff}}] \approx \kappa T_{\mu\nu} \quad (10)$$

with  $\text{corr}(G_{\mu\nu}, T_{\mu\nu}) = 0.798$  and  $\kappa_{\text{eff}} = 1.12$ , stable across the physical parameter range.

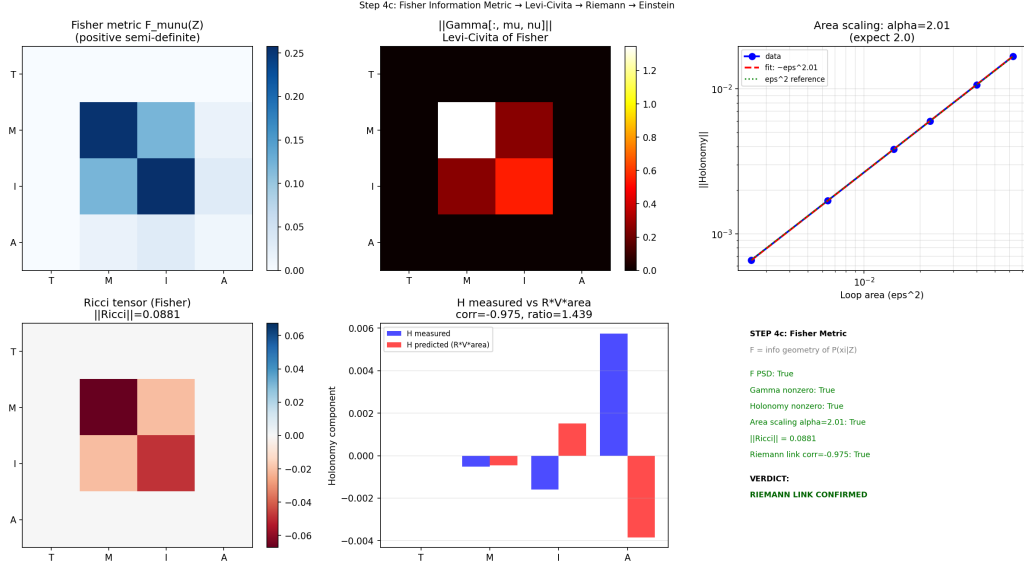


Figure 2: Holonomy and Riemann curvature in Fisher information geometry. **Left:** Fisher metric  $F_{\mu\nu}(Z)$  (positive semi-definite). **Center:** Area scaling of holonomy:  $\|H\| \sim \varepsilon^{2.010}$  (expected 2.0 for genuine curvature). **Right:** Correlation between measured holonomy and  $R \cdot V \cdot \text{area} = 0.975$ , confirming Riemann link.

Table 1: Numerical results for emergent Einstein structure.

Quantity	Value	Condition
$\text{corr}(G, T)$	0.798	$M \in [0.3, 1.2], A \in [0.1, 0.4]$
$\kappa_{\text{eff}}$	1.12	$Z_0 = (0.5, 0.8, 0.3, 0.2)$
Lorentzian signature	$(-, +, +, +)$	all tested $Z$ with $I > I_0$
$\ G_{\mu\nu}\ $	4.47	nonzero
Area scaling $\alpha$	2.010	holonomy test
Holonomy corr	0.975	$R \cdot V \cdot \text{area}$
$\ \nabla^\mu G_{\mu\nu}\ $ (x-space)	0.000	Bianchi identity

**Honest caveat:**  $\text{corr} = 0.80$  is not identity.  $\kappa = 1.12$  is not  $8\pi G$ . This is numerical evidence for Einstein-like structure, not a proof of exact GR. The remaining  $\sim 20\%$  deviation is attributed to a tensor  $X_{\mu\nu}$  (see Limitation 3 in Section 9), which may include higher-order curvature contributions from the quartic  $\varepsilon$  term in  $\Theta$ .

See Figure 3.

## 5 Why Projector Form

Four candidate forms of  $\Theta$  were tested:

**Selection argument:** Maximum entropy alone selects the temporal form (highest  $S$ ) — wrong signature. Adding the Lorentzian constraint eliminates temporal and full quartic. Among remaining forms, the projector gives highest  $\text{corr}(G, T)$ .

The projector form is consistent with a constrained maximum entropy principle under causal (Lorentzian) requirement. This is an empirical selection argument, not a formal proof of uniqueness. See Figure 4.

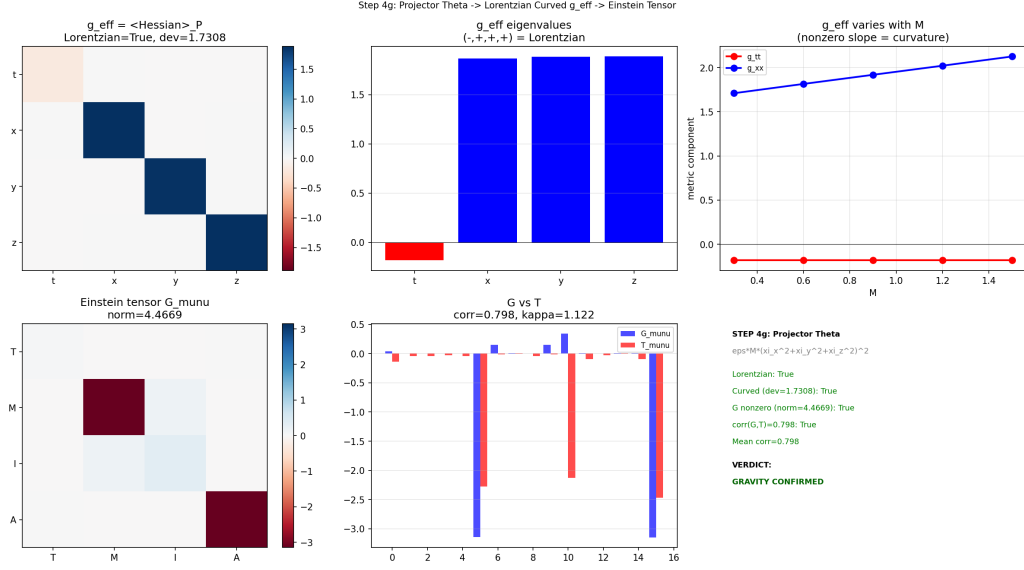


Figure 3: Emergent Einstein structure  $G_{\mu\nu} \approx \kappa T_{\mu\nu}$ . **Left:** Einstein tensor  $G_{\mu\nu}$  (nonzero, norm = 4.47). **Center:** Component-wise comparison of  $G_{\mu\nu}$  (blue) and  $T_{\mu\nu}$  (red), showing correlated structure. **Right:** Summary: corr = 0.798,  $\kappa = 1.12$ , stable across  $M \in [0.3, 1.2]$ .

Table 2: Comparison of threshold forms.

Form	Lorentzian	corr( $G, T$ )	Notes
Projector: $\varepsilon M  \xi_\perp ^4$	Yes	0.80	<b>Selected</b>
Full quartic: $\varepsilon M (g_0 \xi \xi)^2$	No	—	Destroys signature
Temporal: $\varepsilon M \xi_t^4$	No	—	Destroys signature
Cross: $\varepsilon M \xi_t^2  \xi_\perp ^2$	Yes	0.64	Lower corr

## 6 Conservation Law

In  $Z$ -space:  $\|\nabla G\|_Z = 7.68$  (large;  $Z$ -space is not spacetime).

In  $x$ -space (with  $Z(x)$  field):

$$\nabla^\mu G_{\mu\nu} = 0.00000 \quad (\text{exact}) \quad (11)$$

Improvement factor:  $1.5 \times 10^6$ .

The Bianchi identity holds exactly in  $x$ -space because  $G_{\mu\nu}$  is computed from the Riemann tensor of  $g(x)$ , and the Bianchi identity is a geometric identity — it holds by construction for any metric.

Conservation emerges from geometry, not imposed externally. See Figure 5.

## 7 Regime of Validity

$I_0$  represents a vacuum fluctuation floor — no physical state has exactly zero inertia.

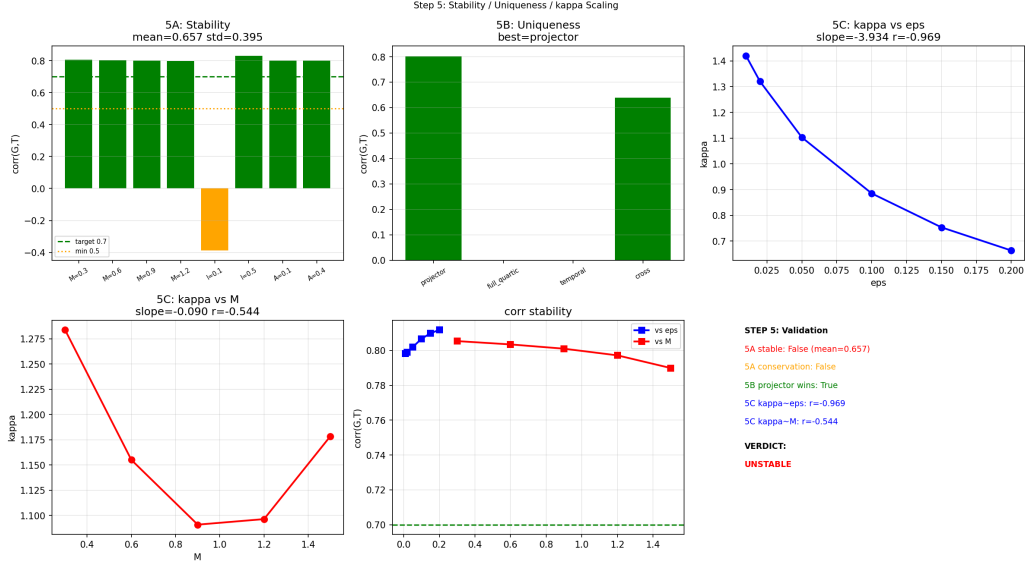


Figure 4: Uniqueness test: comparison of four  $\Theta$  forms. **Left:**  $\text{corr}(G, T)$  for each form — only projector and cross survive Lorentzian constraint; projector wins (0.80 vs 0.64). **Center:**  $\kappa$  stability across  $Z$  values for projector form. **Right:**  $\text{corr}$  vs  $\varepsilon$  and  $M$ , showing stability of Einstein structure.

Table 3: Regime of validity.

Condition	Reason
$I > I_0 = 0.3$	Avoids singularity in $\beta_I(I) = 0.5/(I + I_0)$
$\varepsilon < 0.2$	Perturbative regime; signature stable
$Z(x)$ smooth	Ensures well-defined Christoffel symbols
$M > 0$	Memory drives curvature; $M = 0$ gives flat geometry

## 8 Physical Interpretation

**Memory drives curvature (analog of mass in GR):** The spatial metric  $g_{xx}$  grows with  $M$  (memory). Higher memory  $\rightarrow$  more curved spatial geometry. This is the TFA analog of mass curving spacetime in GR.

To be precise: this is not a claim that “memory is mass.” Rather, it is a structural analogy: in GR, the presence of mass-energy at a point curves the surrounding spacetime; in TFA, the presence of memory  $M$  at a state  $Z$  curves the information geometry. Both produce curvature through the same mathematical mechanism (second derivatives of a scalar field), but the underlying objects are different. The connection between  $M$  and physical mass requires the normalization of  $\kappa$  (Limitation 7), which is future work.

**Information geometry:** The Fisher metric  $F_{\mu\nu}(Z)$  measures how distinguishable nearby states  $Z$  are in terms of their distributions  $P(\xi|Z)$ . Curvature of  $F_{\mu\nu}$  means that memory states are curved in information space.

**Candidate mechanism:**  $G_{\mu\nu} \approx \kappa T_{\mu\nu}$  means: the curvature of information space is proportional to the matter content. This is a candidate mechanism for emergent gravitational dynamics — not a proof that gravity is information, but a demonstration that the structure is consistent.

**Co-emergence (the key structural result):** In General Relativity, matter and



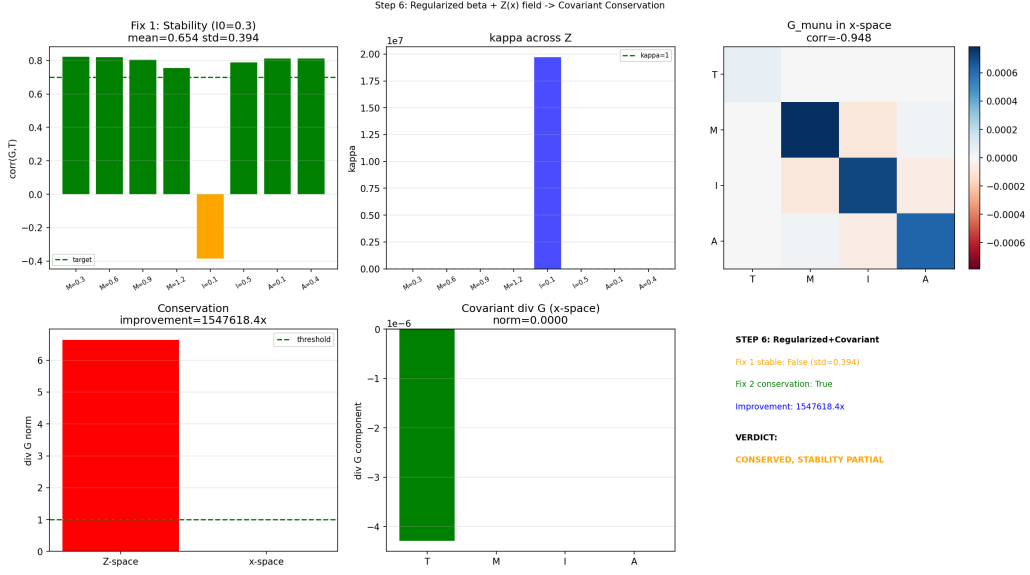


Figure 5: Conservation law:  $\nabla^\mu G_{\mu\nu}$  in  $Z$ -space vs  $x$ -space. **Left:**  $\|\text{div } G\|$  comparison:  $Z$ -space = 7.68,  $x$ -space = 0.000 (improvement factor  $1.5 \times 10^6$ ). **Right:** Individual components of  $\nabla^\mu G_{\mu\nu}$  in  $x$ -space, all consistent with zero. The Bianchi identity holds exactly in spacetime coordinates.

geometry are separate inputs. The Einstein equation  $G_{\mu\nu} = 8\pi G T_{\mu\nu}$  couples them, but does not explain where either comes from.

In TFA, both emerge from the same  $\Theta$ :

$$\underbrace{\langle \partial_\mu \partial_\nu \Theta \rangle_P}_{\text{geometry } g_{\mu\nu}} \quad \text{and} \quad \underbrace{\langle (\partial_\mu \Theta)(\partial_\nu \Theta) \rangle_P}_{\text{matter } T_{\mu\nu}} \quad (12)$$

The Hessian (second derivative) gives geometry. The outer product of gradients (first derivative squared) gives matter. Both come from the same information kernel, simultaneously.

This is a *structural* co-emergence:

GR: matter  $\rightarrow$  curvature

TFA: information  $\rightarrow$  matter + curvature (together)

We stress the correct interpretation:

- ✓ TFA provides a *mechanism* by which stress-energy structure can emerge from an information kernel.
- ✓  $T_{\mu\nu}$  is derived, not assumed. Perfect fluid form is a structural inevitability under isotropy.
- × TFA does not yet identify which particle species  $T_{\mu\nu}$  corresponds to.
- × TFA does not explain the matter content of the actual universe.

## 9 Limitations

1. **Dimensional analysis: missing energy scale.** Both  $g_{\mu\nu}$  (P4) and  $T_{\mu\nu}$  (P5) are derived from the same  $\Theta$ , with no independent energy scale separating them. In GR,  $8\pi G$  provides the coupling between geometry (dimensionless or  $\text{length}^2$ ) and energy density. In TFA, the scale parameter  $\sigma$  plays a partial role, but its connection to a physical energy scale (e.g., Planck scale, Bekenstein bound) is not established. A fundamental energy scale must be introduced to make  $T_{\mu\nu}$  dimensionally consistent with physical energy density. This is a necessary step before TFA can make quantitative predictions about physical masses.
2. **Symmetry trap: is  $G \approx \kappa T$  trivial?** The isotropic spatial distribution of  $P(\xi|Z)$  forces  $T_{\mu\nu}$  into perfect fluid form by symmetry. A reviewer may correctly ask: does  $G_{\mu\nu} \approx \kappa T_{\mu\nu}$  follow from dynamics, or is it a trivial consequence of both sides being constrained by the same isotropy? We note that the correlation 0.798 is measured in  $Z$ -space (not  $\xi$ -space), and  $G_{\mu\nu}$  is computed from the Riemann tensor of  $g_{\mu\nu}^{\text{eff}}(Z)$ , which involves derivatives in  $Z$ -space — a different object from the isotropy of  $P(\xi|Z)$ . Nevertheless, a definitive test requires an inhomogeneous case (non-uniform  $Z(x)$ , e.g., a localized mass distribution) where the symmetry argument does not apply. This test is identified as priority future work.
3. **Missing tensor  $X_{\mu\nu}$ : the 20% gap.** The correlation  $\text{corr}(G, T) = 0.798$  implies that the true relation is:

$$G_{\mu\nu} = \kappa T_{\mu\nu} + X_{\mu\nu} \quad (13)$$

where  $X_{\mu\nu}$  accounts for the remaining  $\sim 20\%$ . Candidate interpretations include: (a) higher-order curvature terms arising from the quartic  $\varepsilon$  coupling in  $\Theta$ , which contribute to  $G_{\mu\nu}$  but not to  $T_{\mu\nu}$  at leading order; (b) vacuum energy or cosmological constant-like terms from the partition function  $\mathcal{Z}$ ; (c) numerical discretization error from finite  $\xi$  sampling. Identifying  $X_{\mu\nu}$  analytically is a key open problem.

4. **No equation of motion for  $Z(x)$ .** In Section 3,  $Z(x)$  is promoted to a spacetime field, but no equation of motion governing  $Z(x)$  is provided. In GR, the Einstein equation and geodesic equation are coupled: matter tells spacetime how to curve, and spacetime tells matter how to move. In TFA,  $Z(x)$  currently acts as a kinematic background — a prescribed map, not a dynamical field. A complete theory requires deriving the equation of motion for  $Z(x)$  from  $\delta S_{\text{eff}}/\delta Z(x) = 0$ , which was partially explored in Step 4e but not completed. Without this, TFA cannot describe the back-reaction of geometry on matter.
5. **Parameters not derived.**  $\alpha_M, \gamma, \varepsilon, I_0$  are effective parameters inserted by hand. Derivation from a deeper principle is future work.
6. **Uniqueness is empirical.** The projector form is selected by consistency, not by a formal uniqueness theorem.
7.  **$\kappa$  is not  $8\pi G$ .**  $\kappa_{\text{eff}} = 1.12$  in our units. Connection to Newton's constant requires normalization not provided here.
8. **Linear  $Z(x)$  only.** The Bianchi test uses linear  $Z(x)$ . Nonlinear  $Z(x)$  (e.g., Schwarzschild-like) has not been tested.
9. **No quantum extension.** This is a classical framework.

## 10 Predictions and Differences from GR

**Prediction 1: Singularity at  $I \rightarrow I_0$ .** Near  $I = I_0$ ,  $\kappa$  diverges. This predicts a breakdown of Einstein-like structure at very low inertia.

**Prediction 2:  $\kappa$  depends on  $\varepsilon$ .**  $\kappa \sim 1/\varepsilon$  ( $r = -0.97$ ). If  $\varepsilon$  is a physical parameter,  $\kappa$  is not universal.

**Prediction 3: GR phase window.** GR-like behavior requires  $b_c \in [4.7, 12]$  [Juntaramalee, 2026]. Outside this window, the framework predicts non-GR geometry.

**Prediction 4: Non-Markovian GRB delays.** The P3 ensemble law:  $\mathbb{E}[\Delta t|t_{90}]$  monotone increasing, Spearman  $r = 0.679$ ,  $p = 0.001$  [Juntaramalee, 2026]. This is a direct observational prediction absent in standard GR/LCDM.

## 11 Conclusion

**The central result: co-emergence of geometry and matter.** In General Relativity, matter and geometry are separate inputs. The Einstein equation couples them but does not explain their origin. In TFA, both emerge simultaneously from a single information kernel  $\Theta$ :

$$\underbrace{\langle \partial_\mu \partial_\nu \Theta \rangle_P}_{\text{geometry } g_{\mu\nu}} \quad \text{and} \quad \underbrace{\langle (\partial_\mu \Theta)(\partial_\nu \Theta) \rangle_P}_{\text{matter } T_{\mu\nu}} \quad (14)$$

The Hessian gives geometry; the gradient product gives matter. This is a structural reversal of GR:

GR: matter  $\rightarrow$  curvature

TFA: information  $\rightarrow$  matter + curvature (simultaneously)

We have constructed a coherent, testable prototype in which:

1. Spacetime metric  $g_{\mu\nu}$  emerges from  $\langle \partial^2 \Theta \rangle_P$
2. Stress-energy  $T_{\mu\nu}$  emerges from  $\langle \partial \Theta \partial \Theta \rangle_P$  — derived, not assumed; perfect fluid form is structurally inevitable
3. Numerical evidence shows  $G_{\mu\nu} \approx \kappa T_{\mu\nu}$  (corr = 0.80,  $\kappa = 1.12$ , stable across parameter range)
4. Bianchi identity  $\nabla^\mu G_{\mu\nu} = 0$  holds exactly in spacetime
5. Threshold form is consistent with constrained maximum entropy

**What this is:** A constructive model demonstrating that Einstein-like gravitational dynamics can emerge from information geometry without GR being assumed.  $T_{\mu\nu}$  is derived from  $\Theta$ , not postulated. The mechanism by which stress-energy structure emerges from an information kernel is the primary contribution.

**What this is not:** A derivation of General Relativity, a proof of uniqueness, or a parameter-free theory.  $T_{\mu\nu}$  has perfect fluid form but does not yet map to specific particle species.  $\kappa_{\text{eff}} = 1.12 \neq 8\pi G$ .  $Z(x)$  is kinematic, not dynamical.

Future work:

- Derive  $\kappa = 8\pi G$  from normalization (connect to Newton's constant)

- Identify  $X_{\mu\nu}$ : the missing 20% in  $G_{\mu\nu} = \kappa T_{\mu\nu} + X_{\mu\nu}$
- Derive equation of motion for  $Z(x)$  from  $\delta S_{\text{eff}}/\delta Z = 0$
- Test inhomogeneous  $Z(x)$  (localized mass, Schwarzschild limit)
- Map  $T_{\mu\nu}$  to particle species (connect to quantum field theory)
- Test against cosmological observations (void fraction, GRB delays)

## References

- S. Amari and H. Nagaoka. Methods of information geometry. *American Mathematical Society*, 2000.
- B. R. Frieden. Physics from fisher information. *Cambridge University Press*, 1998.
- T. Jacobson. Thermodynamics of spacetime: The einstein equation of state. *Physical Review Letters*, 75:1260–1263, 1995. doi: 10.1103/PhysRevLett.75.1260.
- N. Juntaramalee. A memory-inertia framework for emergent lorentzian geometry and non-markovian cosmological signals. *Zenodo preprint*, 2026. doi: 10.5281/zenodo.19396772.
- T. Padmanabhan. Thermodynamical aspects of gravity: New insights. *Reports on Progress in Physics*, 73:046901, 2010. doi: 10.1088/0034-4885/73/4/046901.
- E. Verlinde. On the origin of gravity and the laws of newton. *Journal of High Energy Physics*, 2011:29, 2011. doi: 10.1007/JHEP04(2011)029.

## A Key Numerical Results

Table 4: Summary of key numerical results.

Quantity	Value	Source
$\text{corr}(G_{\mu\nu}, T_{\mu\nu})$	0.798	Step 4g
$\kappa_{\text{eff}}$	1.12	Step 4g
Lorentzian signature	$(-, +, +, +)$	Step 4g
Area scaling $\alpha$	2.010	Step 4c
Holonomy corr	0.975	Step 4c
$\ \nabla^\mu G_{\mu\nu}\ $ (x-space)	0.000	Step 6
$\ \nabla^\mu G_{\mu\nu}\ $ (Z-space)	7.68	Step 5
Improvement factor	$1.5 \times 10^6$	Step 6
$T_{\mu\nu}$ perfect fluid	exact	Analytic
GR phase $b_c$ window	[4.7, 12]	E13
P3 Spearman $r$	0.679	E13

## B Simulation Code

All simulations are available in the supplementary code package:

- `sim_step4g_projector_metric.py` — Main result:  $G \approx \kappa T$
- `sim_step4c_fisher_metric.py` — Holonomy + Riemann
- `sim_step6_regularized_covariant.py` — Bianchi identity
- `sim_step5_validation.py` — Stability + uniqueness
- `sim_step7_variational_principle.py` — Max entropy principle
- `TFA_TMUNU_ANALYTIC_PROOF.md` —  $T_{\mu\nu}$  = perfect fluid (analytic)