

Schmidt Number of Sand Suspensions In Oscillating-Grid Turbulence.

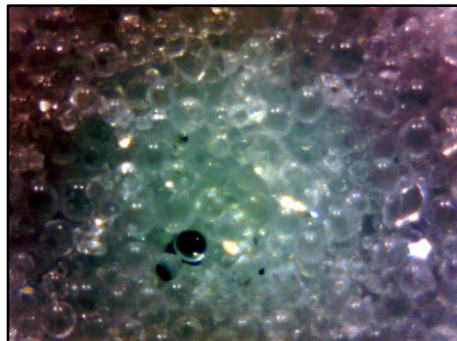
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Schmidt Number

$$\beta = \frac{\nu_t}{\varepsilon_s}$$

Ratio of momentum and mass diffusivities

Many models assume $\beta=1$. Only for fine particles in very dilute concentrations $C=O(0.001)$

$\beta>1$: particles lose correlation with fluid motion as settle through eddies?

$\beta<1$: centrifugal forces have larger effect on particles than on surrounding fluid?

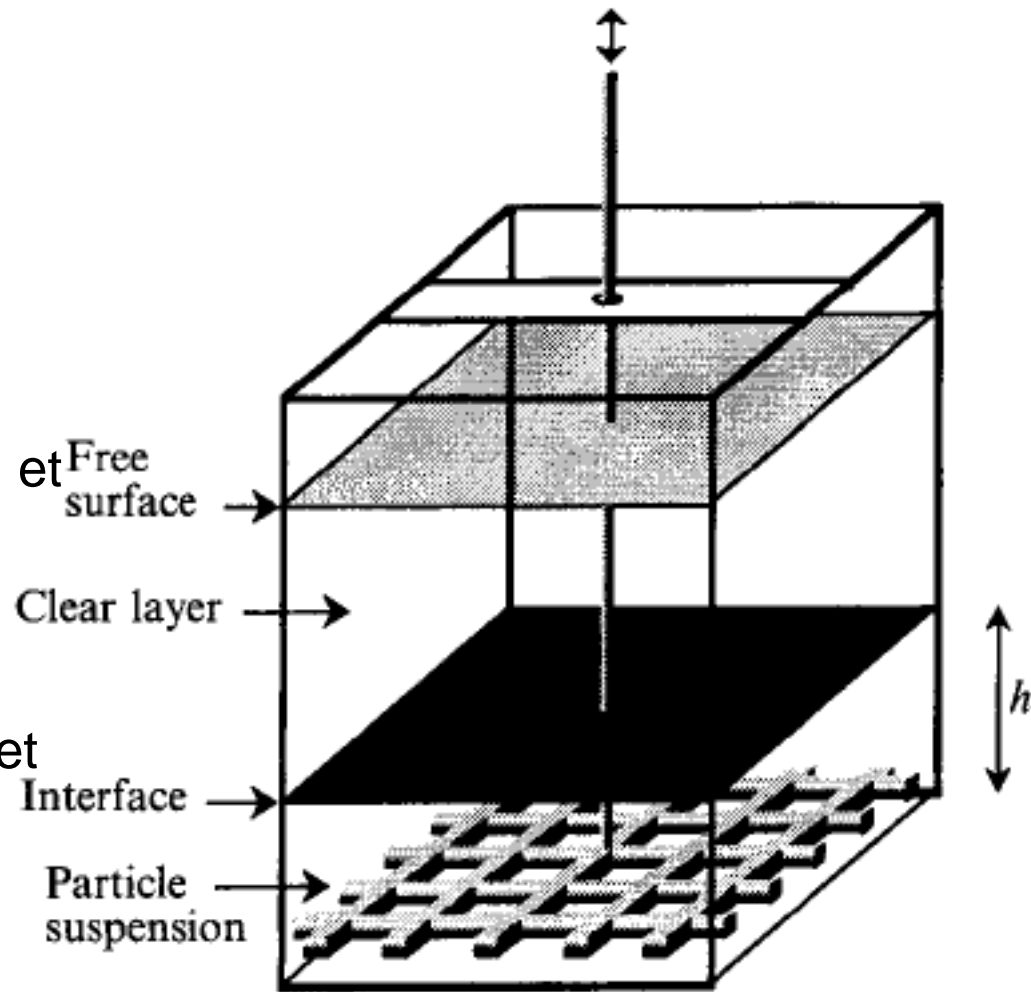
Literature reports values 0.1 to 10

May depend on model equations and boundary conditions

Often used as a tunable parameter

Oscillating Grid Turbulence

- Statistical characteristics of turbulence well-known (e.g. Hopfinger & Toly, 1976; Matsunaga et al., 1999)
- Non-cohesives: sediment initiation of motion (e.g. Medina et al., 2001)
- Cohesives: stratification (e.g. Michallet & Mory 2004; Gratiot et al., 2005)
- Sediment diffusivity: stationary sediment suspension, gradient diffusion



Huppert et al., JFM 1995

Oscillating Grid Turbulence Tank

50x50x80cm

Bar thickness $m = 1$ cm, mesh size $M = 5$ cm ($M/m = 5$)

Grid porosity 65% = most efficient for reducing secondary flows (Hopfinger and Toly, 1976)

Fresh tap water at 20°C
seeded with 11μm
hollow spheres

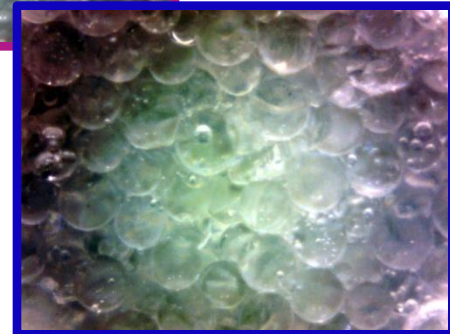
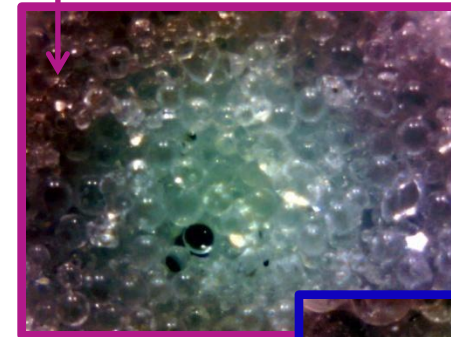
$f=2\text{Hz}$, $S=10\text{cm}$

$f=3\text{Hz}$, $S=7\text{cm}$

$$\text{Re} = \frac{fS^2}{\nu}$$



Solid glass spheres:
70-110μm and 145-205μm

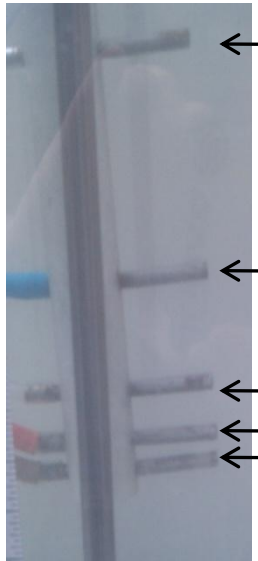


Nortek Vectrino II
Acoustic Doppler Profiler
(30mm profiles at 100Hz)

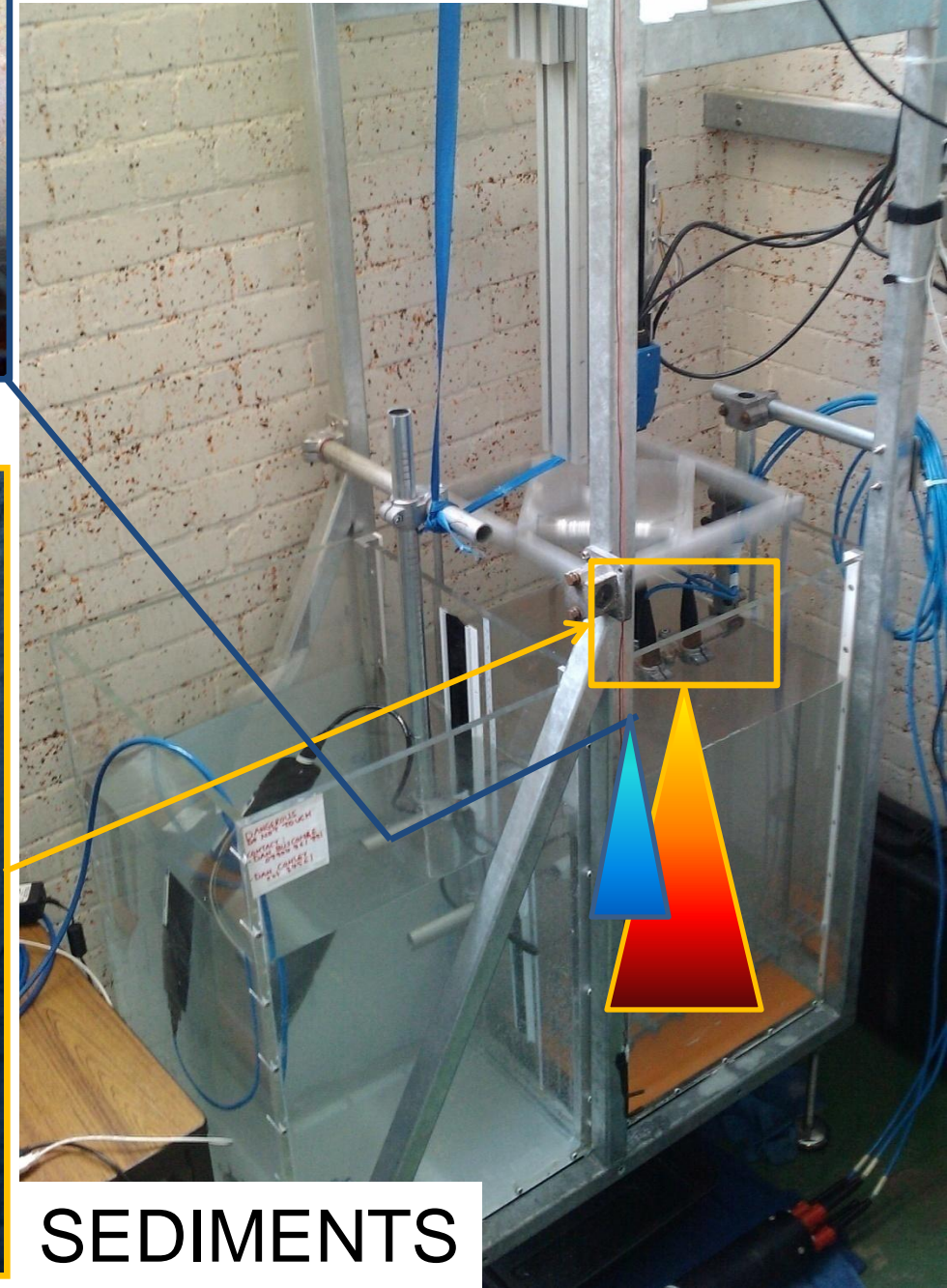
Only $R > 90\%$,
Amplitudes $> -50\text{dB}$
Phase-space de-spiking
(Goring and Nikora, 2002)

1,2,4MHz Acoustic Backscatter
System (ABS)
Suspension of spheres:
analytical form
function

Physical
samples: pump
sampler with 5
intake hoses
(5mm ID)



TURBULENCE



SEDIMENTS

Sediment Size and Fall Velocity

Stokes' law used for **fine sediment**

$$Re = \frac{w_s D}{\nu} = 0.45 \quad w_s = \frac{RgD^2}{C_1 \nu}$$

$Re=2.5$ for **coarser sediment**

Ferguson and Church (2004):

$$w_s = \frac{RgD^2}{C_1 \nu + \sqrt{0.75 C_2 RgD^3}}$$

$$C_1 = 18$$

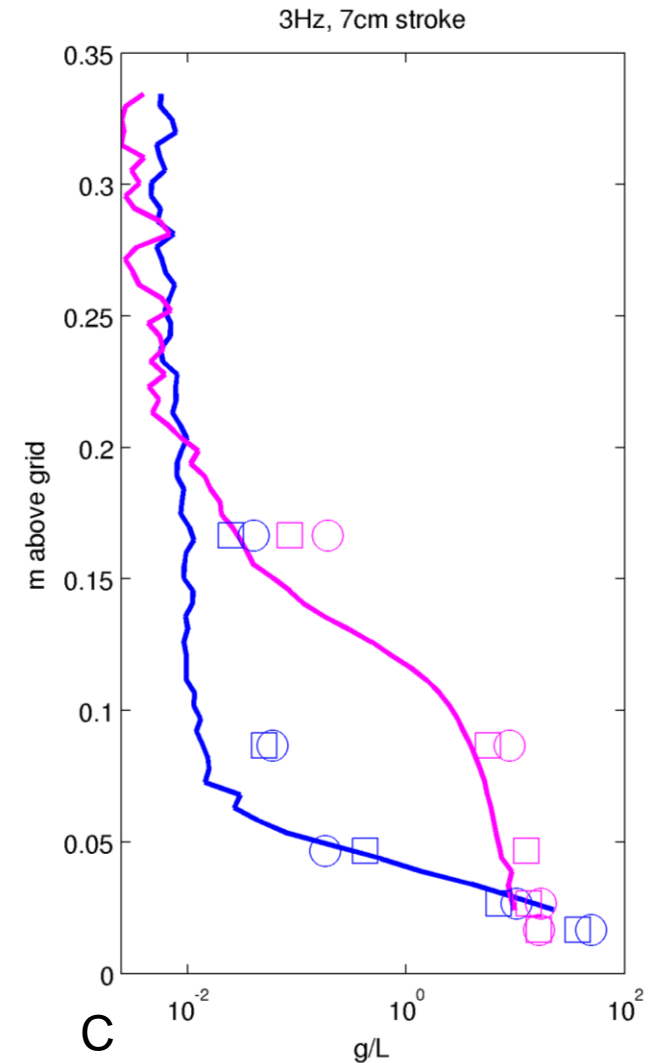
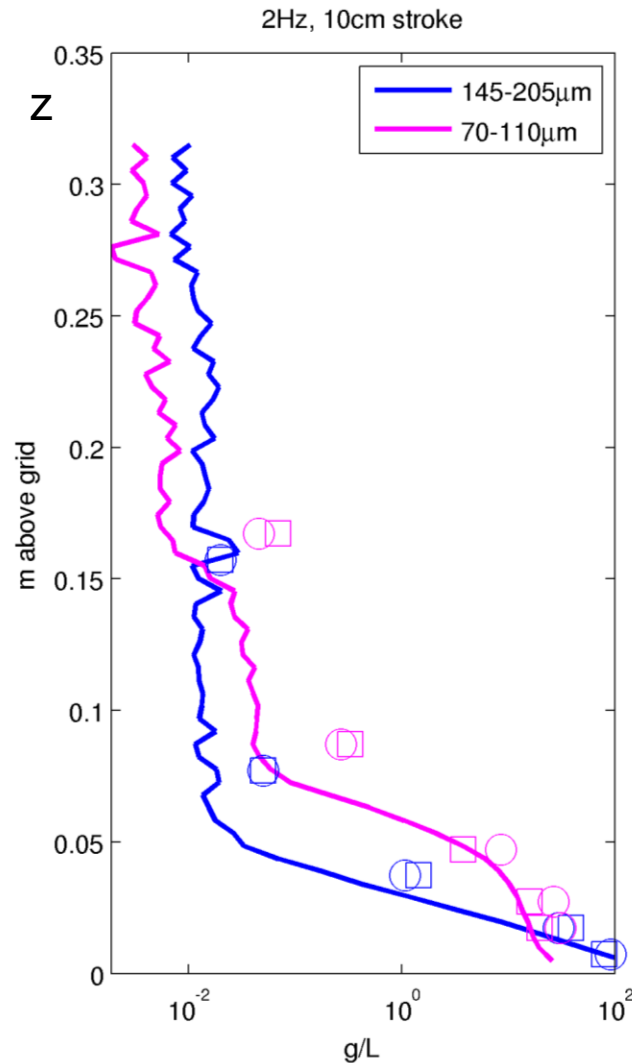
$$C_2 = 0.4 \text{ for smooth spheres}$$

$$R = 1.65 \text{ for quartz in water}$$



Sediment Concentration

Time-averages of C from ABS:



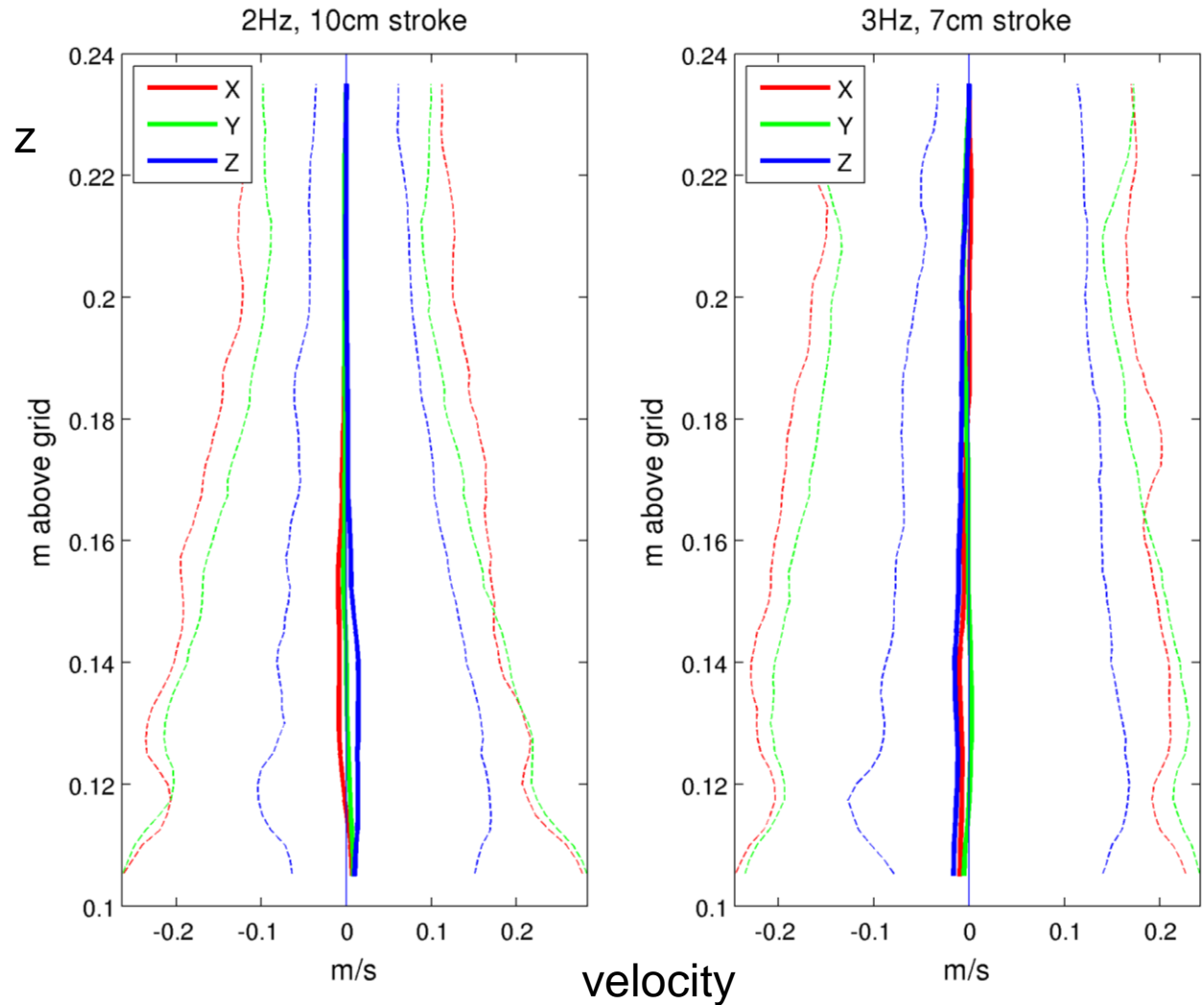
COARSE

FINE

Mean Velocity Profiles

$$0.8 \leq \frac{\overline{\rho u' w'}}{\rho \sigma_u \sigma_w} \leq 1$$

(=1 for homogeneous and isotropic turbulence)



Gradient Diffusion

$$\epsilon_s \frac{d\bar{C}}{dz} - \bar{C}(z) w_s = 0$$



Upward mixing flux:
proportional to concentration gradient



Downward settling flux

$$\epsilon_s = \frac{-w_s \bar{c}}{\frac{d\bar{c}}{dz}}$$

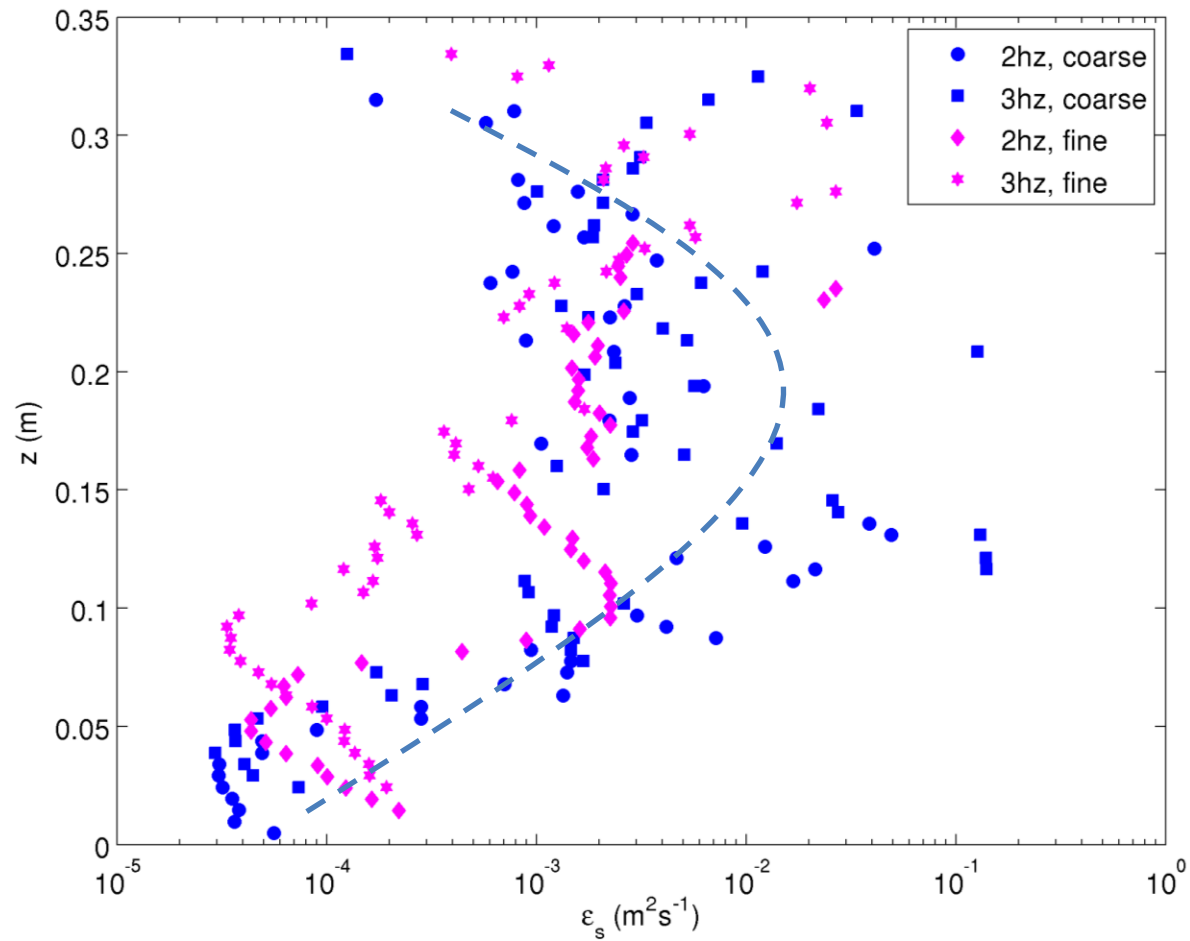
Diffusivity of Sediment

$$\varepsilon_s = \frac{\frac{w_{sj} + w_{sk}}{2} \frac{\bar{c}_j + \bar{c}_k}{2} z}{\frac{\bar{c}_k - \bar{c}_j}{\Delta jk}}$$

$$\Delta jk = 5\text{mm}$$

COARSE

FINE



Model for Concentration Profile

$$\bar{c} = \bar{c}_{z=z_a} \left(\frac{h-z}{z} \frac{z_a}{h-z_a} \right)^{-w_s / \kappa u_*}$$

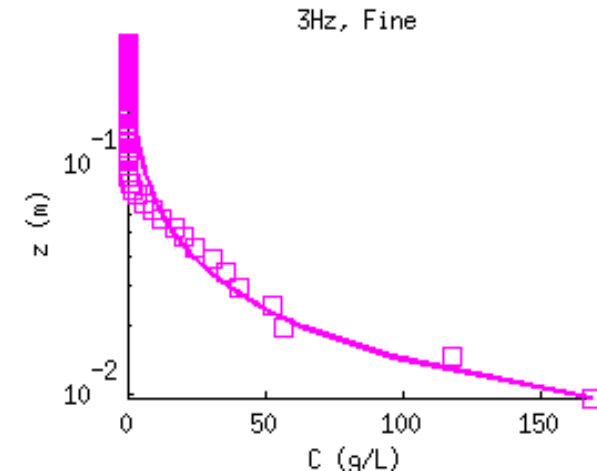
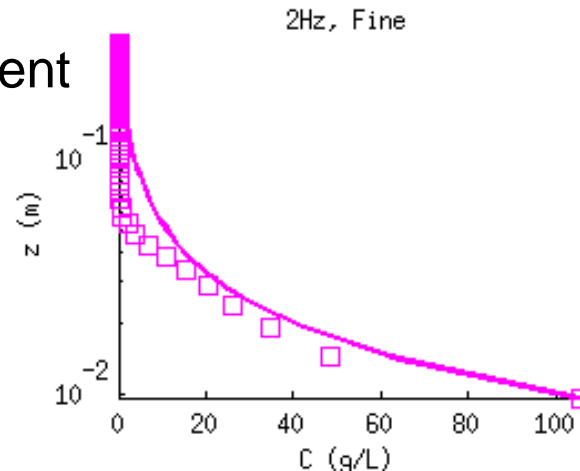
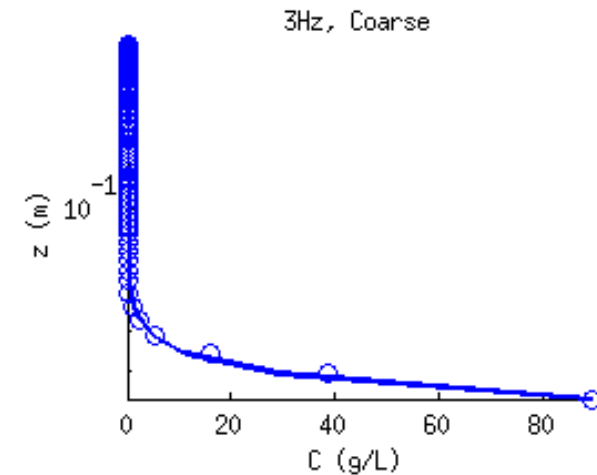
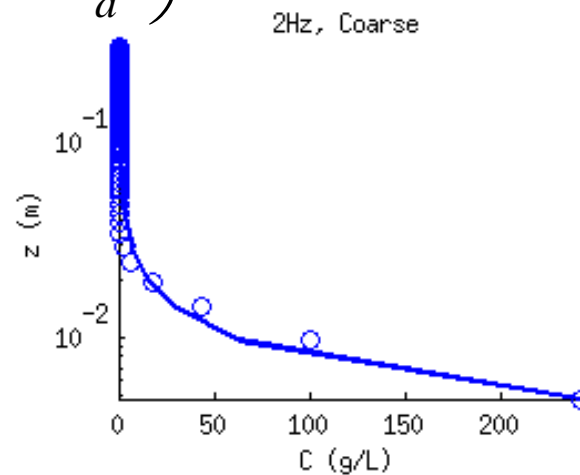
← Rouse

Replace with the form:

$$\bar{c} = \alpha \left(\frac{h-z}{z} \right)^\gamma$$

↑
diffusion coefficient

↑
'reference concentration'

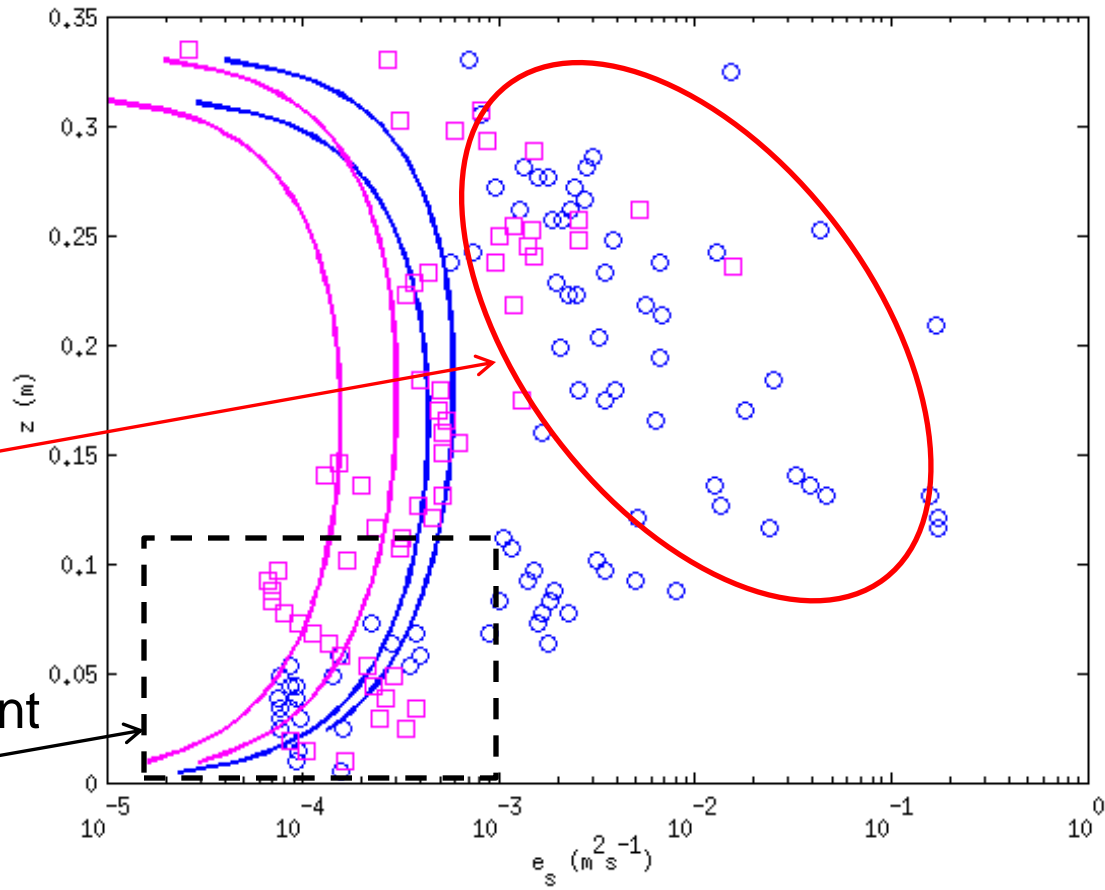


Expression for Sediment Diffusivity

$$\varepsilon_s = \frac{-w_s \bar{c}}{\frac{-\alpha \gamma h}{z^2} \left(\frac{h-z}{z} \right)^{\gamma-1}}$$

Worse agreement
when C measurements
don't rapidly go to zero

Good agreement
at high C

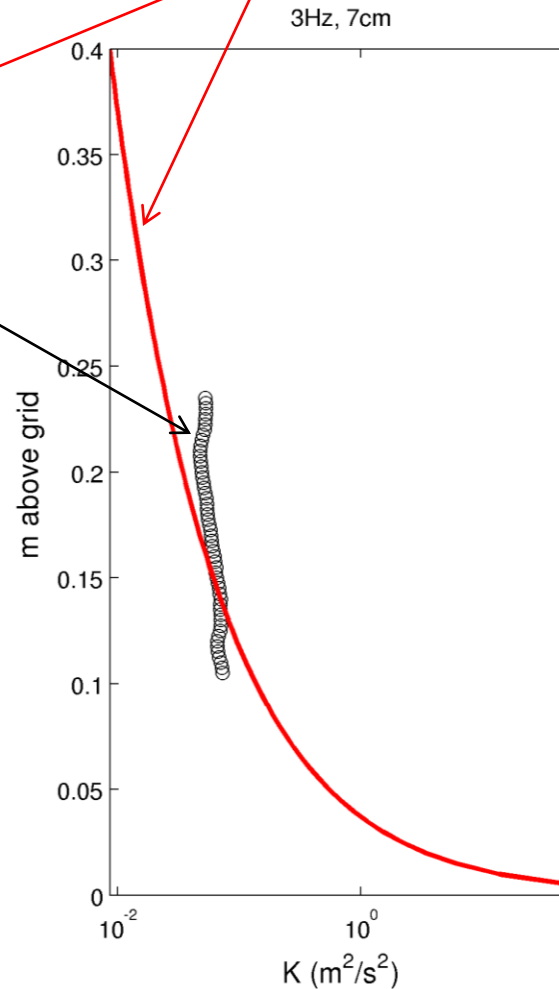
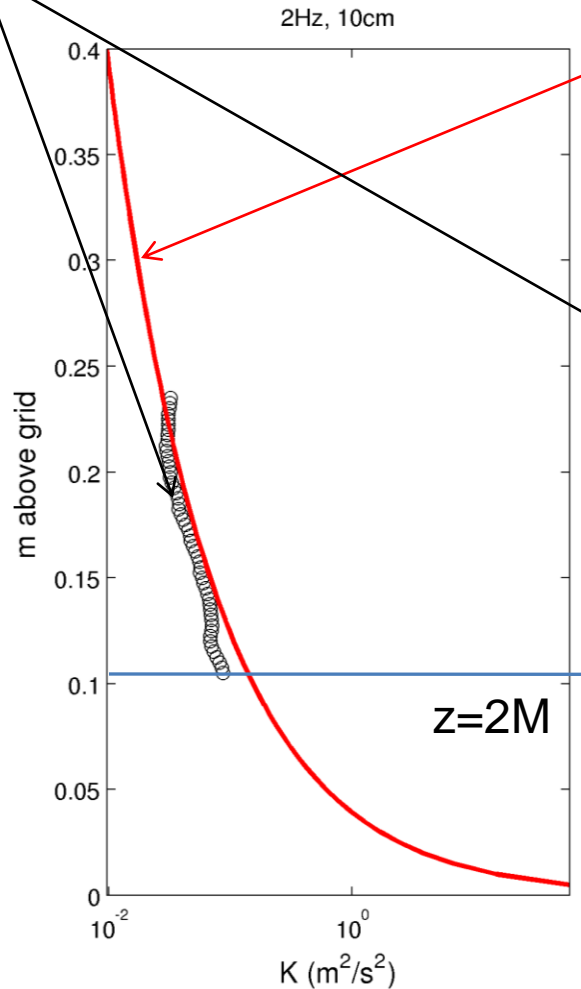


Turbulent Kinetic Energy

$$k = \frac{1}{2} (u'^2 + v'^2 + w'^2)$$

$$k = \frac{1}{2} (2C_1^2 + C_2^2) (M^{0.5} S^{1.5} f z^{-1})^2$$

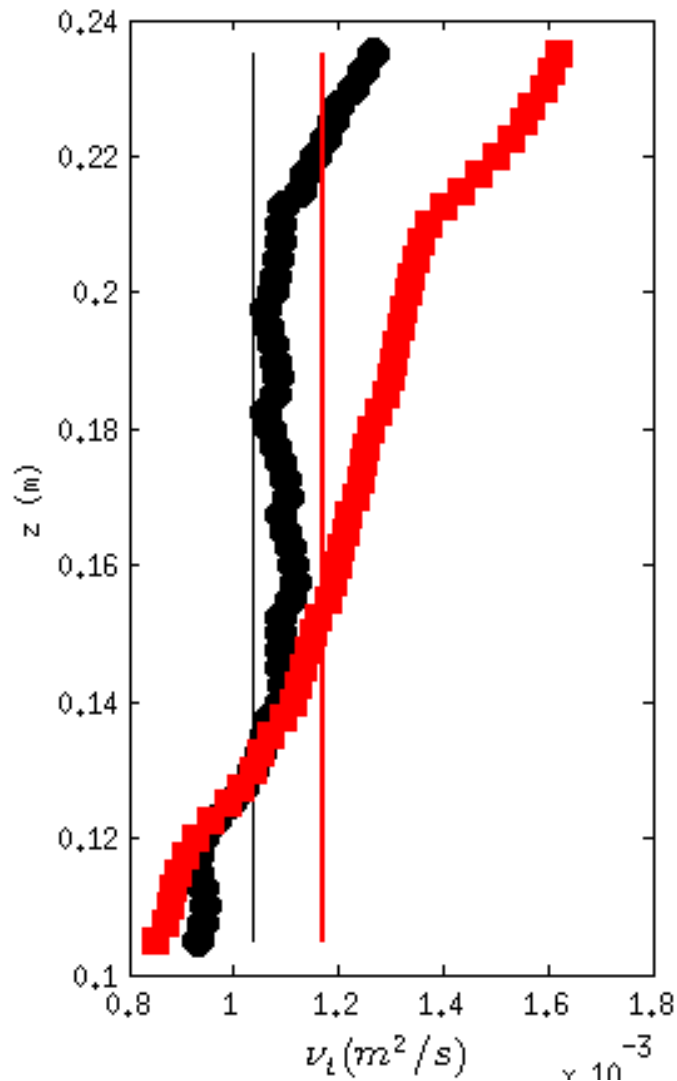
Orlins & Gulliver
(2003)



$C1 = 0.22$
 $C2 = 0.26$
 DeSilva
 & Fernando
 (1992)

$M=5$
 $S=10 \text{ or } 7 \text{ cm}$
 $f= 2 \text{ or } 3\text{Hz}$

Expression for Momentum Diffusivity



$$\nu_t = C_\mu k^2 / \varepsilon \quad \varepsilon = C_\mu^{3/4} \frac{k^{3/2}}{l}$$

$$l = 0.1z$$

$$k = \frac{1}{2} (2C_1^2 + C_2^2) (M^{0.5} S^{1.5} fz^{-1})^2$$

$$\nu_t = \sqrt{C_\mu} \sqrt{\frac{1}{2} \omega (S^{1.5} fz^{-1} \sqrt{M})} 0.1z$$

$$\omega = 2C_1^2 + C_2^2$$

$$\beta = \frac{\nu_t}{\varepsilon_s}$$

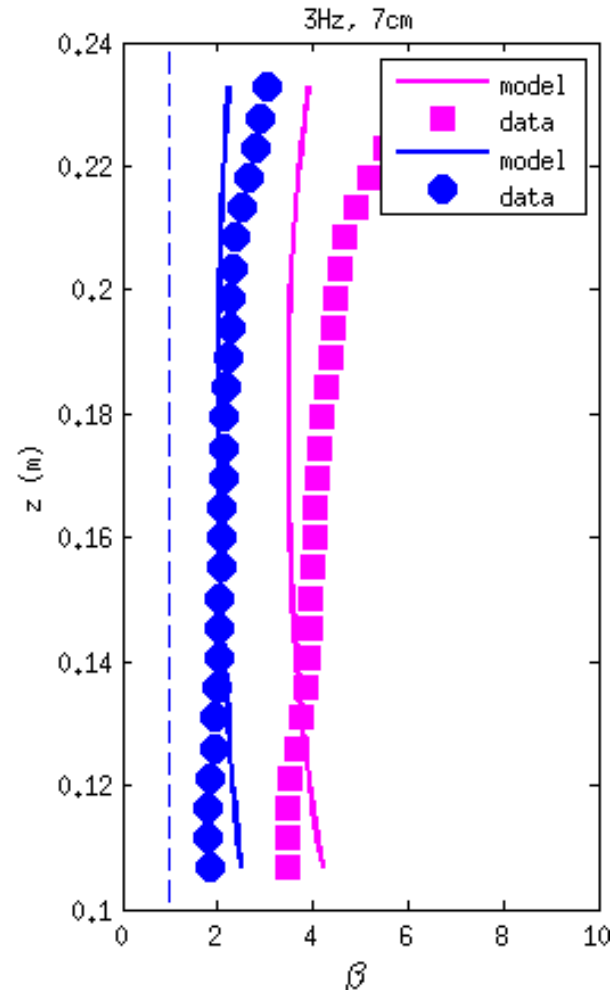
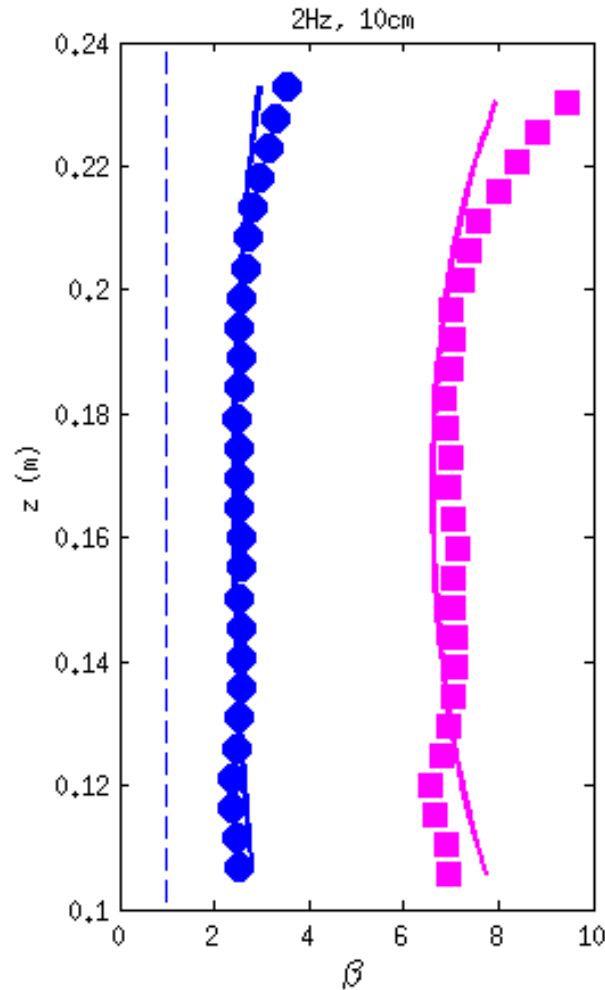
Schmidt Number

COARSE

FINE

coarse
sand
momentum
more
diffusive
than
sediment

fine sand
momentum
much more
diffusive
than
sediment



relatively
invariant with
depth

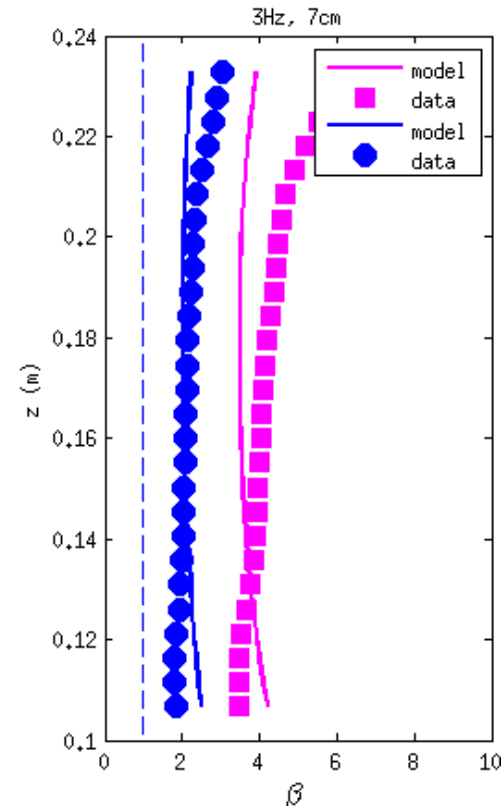
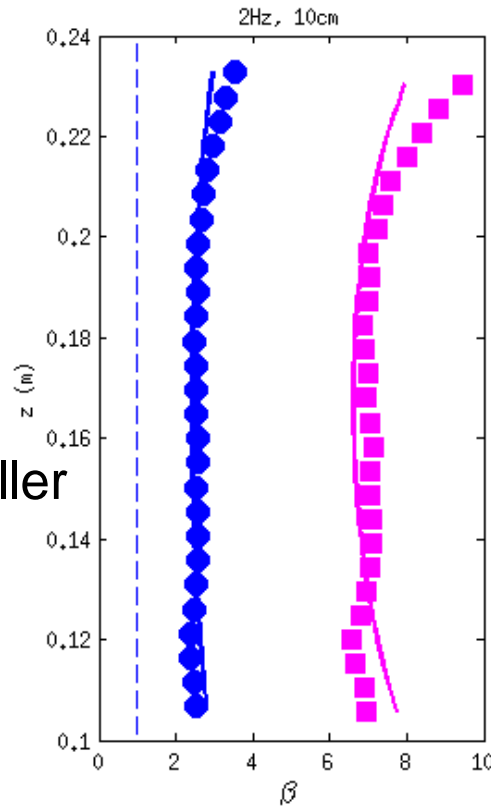
analytical
model gives
good
approximation

$$\text{Re} = \frac{fS^2}{\nu} = 14705$$

$$= 10808$$

Grain Size Dependence?

- Nielsen & Teakle (2004) also observed $>\beta$ for smaller particles
- Settling of finer grains faster in turbulence than in still water?
- Mixing length for finer grains smaller than for the fluid?
- β increases with C because of negative feedback? (Lees, 1981; Amoudry et al., 2005)
- Stratification effects (which would reduce eddy viscosity and β)



Conclusions

- Calculated Schmidt number for sand suspensions in near-isotropic grid turbulence in zero-mean-shear flows
- 2 flow conditions and 2 different sized glass spheres
- **Momentum diffusivity greater than sediment diffusivity ($\beta > 1$)**
- Grain-size dependence?
- Reynolds number dependence

Ongoing work:

- Spectral estimation of ϵ
- Greater range of flow conditions and sediment types
- Stratification effects
- Further investigation of Vectrino II

How do these results apply when gradient diffusion not dominant process (e.g. large mixing lengths)?

Thanks for your attention.

www.research.plymouth.ac.uk/tssar_waves/

www.coastalprocesses.org

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File Edit View Terminal Help

```
ce3plus          = 1.000000000000000000
sig_k            = 1.000000000000000000
sig_e           = 1.1112026371683261
```

```
Value of the stability function
in the log-law,
in shear-free turbulence,
```

```
cm0 = 0.547699999999999996
cmsf = 0.547699999999999996
```

```
von Karman constant,      kappa = 0.400000000000000002
homogeneous decay rate,   d = -1.0869565217391306
spatial decay rate (no shear), alpha = -17.758155956768427
length-scale slope (no shear), L = 2.51825233691378540E-002
steady-state Richardson-number, Ri_st= 0.250000000000000000
```

```
init_output
```

```
Output in NetCDF (time unit is set to seconds):
```

```
./SD_322_dist_ds_run99.nc
```

```
init_sediment
```

```
Using eulerian approach
```

```
Computing sediment concentration in lowest box
according to Smith and McLean (1977)
done.
```

```
time loop
```

```
Saving....1997-10-19 04:39:44.3000
```

```
Saving....1997-10-19 04:39:44.5500
```

```
Saving....1997-10-19 04:39:44.8000
```

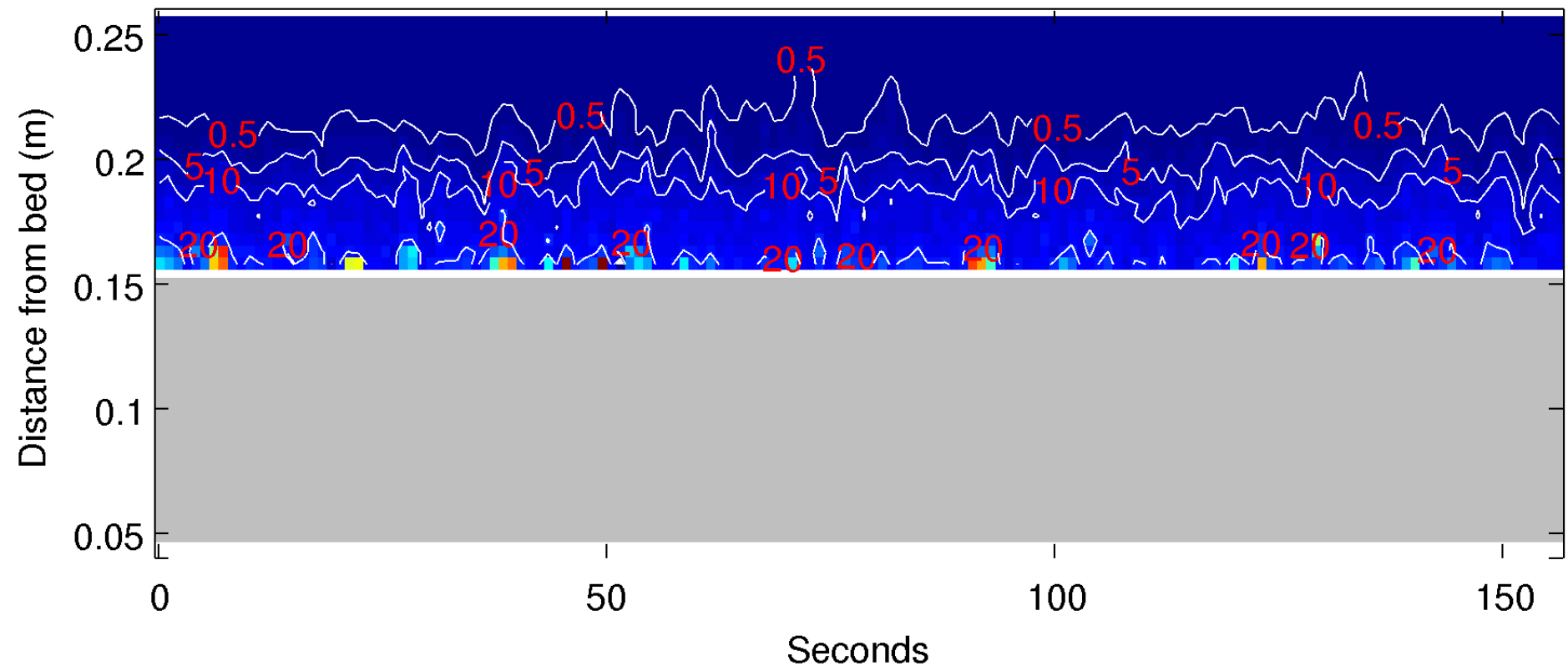
TSSARWaves

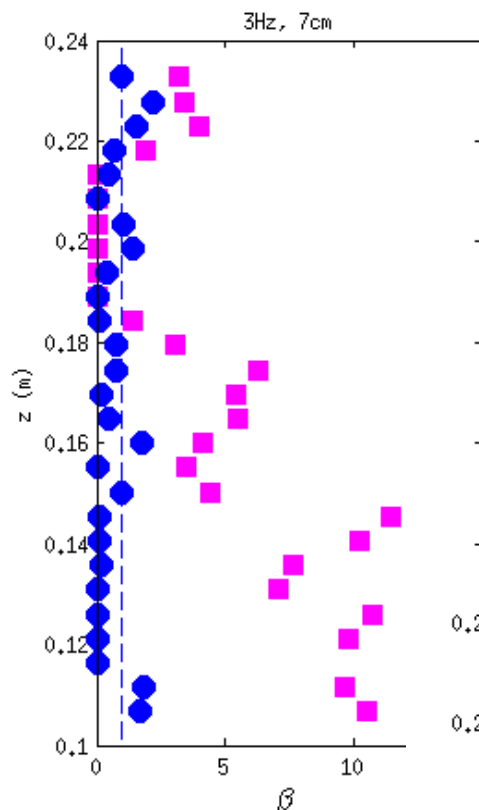
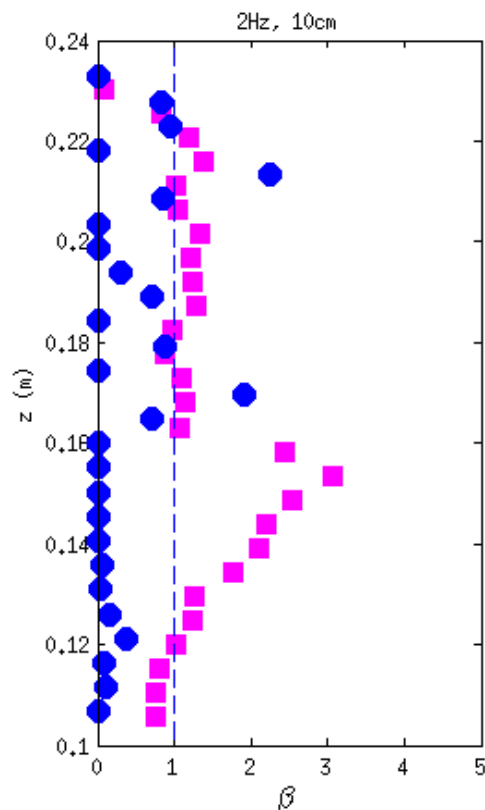
***Turbulence,
Sediment
Stratification,
and
Altered
Resuspension
under
Waves***

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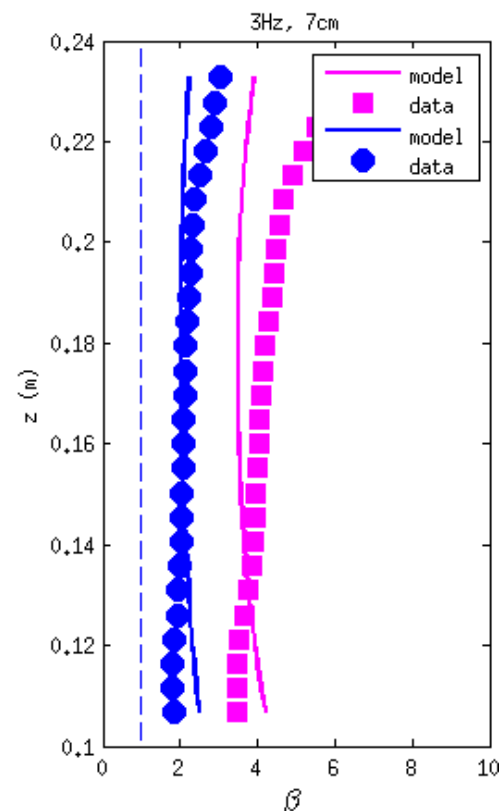
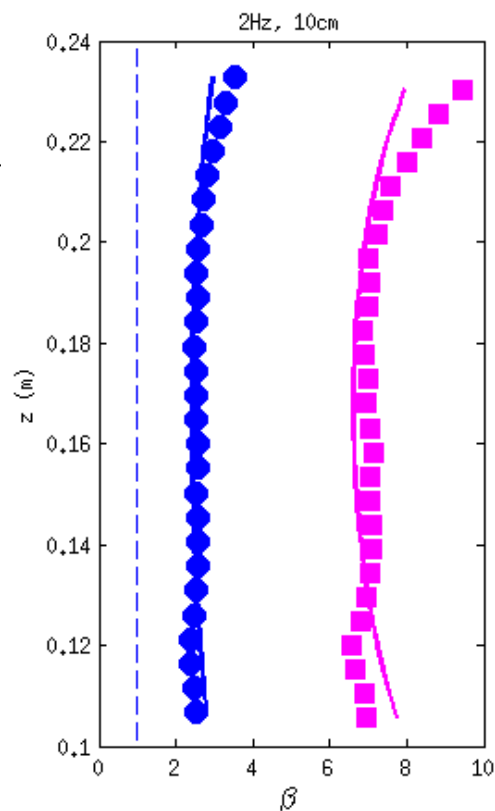
Stationary Suspension

2Hz, 10cm stroke (1s averages)





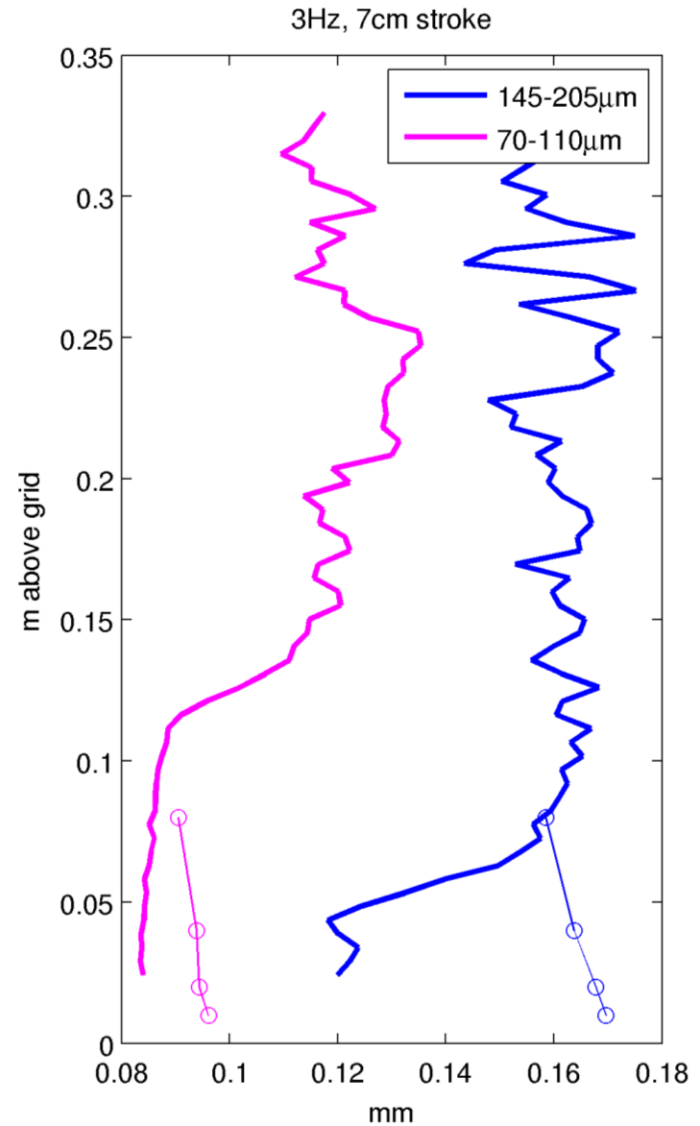
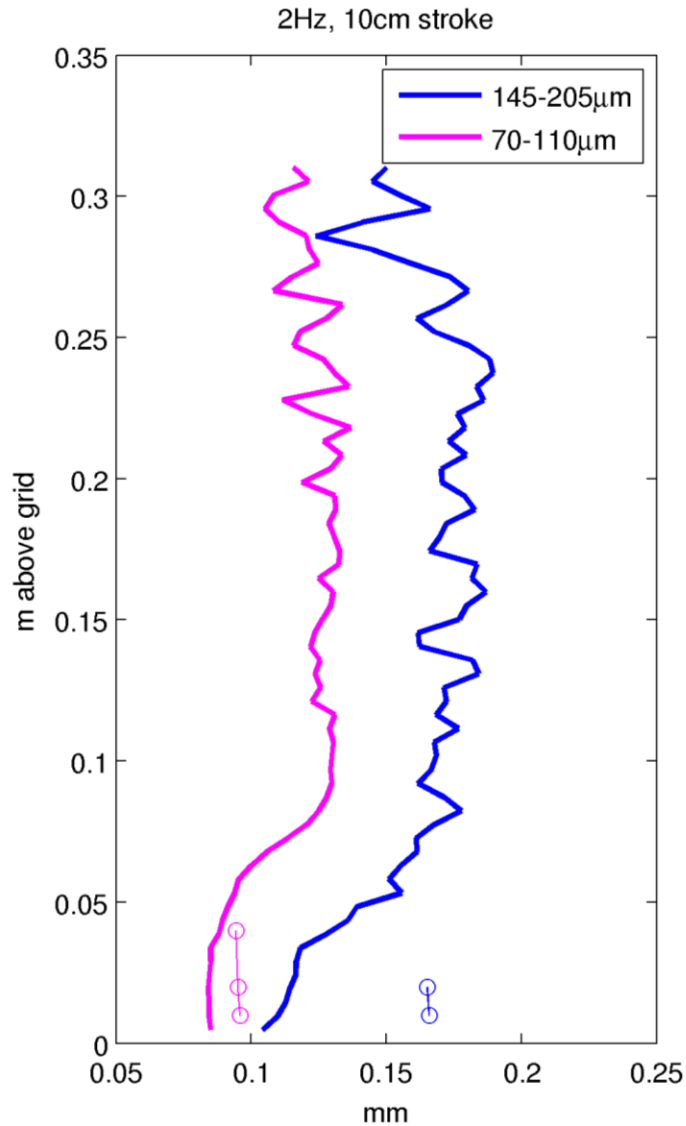
Measured ε_s and v_t based on measured k



Dots: modelled ε_s and v_t based on measured k

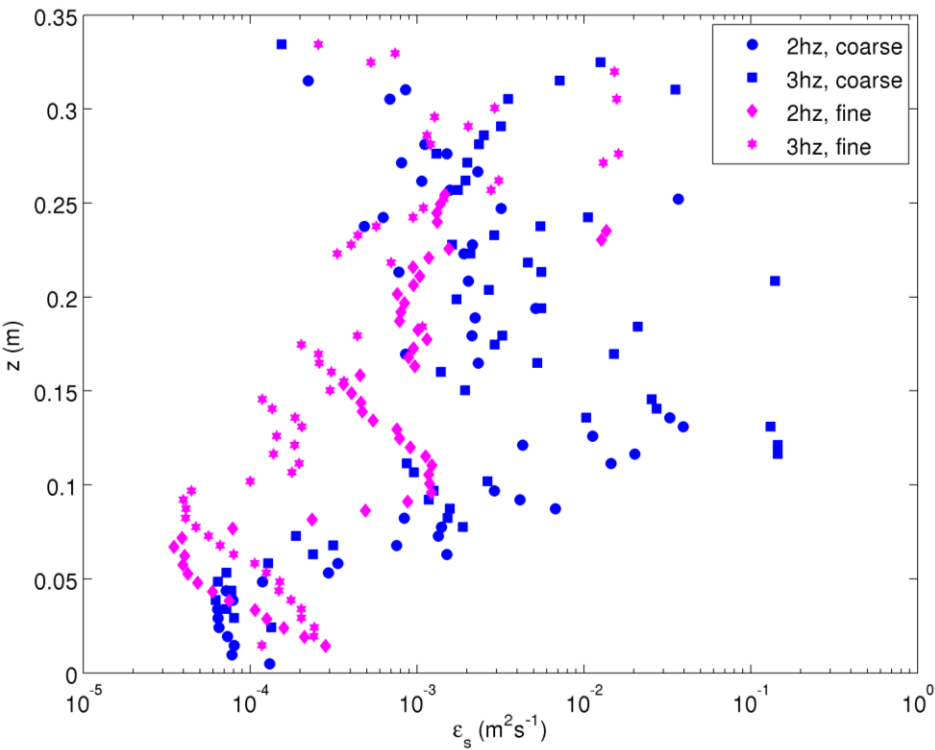
Lines: modelled ε_s and v_t based on modelled k

Variation of D

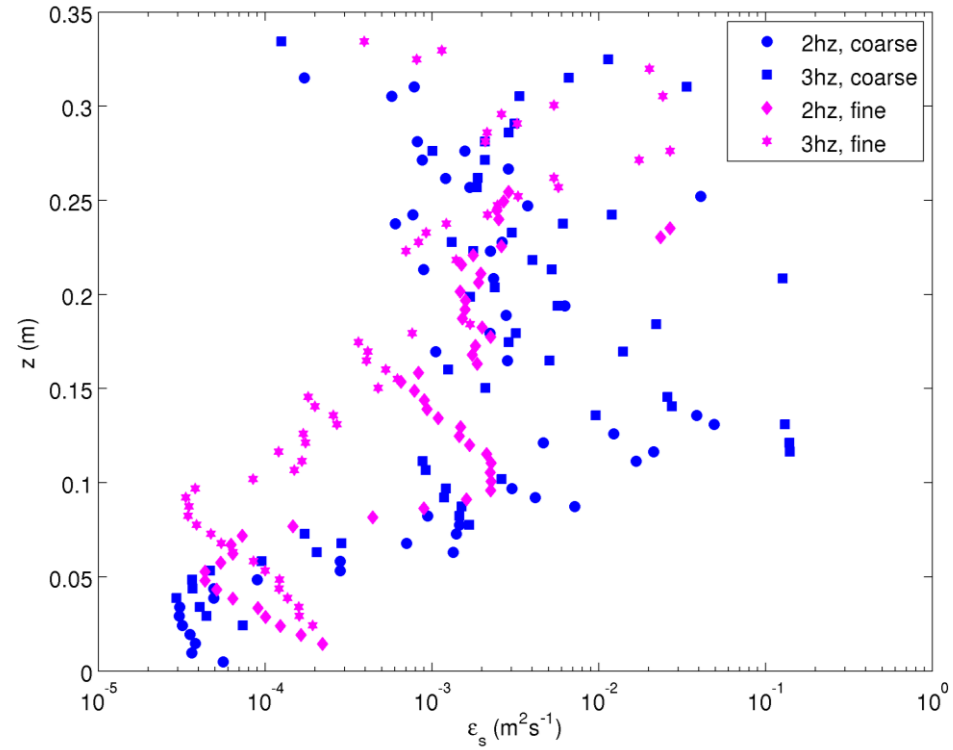


Grain Size Effect on ε_s

Constant D



$D(z)$



Talk Outline

- Oscillating grid turbulence
- Experiments and measurements
- Profiles of velocity and concentration
- Analytical expressions for sediment diffusivity and turbulent mixing
- Vertical profiles of Schmidt number
- Discussion of these initial results and ongoing/future work