

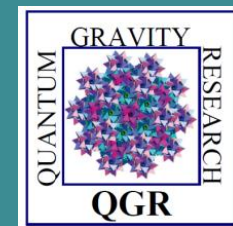
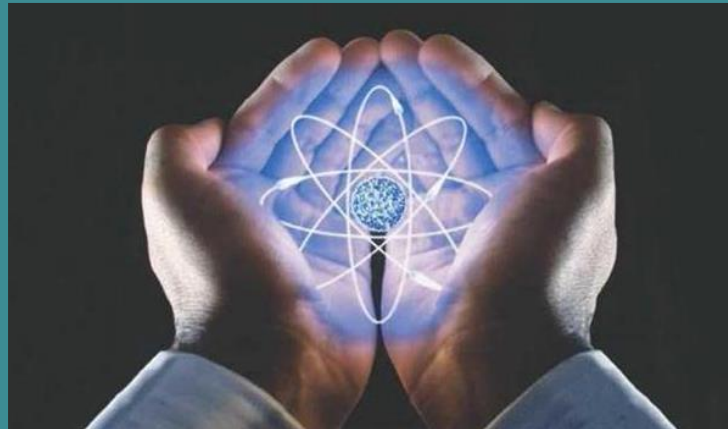
Chemical and nuclear catalysis mediated by the energy localization in crystals and quasicrystals

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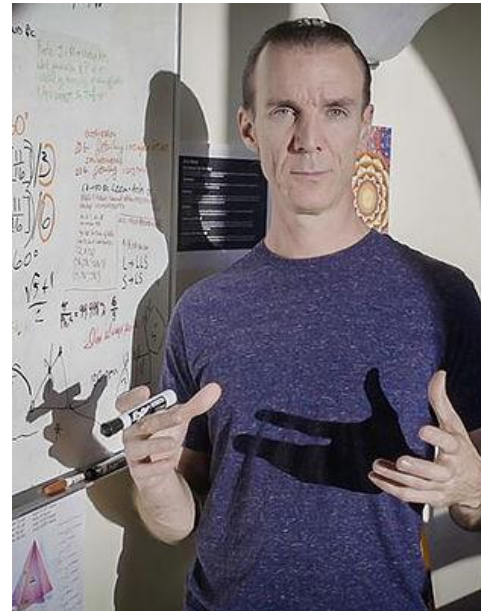
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Outline

- Localized Anharmonic Vibrations: history and the state of the art
- LAV role in **chemical** and **nuclear** catalysis
- MD simulations in crystals and quasicrystalline clusters

Energy localization in anharmonic lattices

In the summer of 1953 [Enrico Fermi](#), [John Pasta](#), [Stanislaw Ulam](#), and [Mary Tsingou](#) conducted numerical experiments (i.e. computer simulations) of a vibrating string that included a non-linear term (quadratic in one test, cubic in another, and a piecewise linear approximation to a cubic in a third). They found that the behavior of the system was quite different from what intuition would have led them to expect. Fermi thought that after many iterations, the system would exhibit [thermalization](#), an ergodic behavior in which the influence of the initial modes of vibration fade and the system becomes more or less random with [all modes excited more or less equally](#). Instead, the system exhibited a very complicated quasi-periodic behavior. They published their results in a [Los Alamos](#) technical report in 1955.

The **FPU paradox** was important both in showing the **complexity of nonlinear system** behavior and the value of computer simulation in analyzing systems.

Localized **A**nharmonic **V**ibrations (**LAV**s) A. Ovchinnikov (1969)

Two coupled anharmonic oscillators

$$\ddot{x}_1 + \omega_0^2 x_1 + \varepsilon \lambda x_1^3 = \varepsilon \beta x_2$$

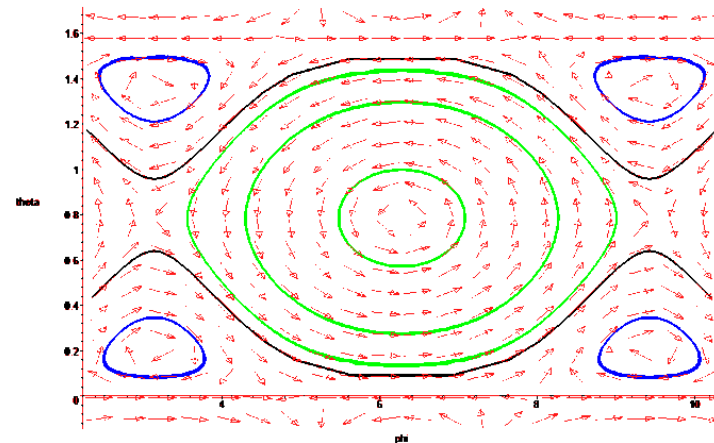
$$\ddot{x}_2 + \omega_0^2 x_2 + \varepsilon \lambda x_2^3 = \varepsilon \beta x_1$$

$$\tau = \frac{\omega_0}{\varepsilon \beta} \int_0^{\pi/2} \frac{d\eta}{\sqrt{1 - \left(\frac{3A_0 \lambda}{4\beta} \right)^2 \sin^2 \eta}}$$

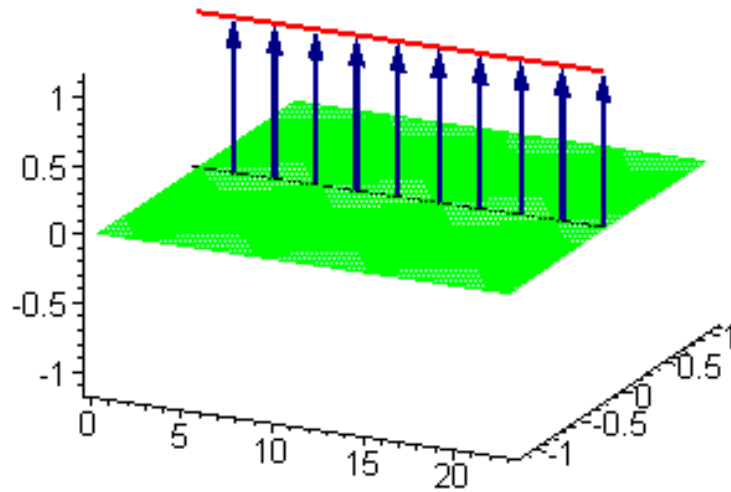
Localization condition

$$A_0 > \frac{4\beta}{3\lambda} \Rightarrow \tau \rightarrow \infty$$

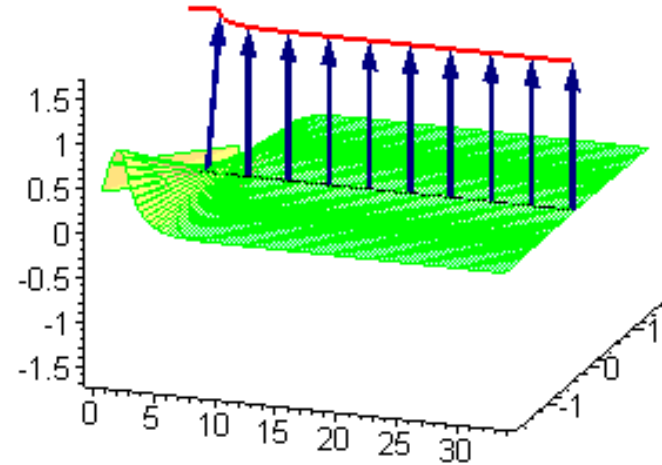
Phase diagram



Discrete Breathers

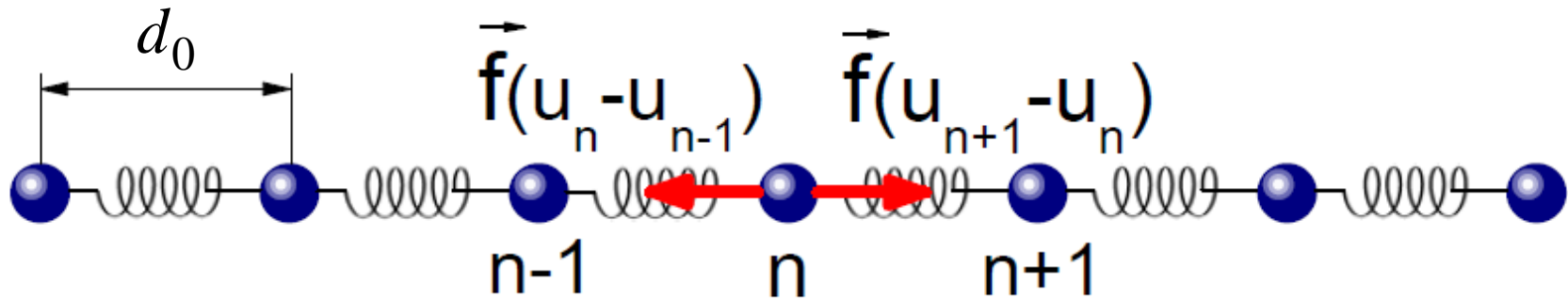


Sine-Gordon standing breather is a swinging in time coupled kink-antikink 2-soliton solution.



Large amplitude moving sine-Gordon breather.

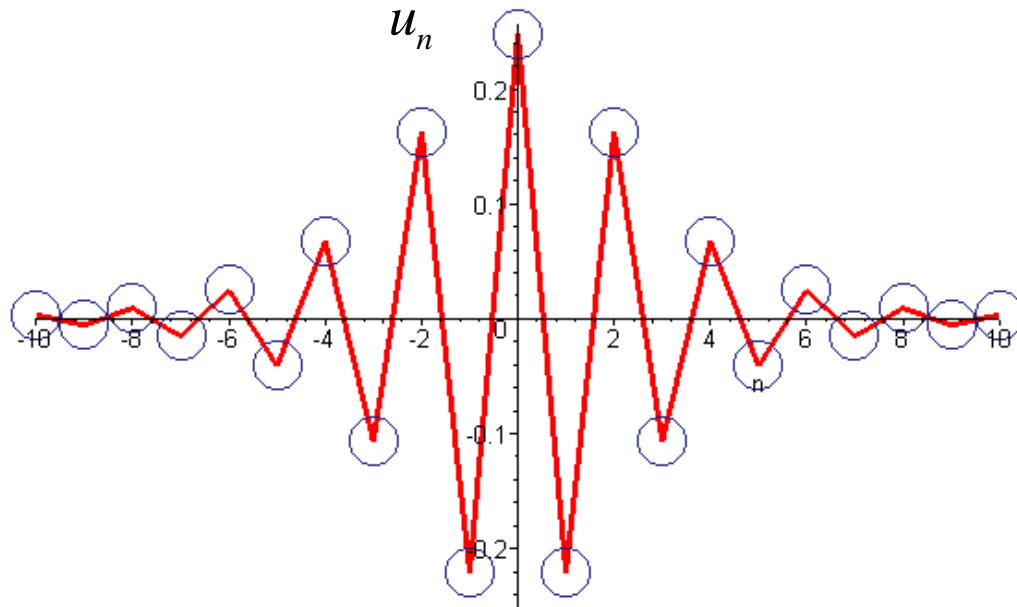
1D crystal — Hirota lattice model (nonlinear telegraph equations, 1973)



Equation of motion of Hirota lattice

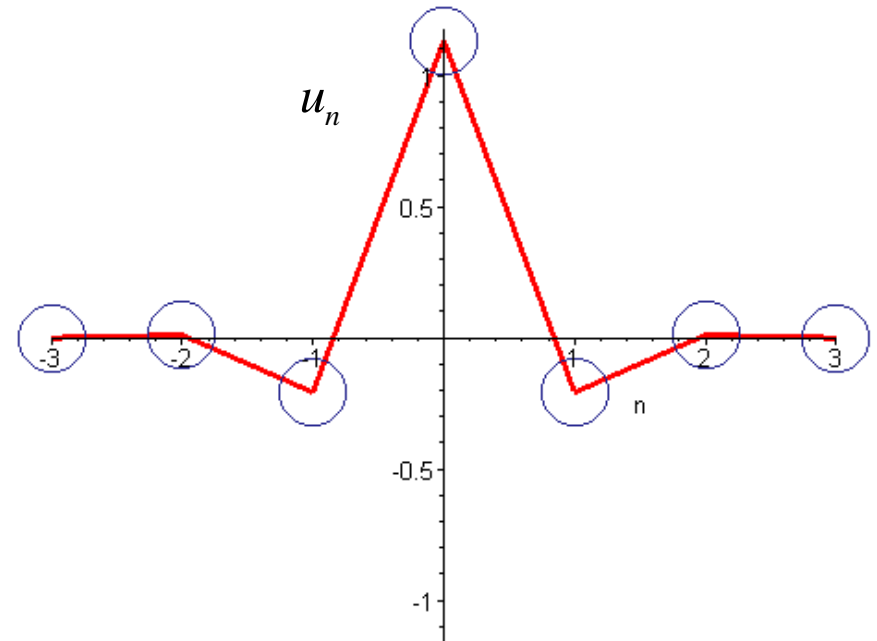
$$\frac{m\ddot{u}_n}{1 + \frac{\pi^2}{4} \frac{\dot{u}_n^2}{s^2}} = \frac{2}{\pi} \gamma d_0 \left\{ \operatorname{tg} \left[\frac{\pi}{2} \left(\frac{u_{n-1} - u_n}{d_0} \right) \right] - \operatorname{tg} \left[\frac{\pi}{2} \left(\frac{u_n - u_{n+1}}{d_0} \right) \right] \right\}$$

$$H = \left(\frac{2}{\pi} \right)^2 ms^2 \sum_{n=-\infty}^{+\infty} \left\{ \frac{1}{2} \ln \left[1 + \operatorname{tg}^2 \left(\frac{\pi}{2} \frac{p_n}{ms} \right) \right] + \frac{1}{2} \ln \left[1 + \operatorname{tg}^2 \left(\frac{\pi}{2d_0} (u_{n-1} - u_n) \right) \right] \right\}$$



Standing **weakly localized** DB

Bogdan, 2002

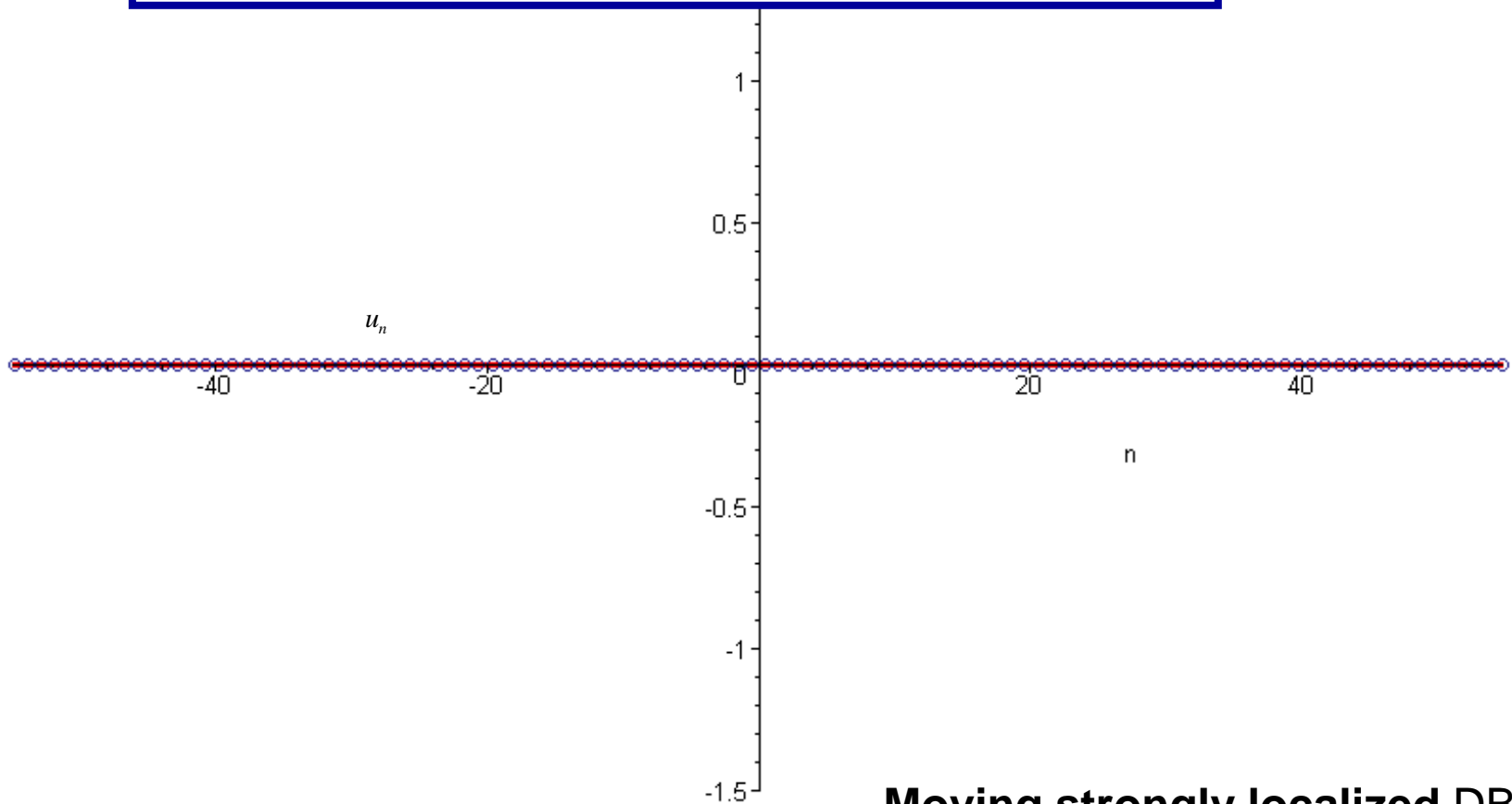


Standing **strongly localized** DB

$$u_n^{(b)} = \frac{2d_0}{\pi} \operatorname{arctg} \left[\frac{\operatorname{sh}(\kappa d_0/2)}{\sin(kd_0/2)} \frac{\cos(knd_0 - \omega t)}{\operatorname{ch} \kappa(nd_0 - Vt)} \right],$$

Bogdan, 2002

$$\omega = \frac{s}{d_0} 2 \operatorname{ch} \left(\frac{\kappa d_0}{2} \right) \sin \left(\frac{kd_0}{2} \right), \quad V = s \frac{\operatorname{sh}(\kappa d_0/2)}{\kappa d_0/2} \cos \left(\frac{kd_0}{2} \right).$$



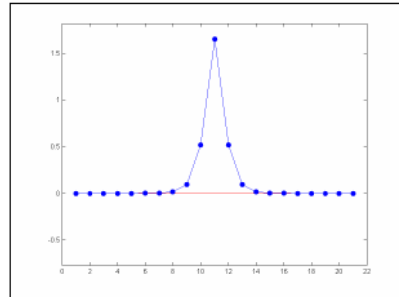
Moving strongly localized DB

Nonlinear coupled oscillators



$$V = \sum V(X_n) + C W(X_n, X_{n+1})$$

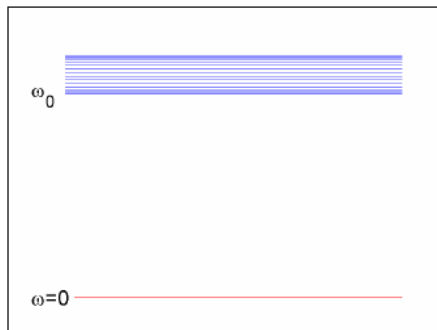
- Exact, periodic and localized solution



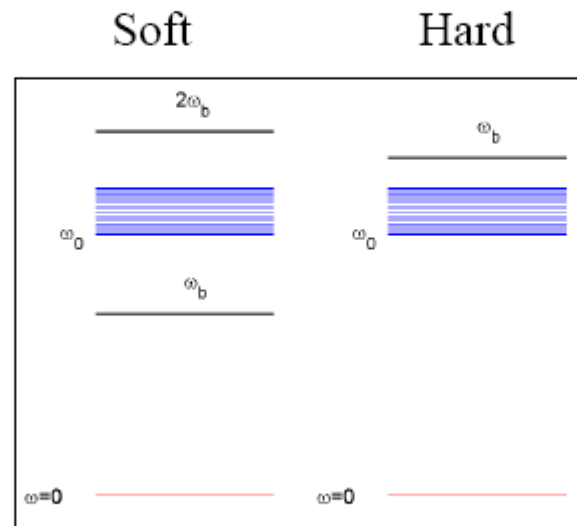
The concept of **LAV** in regular lattices is based on *large anharmonic* atomic oscillations in **Discrete Breathers** excited *outside the phonon bands*.

Phonons

- Frequency band $\omega_{ph}^2 = \omega_0^2 + 4C \sin^2 q/2$
- Non localized states



Existence of breathers (1994)



$$n \omega_b \notin [\omega_0, \omega_{f, \max}], \quad \omega_b'(E) \neq 0$$

DBs in metals Hizhnyakov et al (2011)

PREDICTION OF HIGH-FREQUENCY INTRINSIC ...

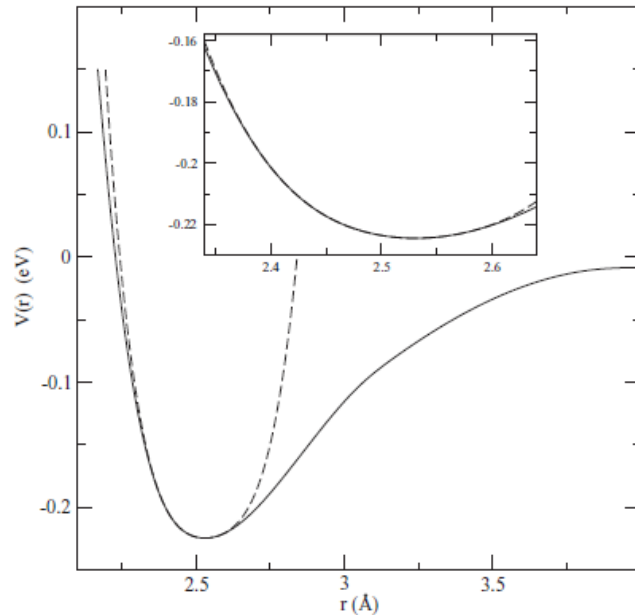


FIG. 1. The pair potential $V(r)$ of Ni (solid line) and its approximation by the fourth-order polynomial (dashed line). The inset shows an expanded view.

The distance between the nearest atoms in Ni at room temperature is $r_0 = 2.49 \text{ Å}$ and longitudinal sound velocity is $v_l = 5266 \text{ m/s}$. These values give $\tilde{K}_2 = 2.75 \text{ eV/Å}^2$ (as expected, $\tilde{K}_2 > K_2$) and $\tilde{\kappa} \approx 1.2$. The distance r_0 increases

HAAS, HIZHNYAKOV, SHELMAN, KLOPOV, AND SIEVERS

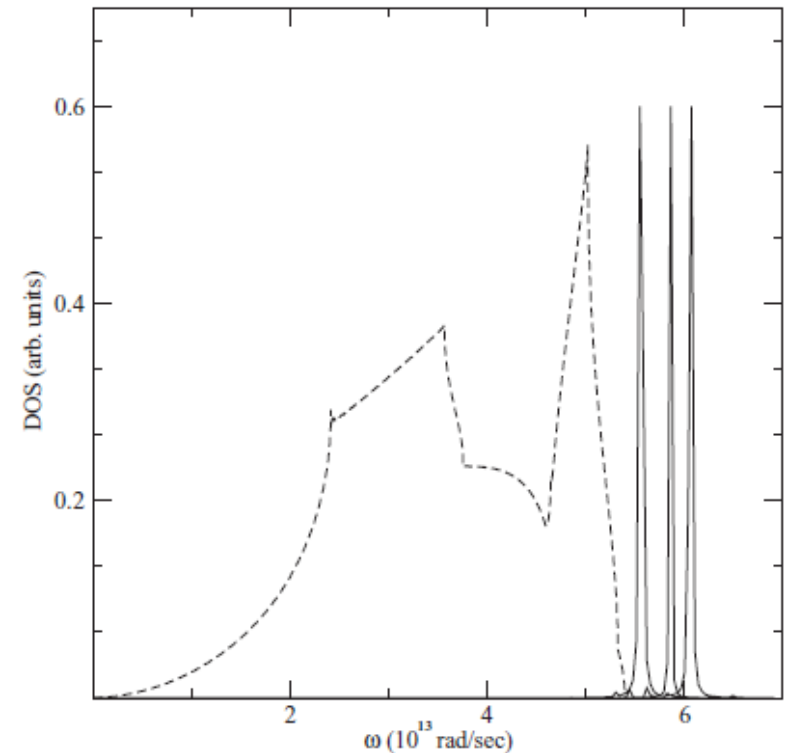
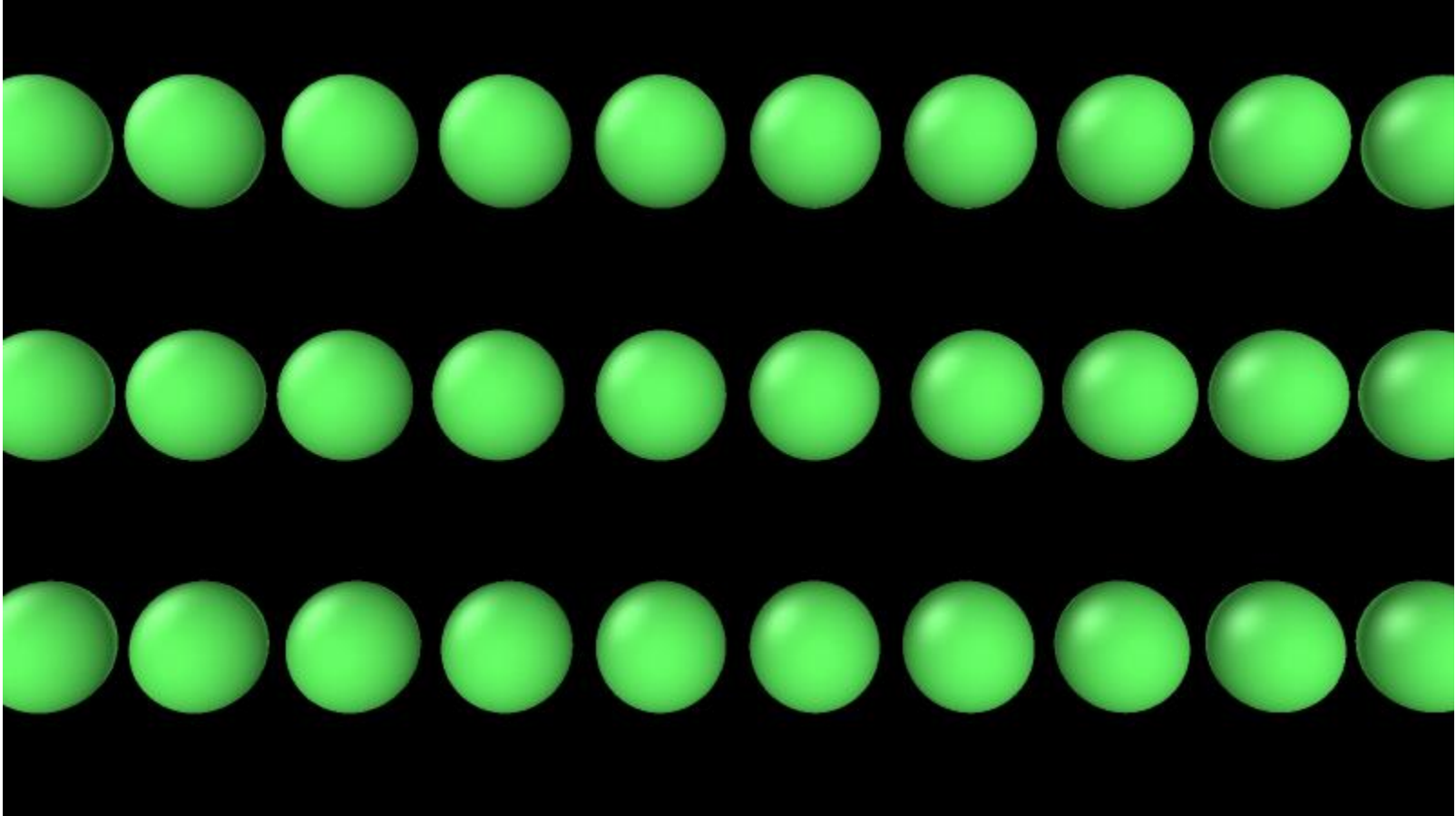
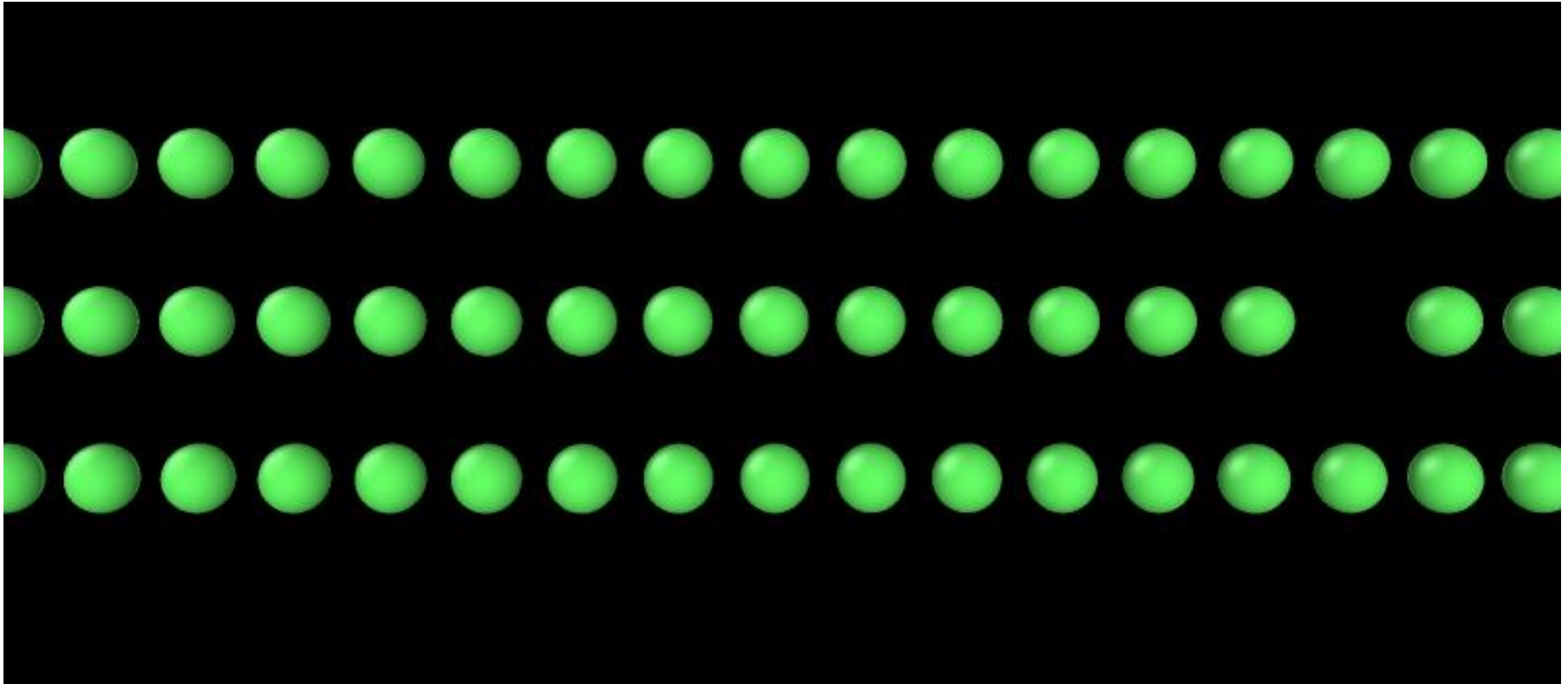


FIG. 2. Phonon density of states and three ILM spectral signatures for Ni. Phonon spectrum (dashed line) and spectrographs (solid line) of the different ILM's: The frequencies are 5.58, 5.86, and 6.07 (10^{13} rad/s) and the amplitudes of vibrations of the central bond are 0.18, 0.31, and 0.42 Å.

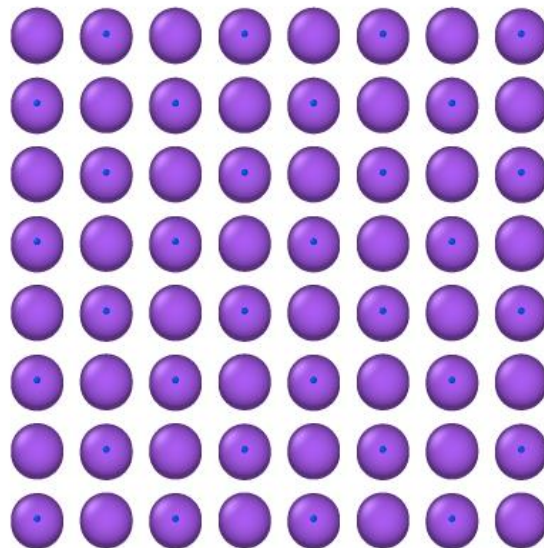
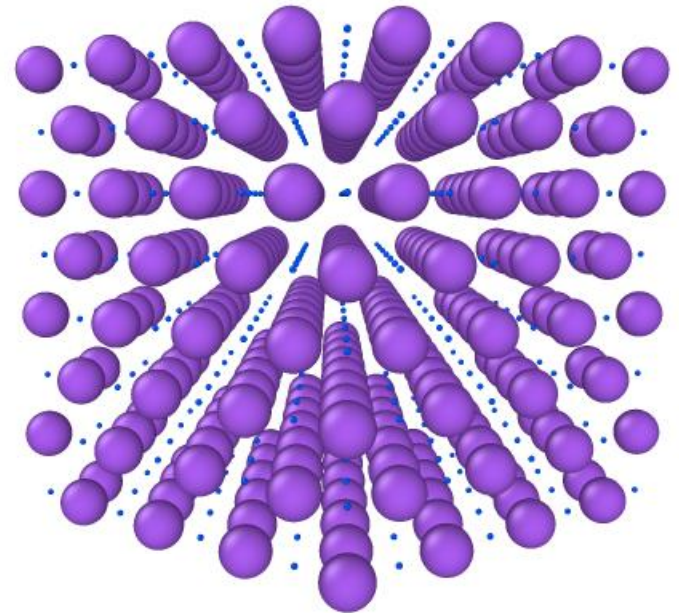
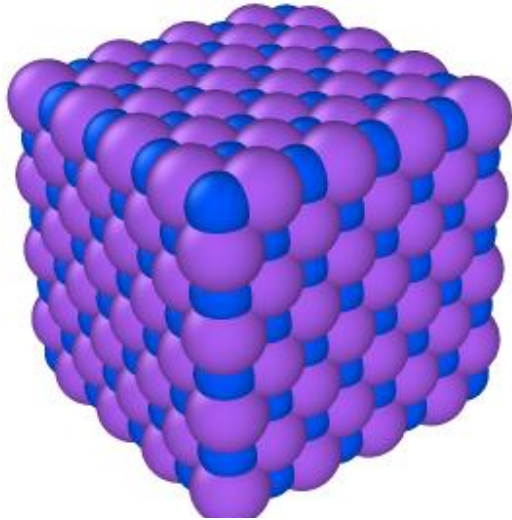
Standing DB in bcc Fe: $d_0=0.3 \text{ \AA}$
D.Terentyev, V. Dubinko, A. Dubinko (2013)



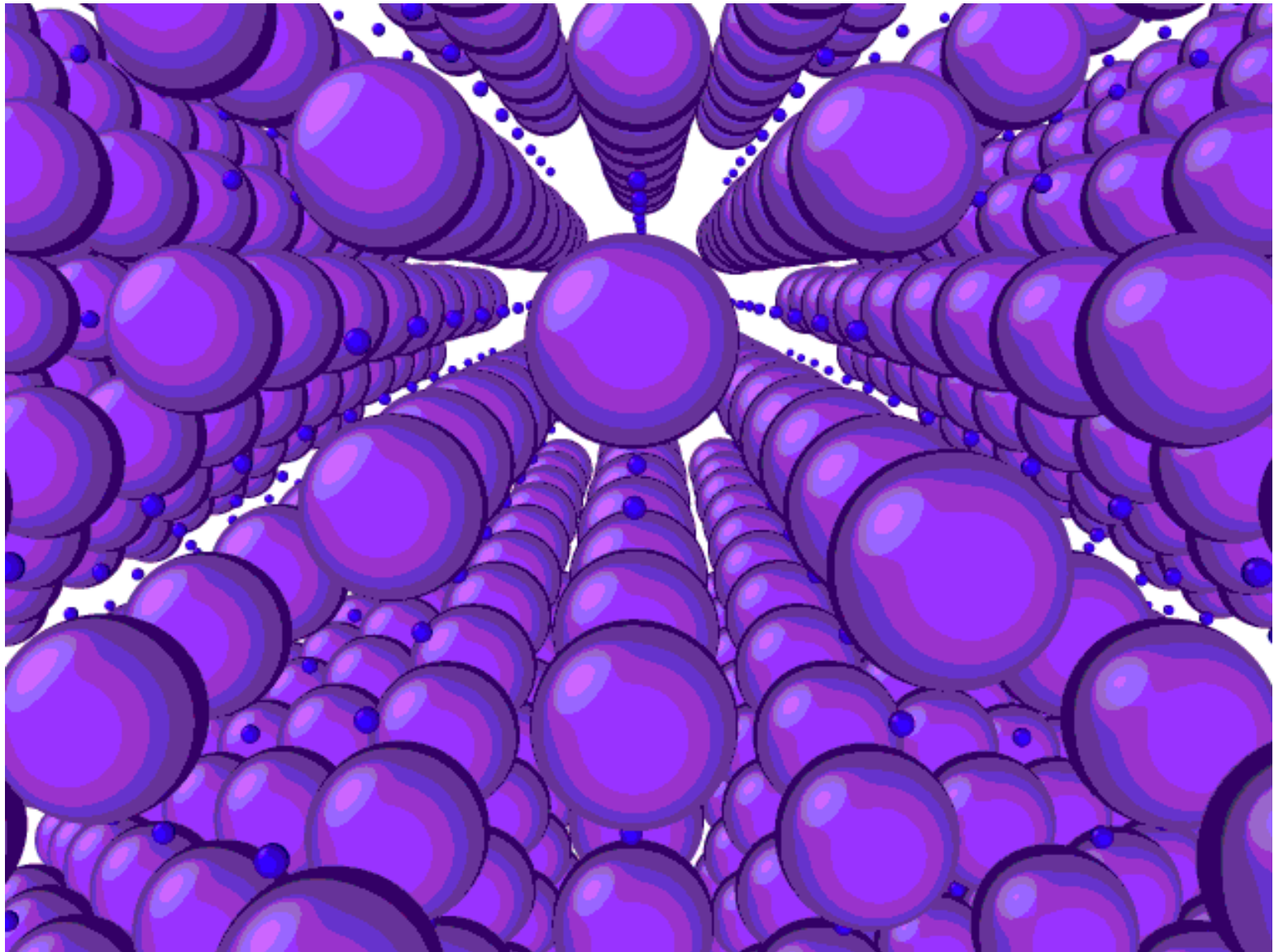
Moving DB in bcc Fe: $d_0=0.4$ Å, $E=0.3$ eV
D.Terentyev, V. Dubinko, A. Dubinko (2013)



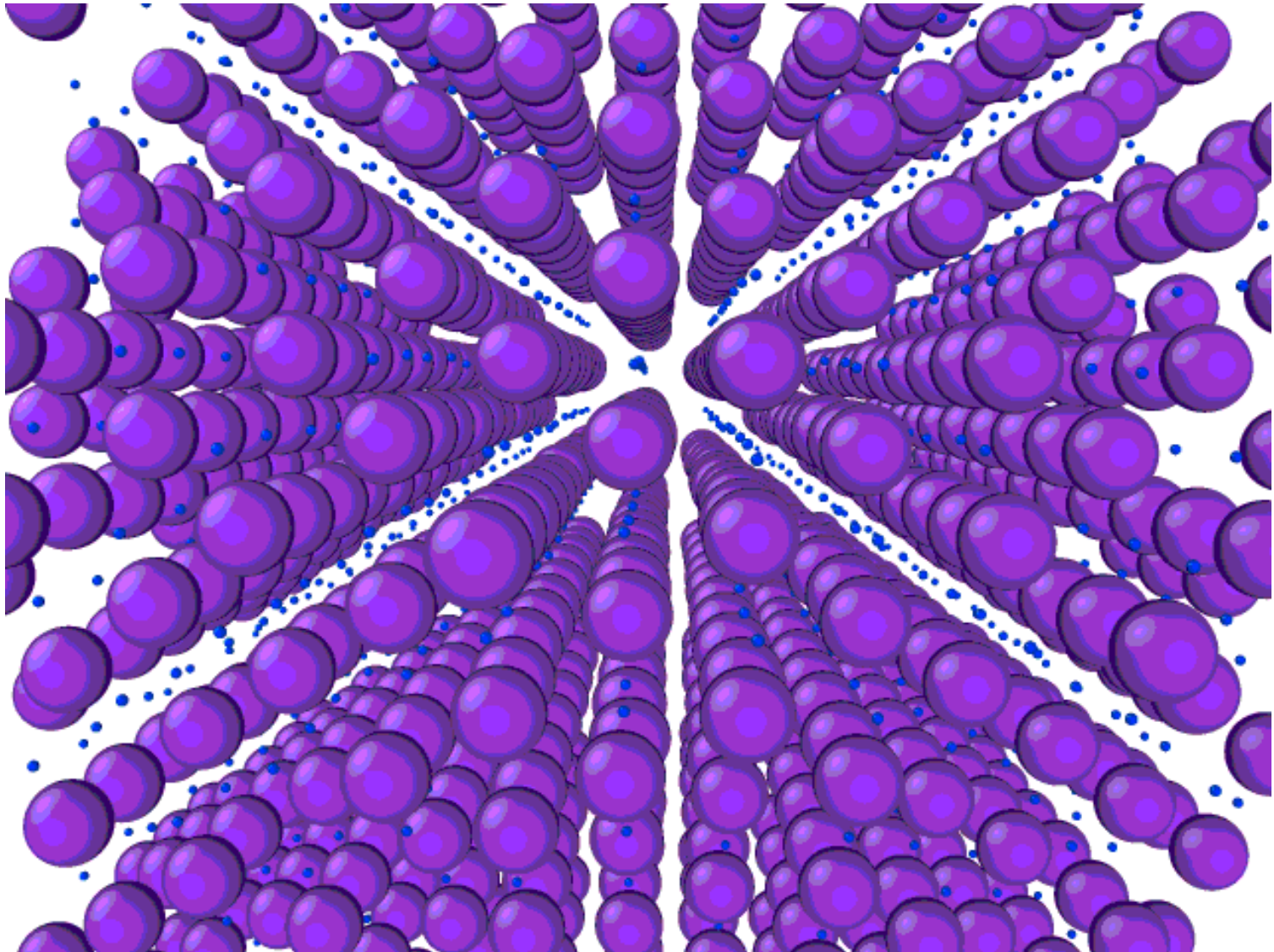
Visualization of the PdH fcc Lattice (NaCl type)



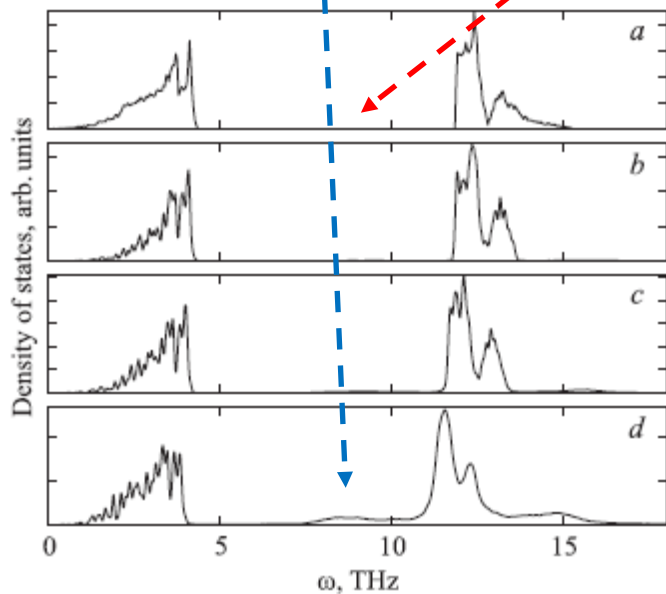
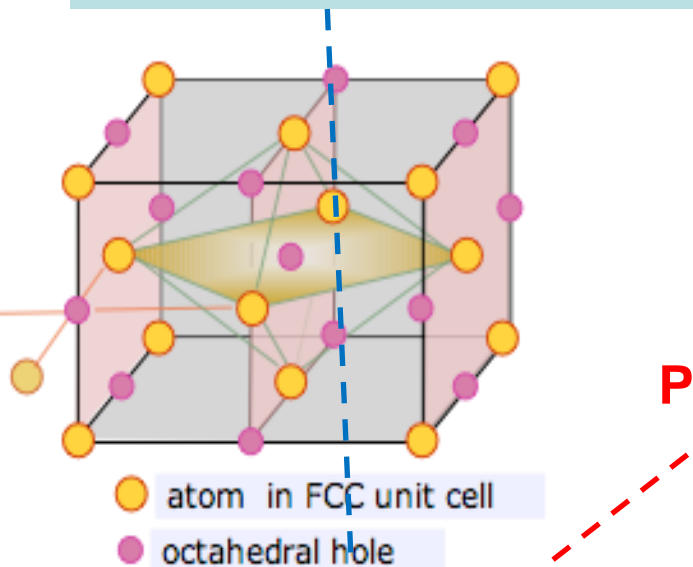
Visualization of the PdH fcc Lattice Oscillations at $T=100$ K



Visualization of the PdH fcc Lattice Oscillations at $T=1000\text{K}$

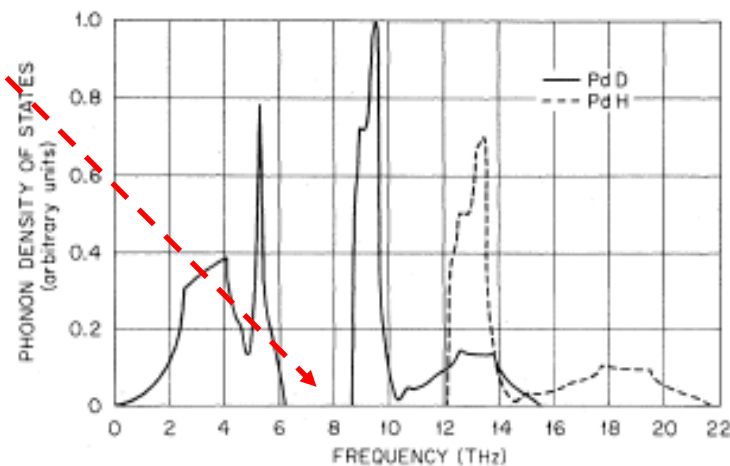
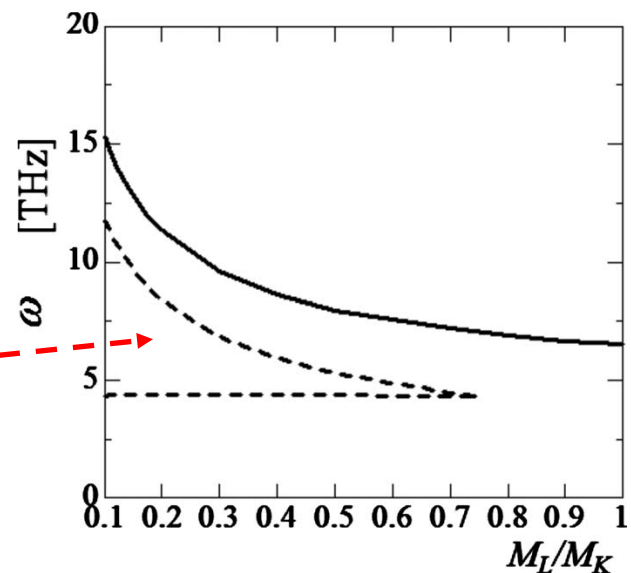


Gap breathers in NaCl type lattices, Dmitriev et al (2010)



NaCl-type $M_H/M_L = 10$ at temperatures $T = (a) 0, (b) 155, (c) 310, \text{ and } (d) 620 \text{ K}$

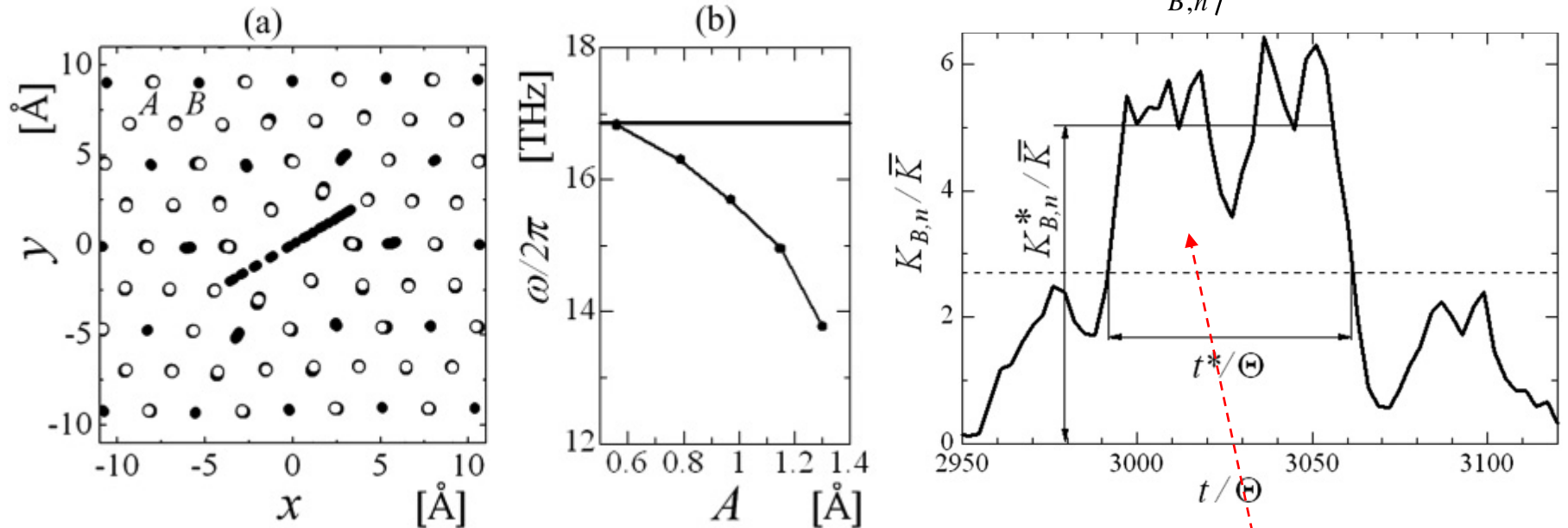
Phonon Gap



DOS for **PdD_{0.63}** and **PdH_{0.63}**: $M_H/M_L = 50; 100$
D pressure of 5 GPa and $T = 600 \text{ K}$

MD modeling of gap DBs in diatomic crystals at elevated temperatures

Hizhnyakov et al (2002), Dmitriev et al (2010)



A_3B type crystals $M_H/M_L = 10$

$t^*/\Theta \approx 70$ $\bar{K} = 0.1 \text{ eV} \geq 1000 \text{ K}$

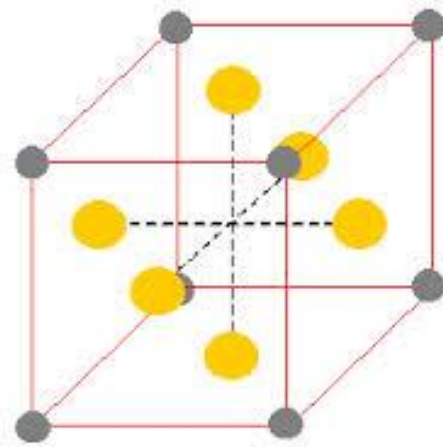
In NaI and KI crystals Hizhnyakov et al has shown that DB amplitudes along $\langle 111 \rangle$ directions can be as high as 1 \AA , and $t^*/\Theta \sim 10^4$

ICCF19

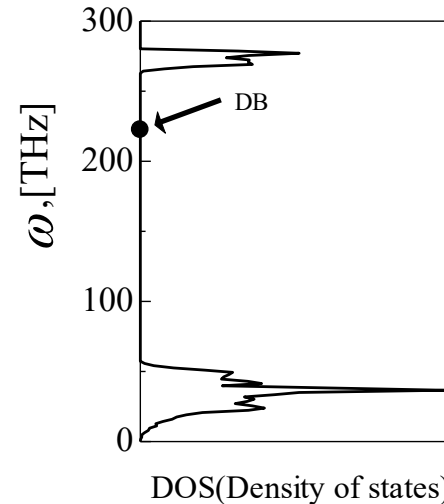
Lifetime and concentration of **high-energy light atoms** increase exponentially with increasing T

MD modeling of gap DBs in diatomic crystals at elevated temperatures

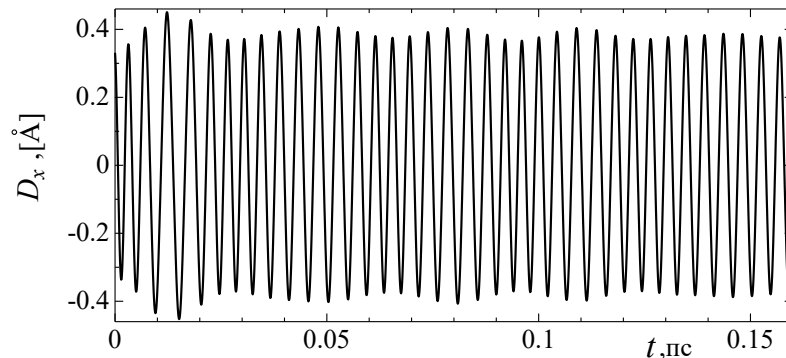
A_3B type crystals, Kistanov, Dmitriev (2014),



A_3B compound based on fcc lattice with Morse interatomic potentials. Grey atoms are **50 times lighter** than yellow (similar to the PdD crystal).

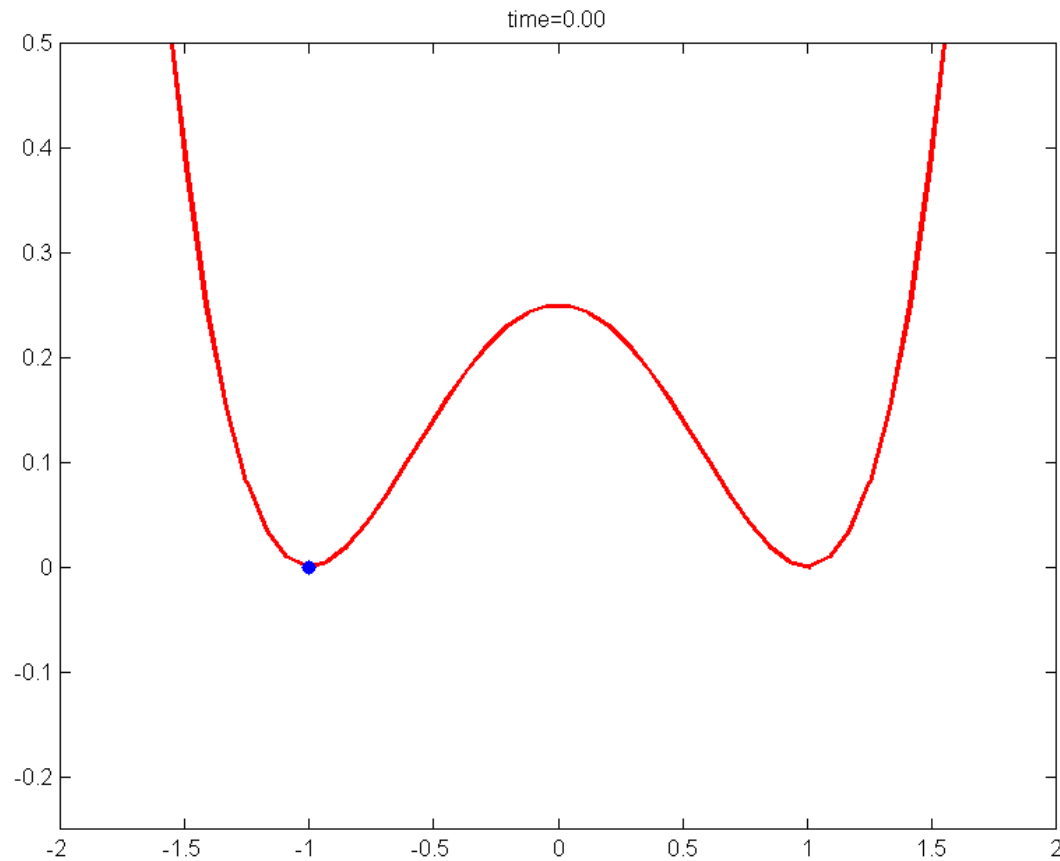


DOE of a A_3B compound
with $M_H / M_L = 50$



DB is localized on a **single light atom** vibrating along **<100> direction** with the frequency of **227 THz**, which is **inside the phonon gap**. Shown is the x-displacement of the light atom as the function of time. DB has very large amplitude of **0.4 angstrom**, which should be compared to the lattice parameter **$a=1.35$ angstrom**

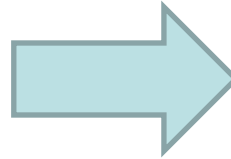
LAV effect (1): periodic in time modulation of the potential barrier height



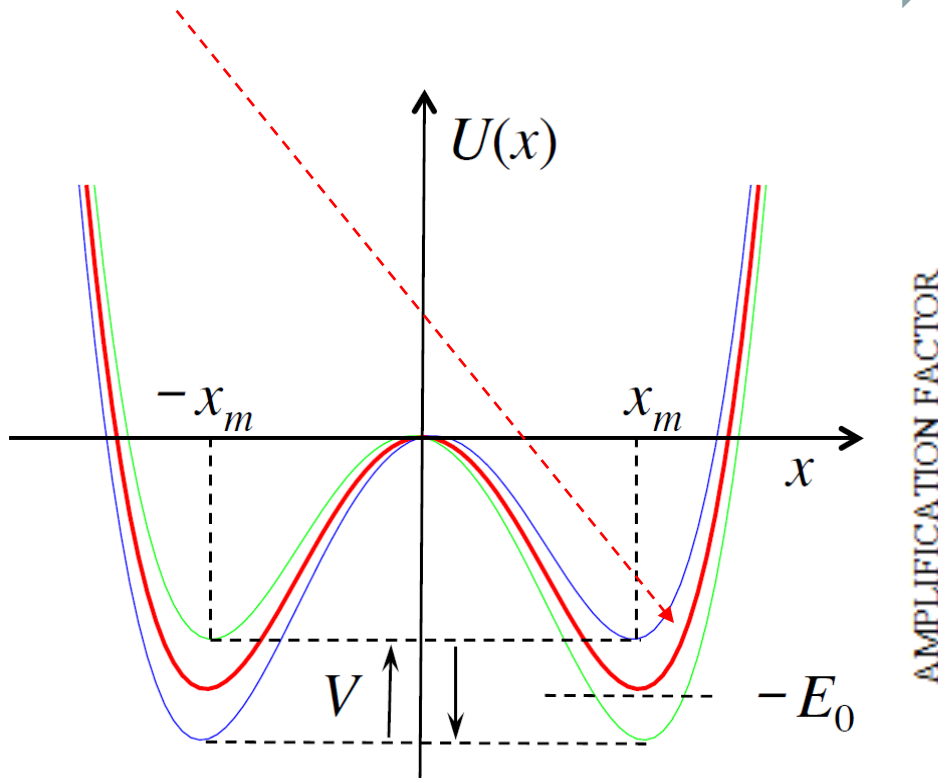
Reaction-rate theory with account of the crystal anharmonicity

Dubinko, Selyshchev, Archilla, Phys. Rev. E. (2011)

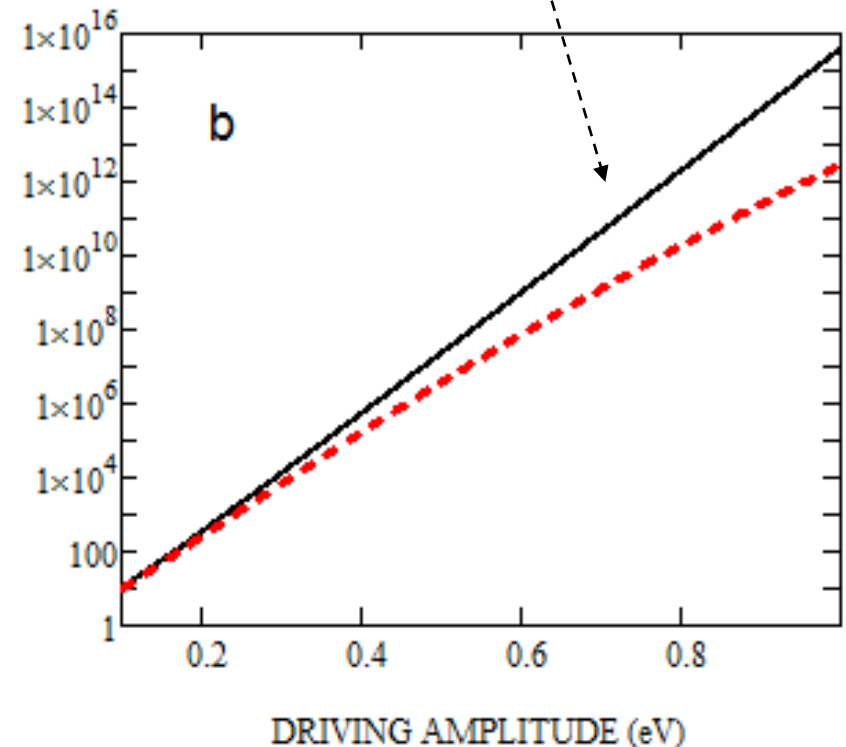
$$U(x, t) = U(x) - (V \cdot x/x_m) \cos(\Omega t)$$



Kramers rate is amplified:
Bessel function $I_0(V_m/k_B T)$



AMPLIFICATION FACTOR



**How extend LAV concept
to include**

**Quantum effects,
Tunneling**

?

Tunneling as a classical escape rate induced by the vacuum zero-point radiation, [A.J. Faria](#), [H.M. Franca](#), [R.C. Sponchiado](#) Foundations of Physics (2006)

The Kramers theory is extended in order to take into account the action of the thermal and **zero-point oscillation (ZPO)** energy.

$$R_K = \frac{\omega_0}{2\pi} \exp[-E_0/D(T)]$$

$$D(T) = E_{ZPO} \coth(E_{ZPO}/k_B T) \approx \begin{cases} E_{ZPO}, & T \rightarrow 0 \\ k_B T, & T \gg E_{ZPO}/k_B \end{cases}$$

T – temperature is a measure of *thermal* noise strength

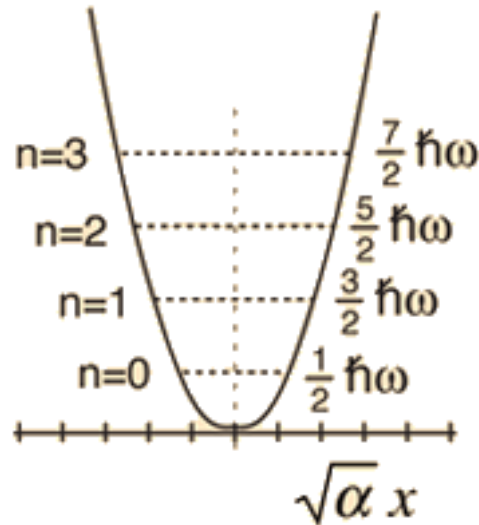
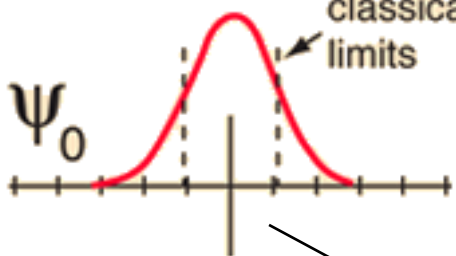
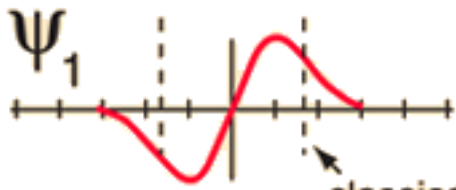
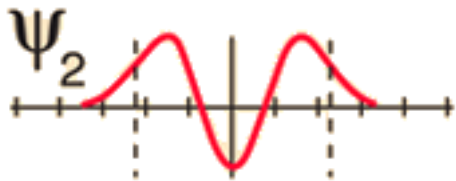
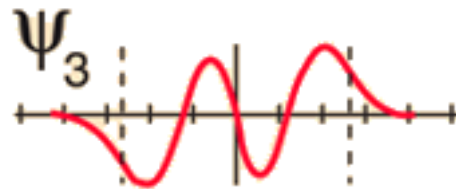
$$E_{ZPO} = \frac{\hbar \omega_0}{2} \quad - \text{ZPO energy is a measure of } \textit{quantum} \text{ noise strength}$$

When we heat the system we increase temperature, i.e. we increase the *thermal* noise strength

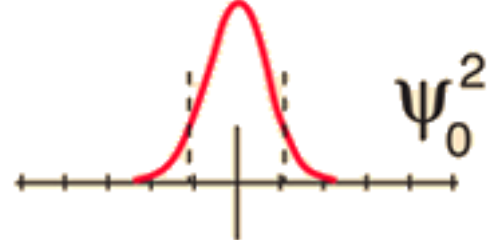
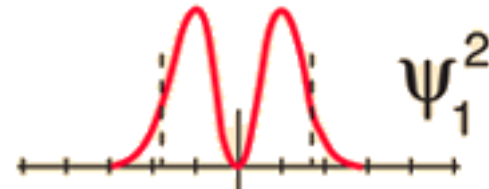
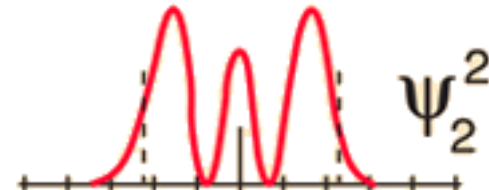
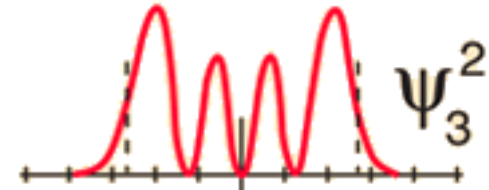
Can we increase the *quantum* noise strength, i.e. ZPO energy?

Stationary harmonic potential

$$\langle E \rangle_n = \hbar \omega_0 \left(n + \frac{1}{2} \right)$$

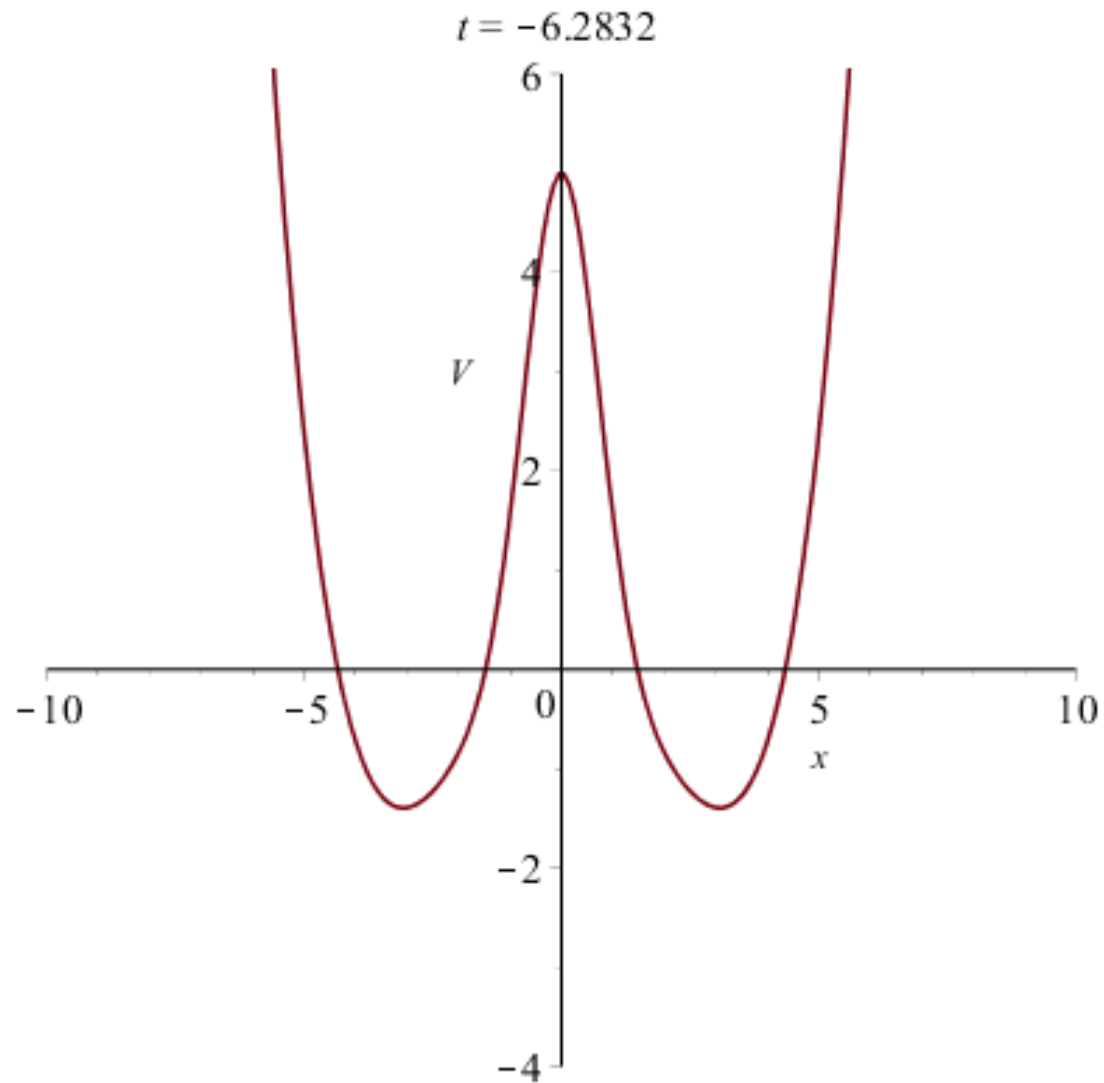


Harmonic oscillator
potential and
wavefunctions



$$E_{ZPO} = \frac{\hbar \omega_0}{2}$$

Time-periodic modulation of the **double-well** shape changes (i) eigenfrequency and (ii) position of the wells



Quasi-energy in time-periodic systems

Consider the Hamiltonian which is periodic in time.

$$i\hbar \frac{\partial \psi}{\partial t} = \hat{H} \psi \qquad \hat{H}(t+T) = \hat{H}(t)$$

It can be shown that Schrodinger equation has class of solutions in the form:

$$\psi_{\alpha}(t+T) = \exp(-i\alpha) \psi_{\alpha}(t)$$

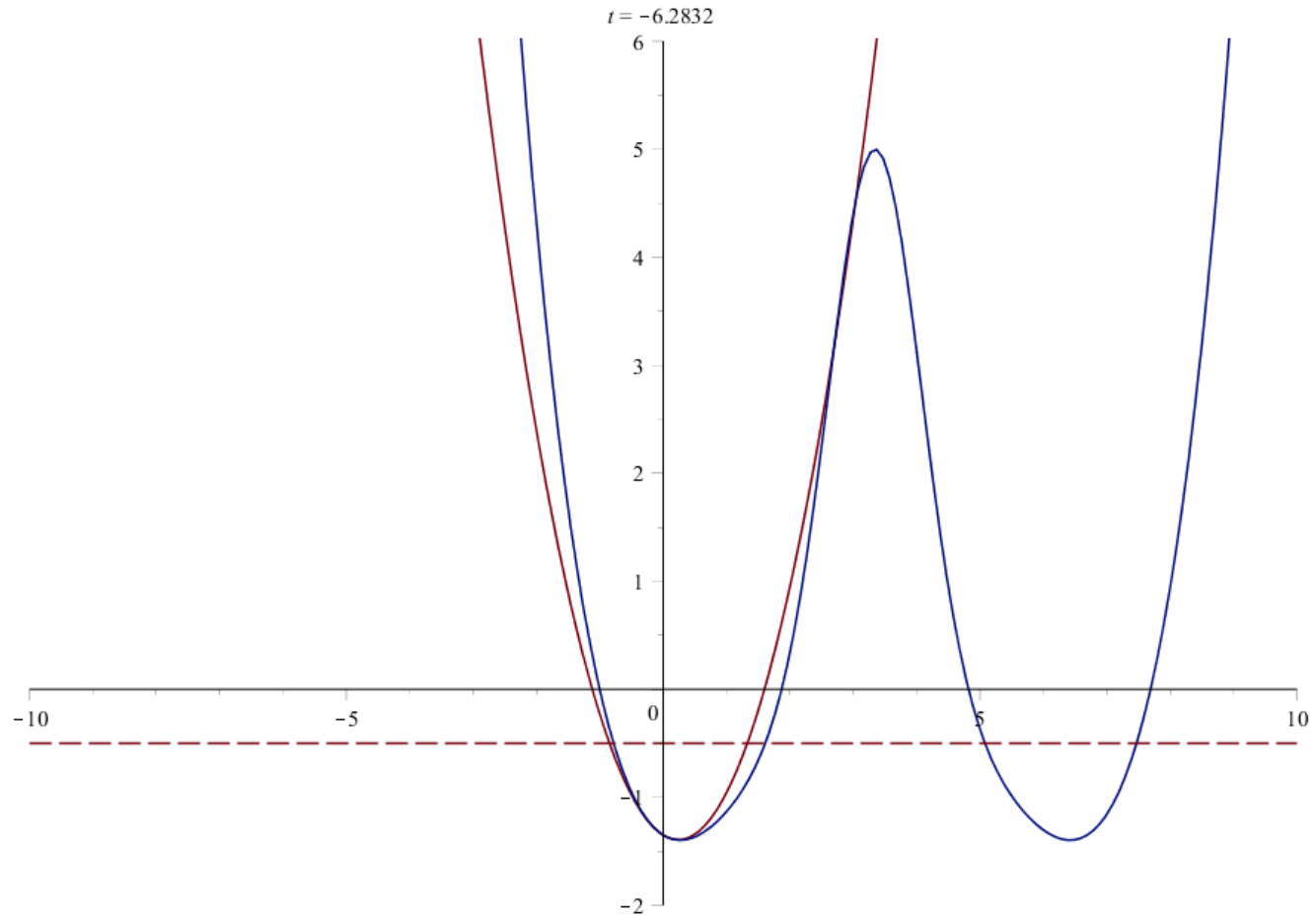
where $\varepsilon = \frac{\hbar \alpha}{T}$ is the quasi-energy

$$i\hbar \frac{\partial}{\partial t} \psi(x,t) = -\frac{\hbar^2}{2m} \frac{\partial^2}{\partial x^2} \psi(x,t) + \frac{m\omega^2(t)}{2} x^2 \psi(x,t)$$

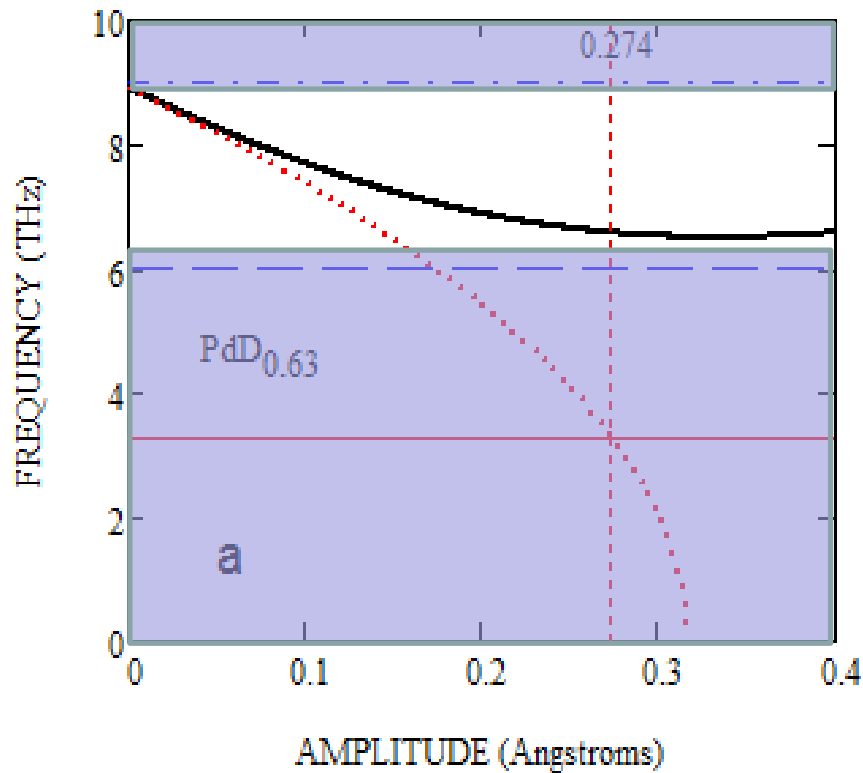
$$\varepsilon_n = \left(n + \frac{1}{2} \right) \lambda(\omega(t))$$

Time-periodic driving of the harmonic oscillator with non resonant frequencies $\Omega \neq 2\omega_0$ renormalizes its energy spectrum, which remains equidistant, but the quasi-energy quantum $\lambda(\omega(t))$ becomes a function of the driving frequency

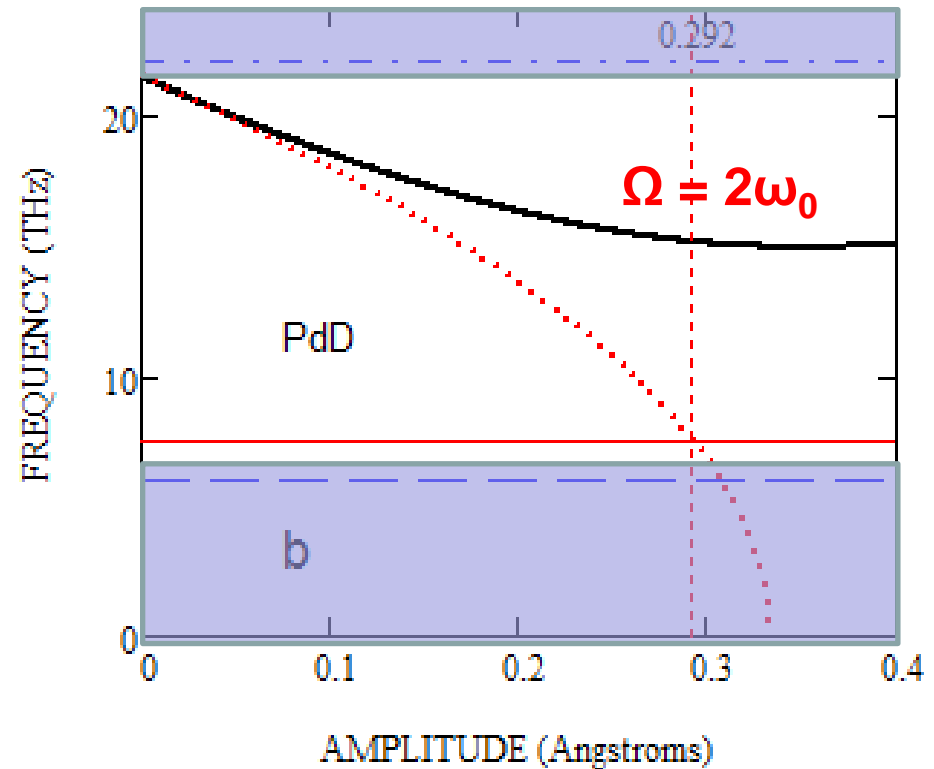
Time-periodic modulation of the double-well shape changes (i) eigenfrequency and (ii) position of the wells



DB frequency and eigenfrequency of the potential wells of neighboring D ions in PdD (Dubinko, ICCF 19)



DB polarized along the close-packed D-D direction $\langle 110 \rangle$



- DB frequency
- Eigenfrequency
- Upper acoustic phonon edge
- - Lower optic phonon edge
- Resonance frequency

Parametric resonance with time-periodic eigenfrequency $\Omega = 2\omega_0$

$$i\hbar \frac{\partial \psi}{\partial t} = -\frac{\hbar^2}{2m} \frac{\partial^2 \psi}{\partial x^2} + \frac{m\omega^2(t)}{2} x^2 \psi$$

Schrödinger equation

$$\psi(x_0, t_0 = 0) = \frac{1}{\sqrt[4]{2\pi\sigma_0}} \exp\left(-\frac{x_0^2}{4\sigma_0}\right)$$

Initial Gaussian packet $\sigma_0 = \frac{\hbar}{2m\omega_0}$

Parametric regime $\Omega = 2\omega_0$: $\ddot{x} + \omega_0^2 [1 - g \cos(2\omega_0 t)] x = 0$

$g \ll 1$ – modulation amplitude

$$\sigma_x(t) = \sigma_0 \cosh\left(\frac{g\omega_0 t}{2}\right) \left[1 + \tanh\left(\frac{g\omega_0 t}{2}\right) \sin(2\omega_0 t) \right] \quad \text{dispersion}$$

ZPO energy:

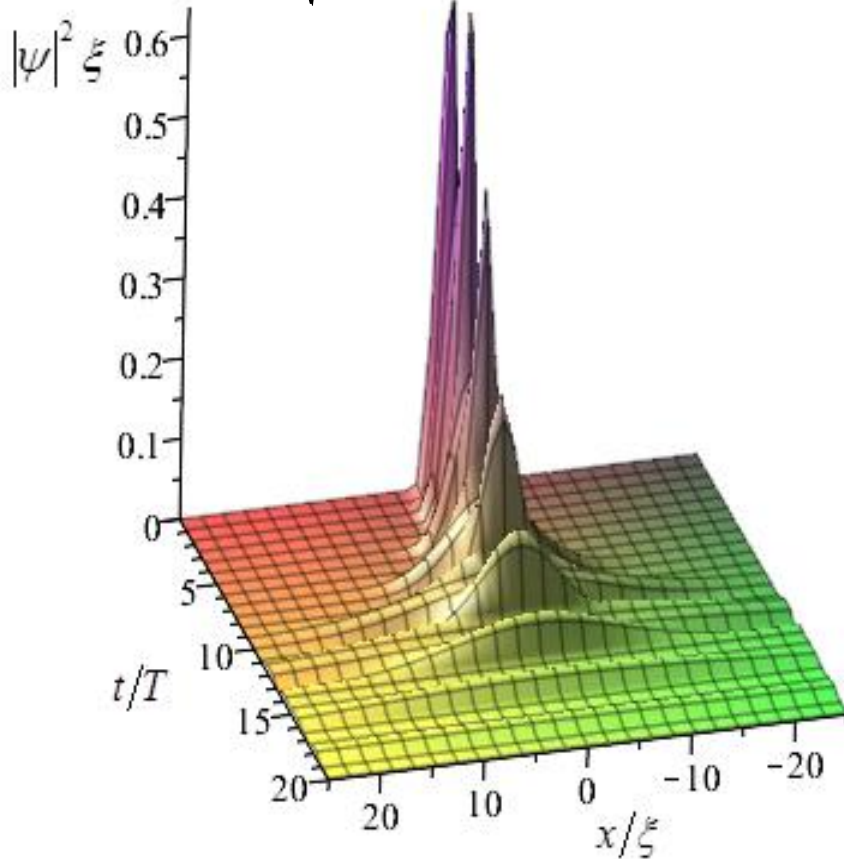
$$E_{ZPO}(t) = \frac{\hbar\omega_0}{2} \cosh \frac{g\omega_0 t}{2}$$

ZPO amplitude:

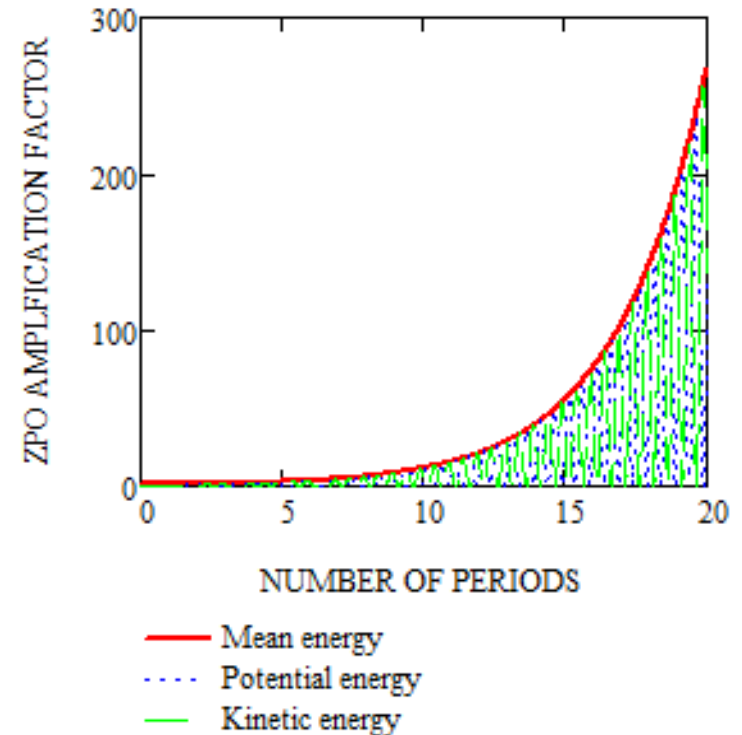
$$\Lambda_{ZPO}(t) = \sqrt{\frac{\hbar}{2m\omega_0} \cosh \frac{g\omega_0 t}{2}}$$

Non-stationary harmonic potential with time-periodic eigenfrequency $\Omega = 2\omega_0$

$$\Lambda_{ZPO}(t) = \sqrt{\frac{\hbar}{2m\omega_0} \cosh \frac{g\omega_0 t}{2}}$$



$$E_{ZPO}(t) = \frac{\hbar\omega_0}{2} \cosh \frac{g\omega_0 t}{2}$$



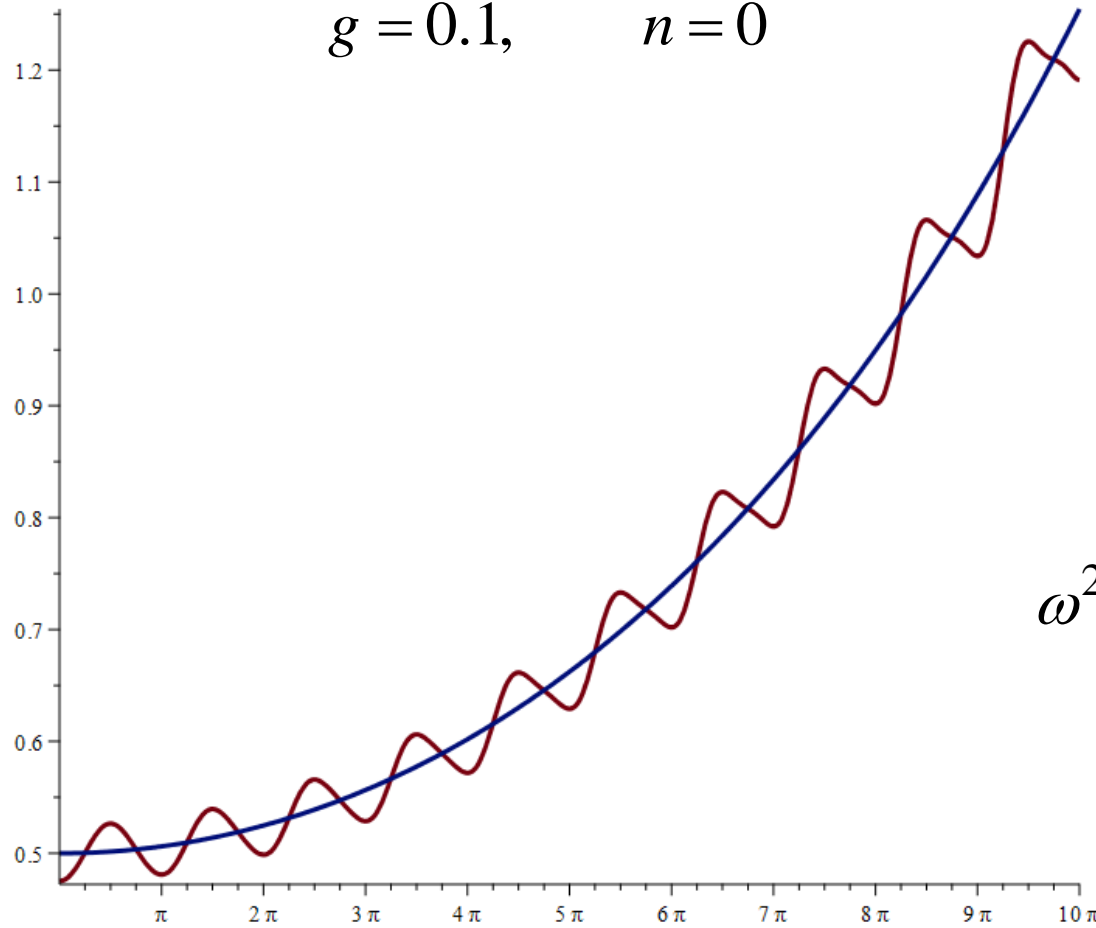
$$\langle E \rangle_{theor}(t) \approx \hbar \omega_0 \left(n + \frac{1}{2} \right) \cosh \frac{g \omega_0 t}{2}$$

$$g \ll 1$$

General case: $n = 0, 1, 2, \dots$

$$\langle E \rangle_{num}(t) = \frac{\hbar \omega_0}{2} \left(n + \frac{1}{2} \right) \left[\frac{\dot{Y}^2 + \omega_0^2 \dot{Z}^2}{\omega_0^2} + \frac{\omega^2(t)}{\omega_0^2} (Y^2 + \omega_0^2 Z^2) \right]$$

$$g = 0.1, \quad n = 0$$



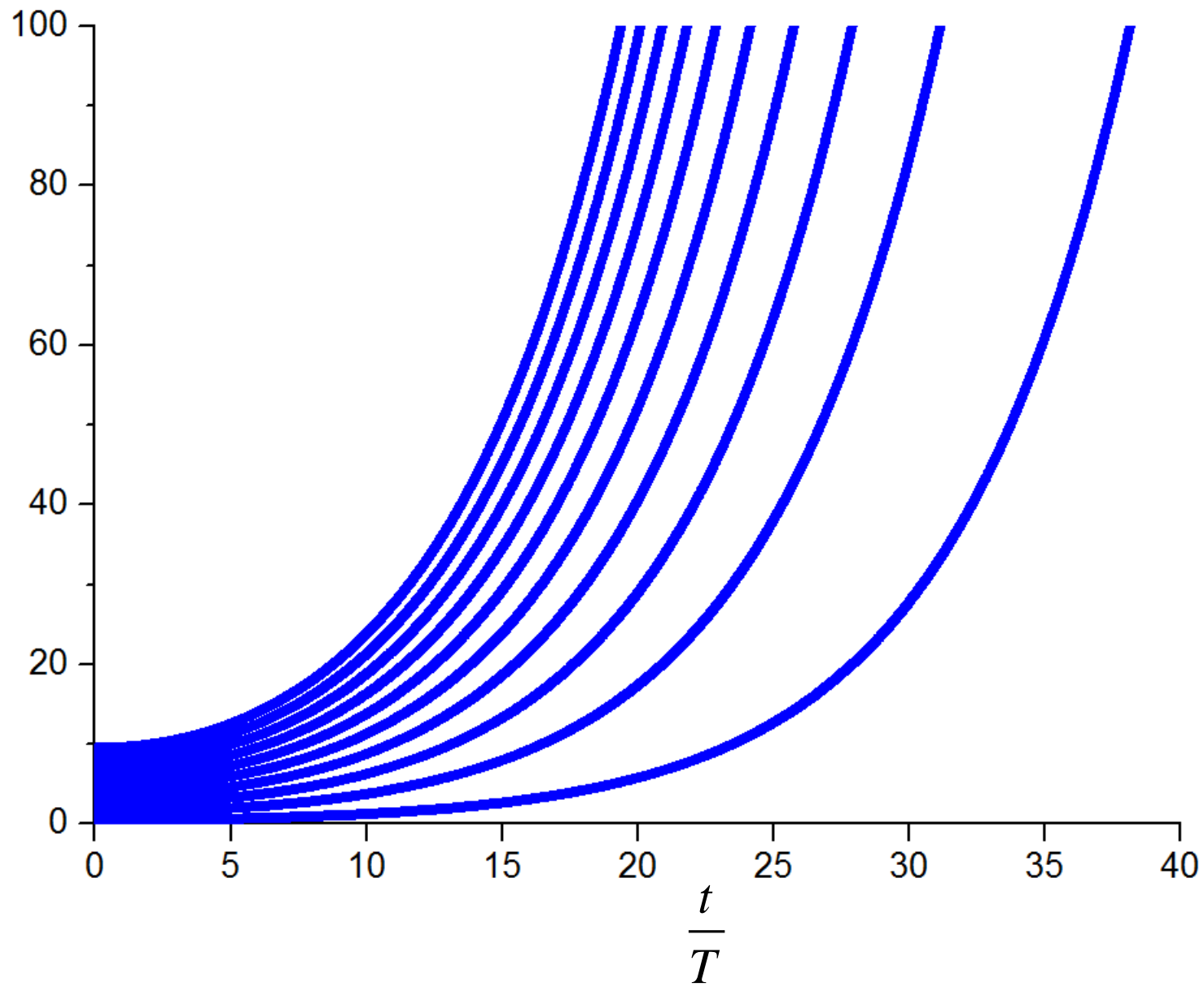
$$\begin{cases} \ddot{Y}(t) + \omega^2(t) Y(t) = 0 \\ \dot{Y}(0) = 0, \quad Y(0) = 1 \end{cases}$$

$$\begin{cases} \ddot{Z}(t) + \omega^2(t) Z(t) = 0 \\ \dot{Z}(0) = 1, \quad Z(0) = 0 \end{cases}$$

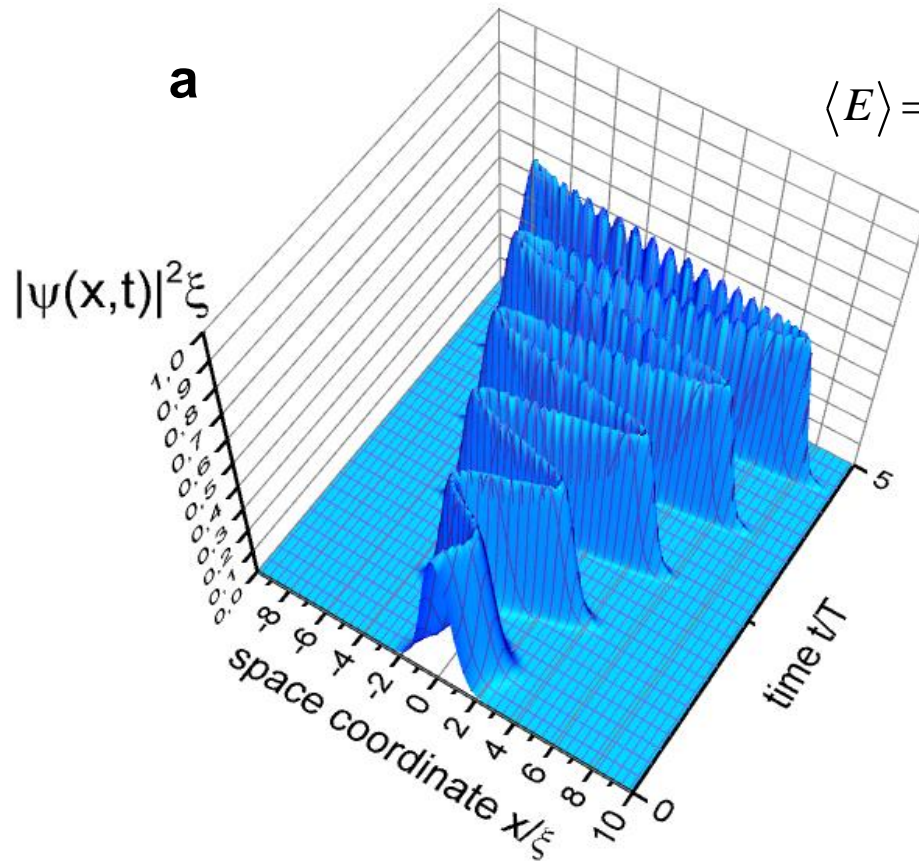
$$\omega^2(t) = \omega_0^2 [1 - g \cos(2\omega_0 t)]$$

$g = 0.1$

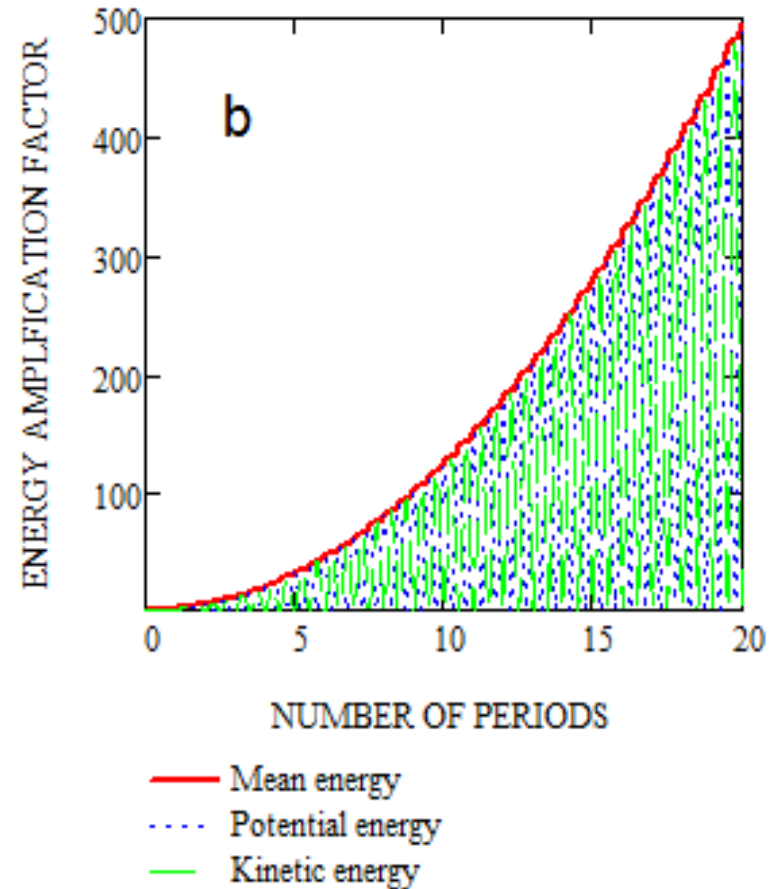
$$\frac{\langle E \rangle_n}{\hbar \omega_0}$$



Non-stationary harmonic potential with time-periodic shifting of the well position at $\Omega = \omega_0$



$$\langle E \rangle = \frac{\hbar\omega_0}{2} + \frac{(g_A A_{ZPO})^2 m\omega_0^2}{8} \left[\omega_0^2 t^2 + \omega_0 t \sin 2\omega_0 t + \sin^2 \omega_0 t \right]$$



$$\lambda(t) = \frac{g_A A_{ZPO}}{2} \omega_0 t \left(\cos \omega_0 t - \frac{\sin \omega_0 t}{\omega_0 t} \right)$$

Well-known and well-forgotten quantum mechanics

W. Heisenberg, “Über den anschaulichen Inhalt der quantentheoretischen Kinematik und Mechanik”, *Z. Phys.*, **43**, 172–198 (1927).

$$\Delta x \Delta p \geq \hbar/2$$

Uncertainty Relations (UR)
Heisenberg (1927)

E. Schrödinger, “Zum Heisenbergschen Unschärfeprinzip”, *Ber. Kgl. Akad. Wiss. Berlin*, **24**, 296–303 (1930).

H. P. Robertson, “A general formulation of the uncertainty principle and its classical interpretation”, *Phys. Rev.*, **35**, 667 (1930).

$$\sigma_x \sigma_p - \sigma_{xp}^2 \geq \hbar^2/4,$$

Generalization of the UR
Schrödinger (1930); Robertson (1930)

$$\sigma_x = \langle (x - \langle x \rangle)^2 \rangle$$

$$\sigma_p = \langle (p - \langle p \rangle)^2 \rangle$$

$$\sigma_{xp} = \langle \hat{x}\hat{p} + \hat{p}\hat{x} \rangle / 2 - \langle x \rangle \langle p \rangle.$$

ICCF19

Correlator

GENERALIZED UNCERTAINTY RELATION AND CORRELATED COHERENT STATES

V.V. DODONOV, E.V. KURMYSHEV and V.I. MAN'KO **Phys. Letters (1980)**

$$\sigma_x \sigma_p \geq \frac{\hbar^2}{4(1-r^2)}, \quad \text{Correlation coefficient} \quad \longrightarrow \quad r = \frac{\sigma_{xp}}{\sqrt{\sigma_x \sigma_p}}$$

$$\hbar_{ef} = \frac{\hbar}{\sqrt{1-r^2}}, \quad \text{Effective Plank constant} \quad \hbar_{ef} \xrightarrow{r \rightarrow 1} \infty$$

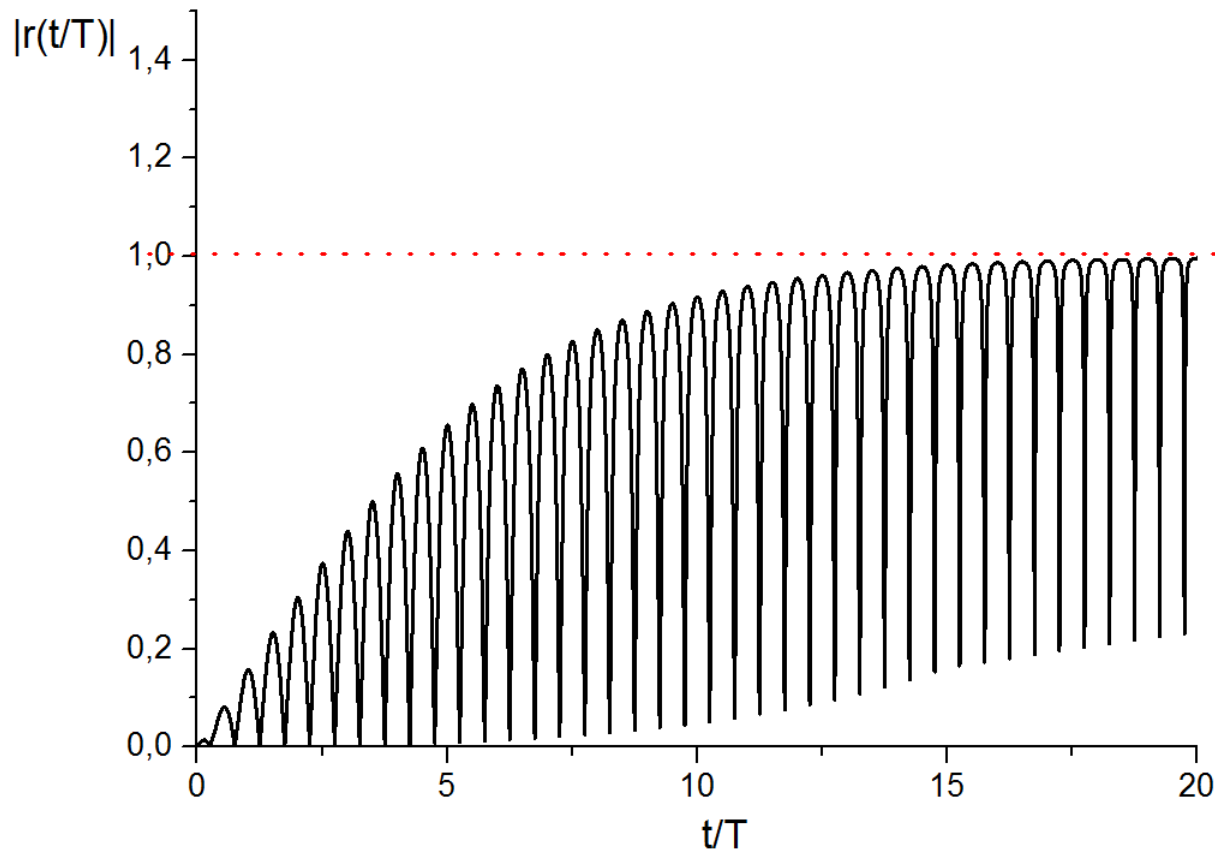
Can CORRELATIONS make the barrier transparent ?!

Vysotskii et al, Eur. Phys. J. A (2013):

$$G_{ef} \approx \exp \left\{ -\frac{2}{\hbar_{ef}} \int_{R_0}^{R_c} dr \sqrt{2\mu(V(r) - E)} \right\} \xrightarrow{r \rightarrow 1, \hbar_{ef} \rightarrow \infty} 1$$

Correlations Coefficient for the parametric resonance $\Omega = 2\omega_0$

$$r_{xp} = r_{xp}(t) = \frac{\sinh\left(\frac{g\omega_0 t}{2}\right) \cos(2\omega_0 t)}{\sqrt{1 + \left[\sinh\left(\frac{g\omega_0 t}{2}\right) \cos(2\omega_0 t)\right]^2}} + O(g)$$

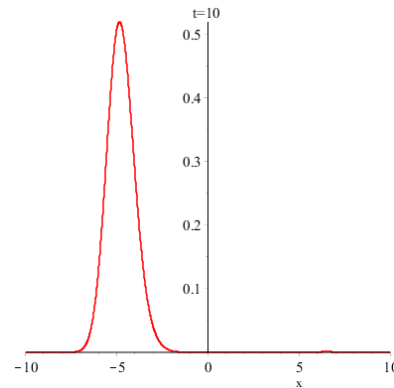
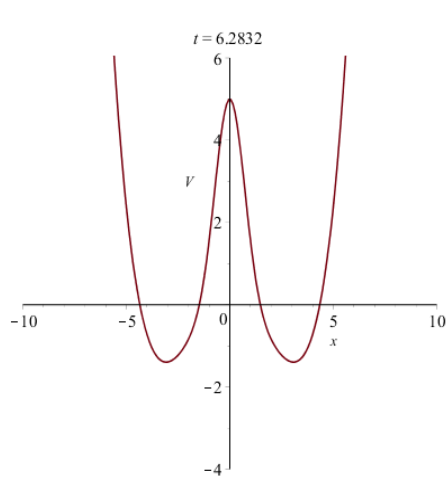


$$g = 0.1$$

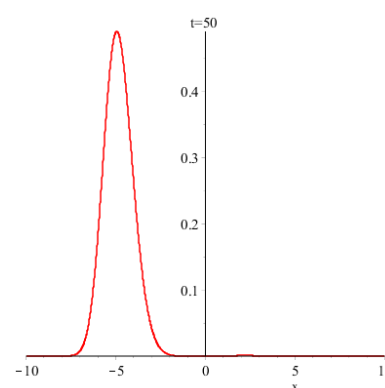
$$T = \frac{2\pi}{2\omega_0}$$

Tunneling: Numerical solution of Schrödinger equation

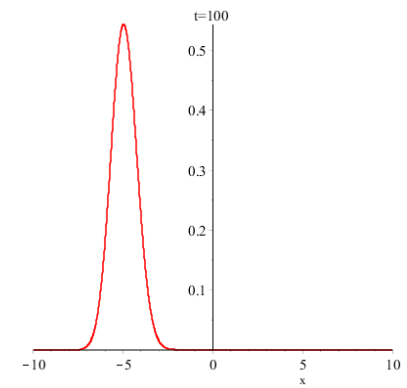
Stationary: $t_{\text{Kramers}} \sim 10^5$ cycles at $V_{\text{barrier}} = 12E_0$



10 cycles

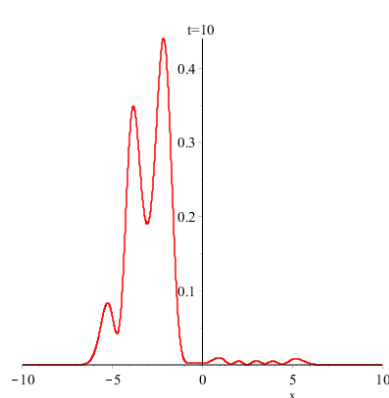
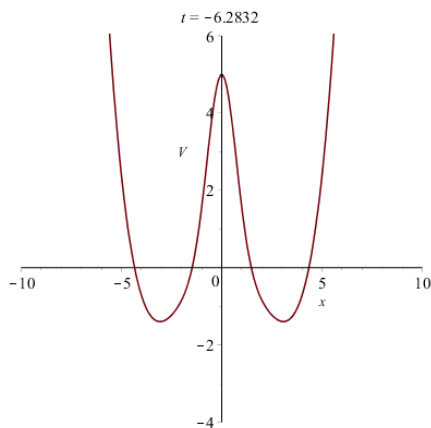


50 cycles

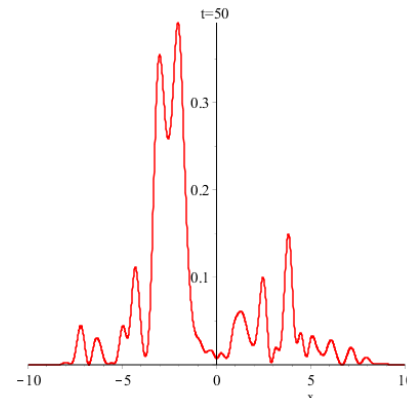


100 cycles

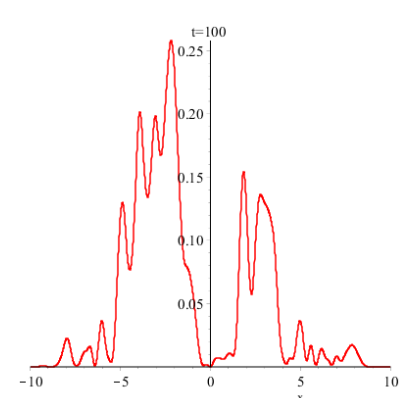
Time-periodically driven: $\Omega = 1.5 \omega_0$, $g = 0.2$



10 cycles



50 cycles



100 cycles

Extreme example – Low Energy Nuclear Reactions (LENR)

Why LENR is unbelievable?

G. Gamow, “Zur Quantentheorie des Atomkernes”, *Z. Phys.*, 51, 204–212 (1928).

$$G \approx \exp \left\{ -\frac{2}{\hbar} \int_{r_0}^{R_c} dr \sqrt{2\mu(V(r) - E)} \right\} \quad \text{Gamow factor}$$

$r_0 \sim 3 \text{ fm}$ Nuclear radius deduced from scattering experiments



$$V(R_0) = \frac{e^2}{r_0} \approx 450 \text{ keV} \quad \Rightarrow \quad \text{Coulomb barrier}$$

At any crystal
Temperature:

$$E \ll V(r_0) \Rightarrow G \approx 10^{-2760}$$

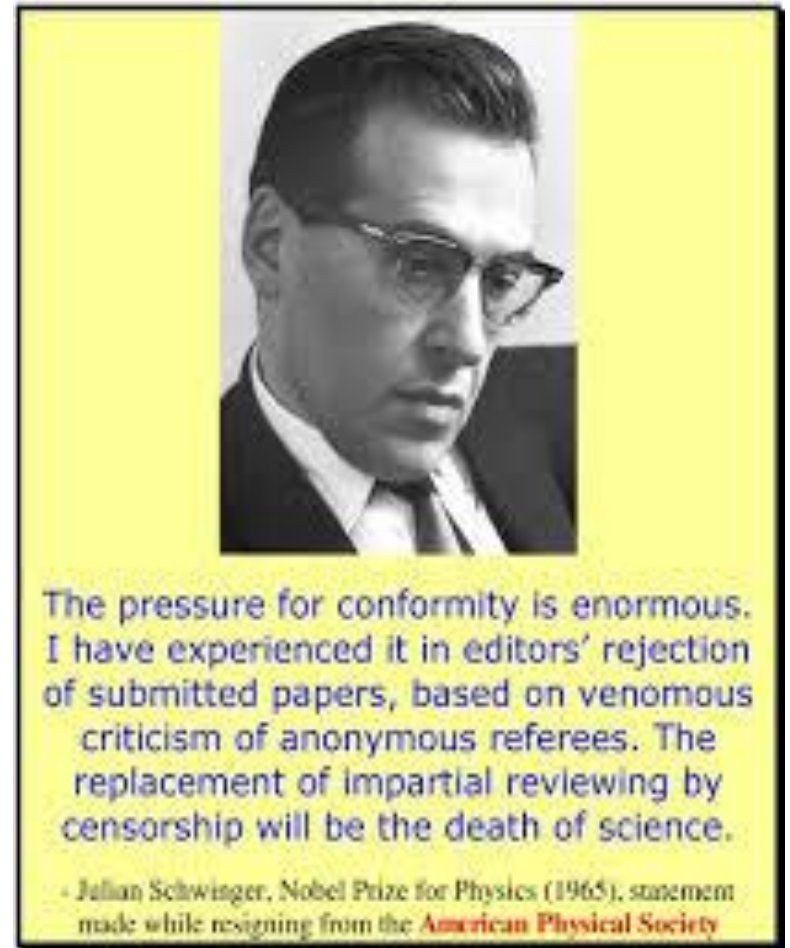
HOWEVER, is the Coulomb barrier that huge in the lattice ?

Willis Eugene *Lamb*
Nobel Prize 1955



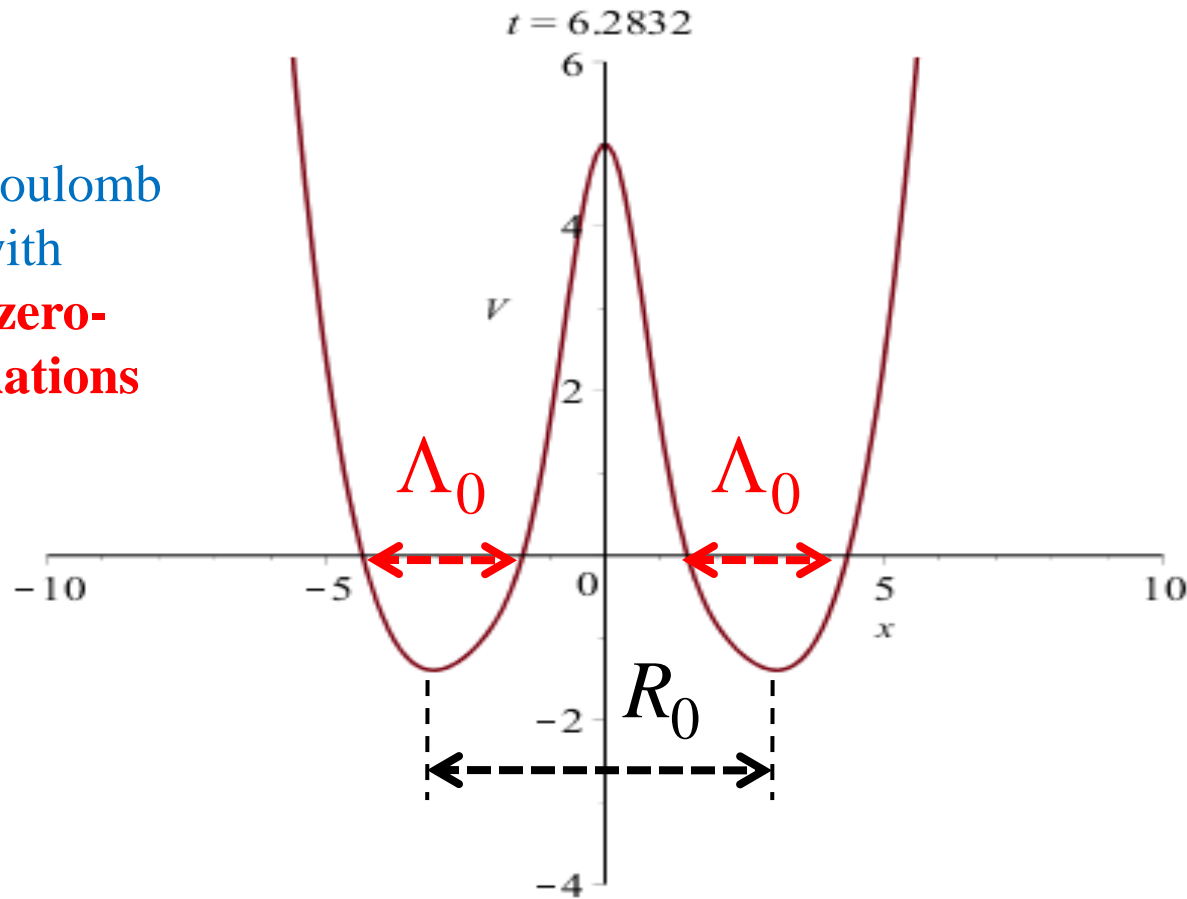
R.H. Parmenter, **W.E. Lamb**,
Cold fusion in Metals (1989)
Electron screening

Julian Schwinger
Nobel Prize 1965



J. Schwinger, **Nuclear Energy in an Atomic Lattice (1990)**
Lattice screening

Effective Coulomb
repulsion with
account of **zero-**
point oscillations



$$\langle V_c(r) \rangle_0 = \frac{e^2}{r} \sqrt{\frac{2}{\pi}} \int_0^{r/\Lambda_0} dx \exp\left(-\frac{1}{2}x^2\right) \approx \begin{cases} r \gg \Lambda_0 : \frac{e^2}{r} \\ r \ll \Lambda_0 : \left(\frac{2}{\pi}\right)^{1/2} \frac{e^2}{\Lambda_0} \sim 100 \text{ eV} (!!!) \end{cases}$$

J. Schwinger, *Nuclear Energy in an Atomic Lattice* The First Annual Conference on Cold Fusion. University of Utah Research Park, Salt Lake City (**1990**)

D-D fusion rate in Pd-D lattice: $\nu_{D-D} = \frac{1}{T_0} = (2\pi/\hbar)_0 \langle V \delta(H - E) V \rangle_0$

T_0 is the mean lifetime of the *phonon vacuum* state before releasing the nuclear energy **directly** to the lattice (**no radiation!**):

$$\frac{1}{T_0} \approx 2\pi\omega_0 \left(\frac{2\pi\hbar\omega_0}{E_{nucl}} \right)^{\frac{1}{2}} \left(\frac{r_{nucl}}{\Lambda_0} \right)^3 \exp \left[-\frac{1}{2} \left(\frac{R_0}{\Lambda_0} \right)^2 \right] \sim 10^{-19} s^{-1} \div 10^{-30} s^{-1}$$

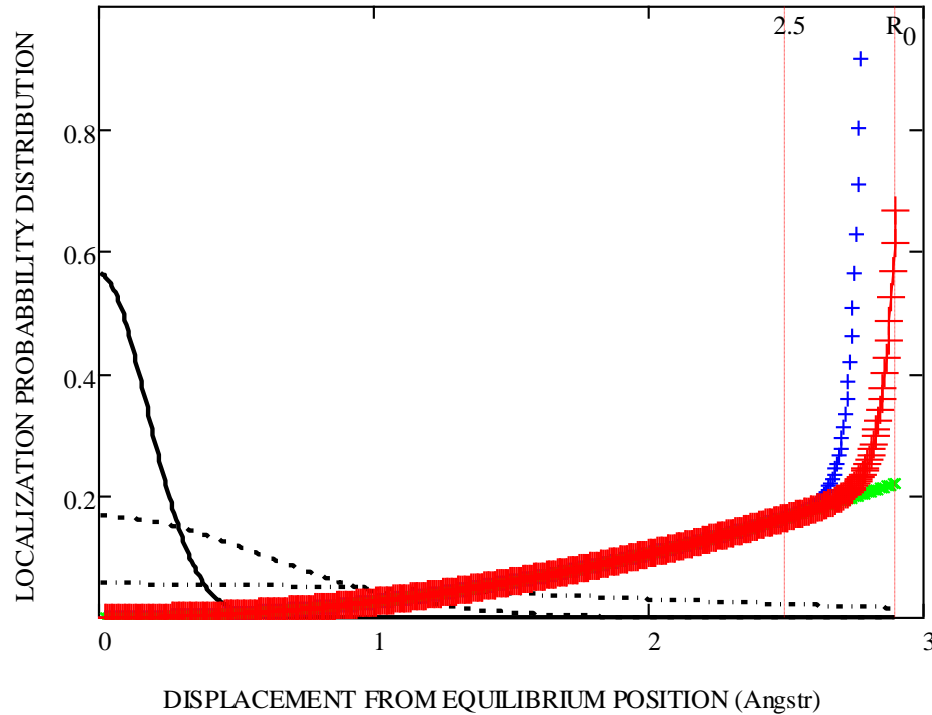
$\Lambda_0 = 0.1 \text{ \AA}$

$R_0 = 0.94 \text{ \AA} \div 2.9 \text{ \AA}$

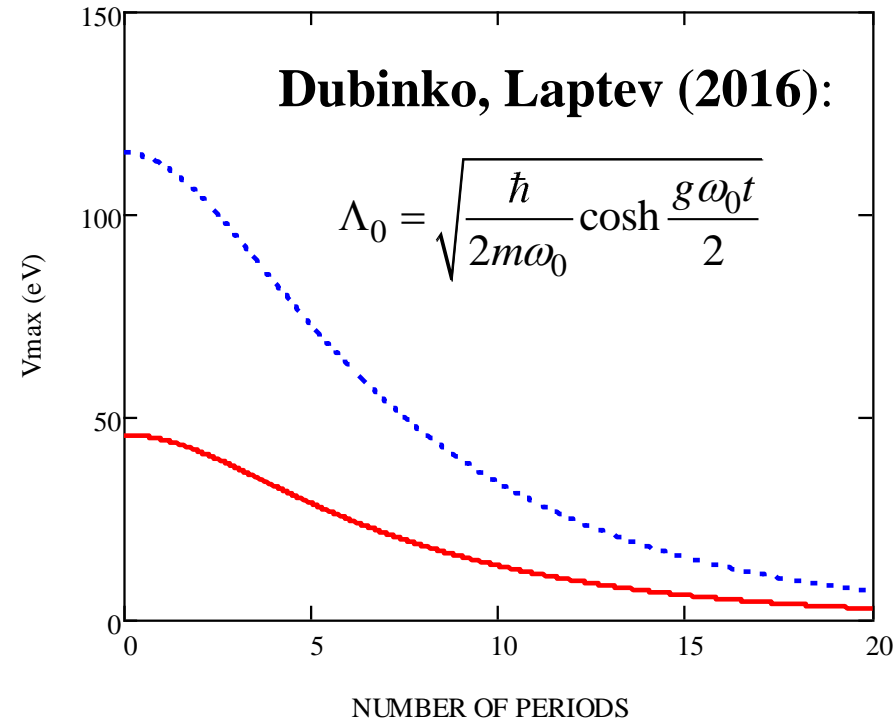
Schwinger, ***Nuclear Energy in an Atomic Lattice*** I, Z. Phys. D 15, 221 (1990).

Parmenter, Lamb, ***Cold fusion in Metals***, Proc. Natl. Acad. Sci. USA, v. 86, 8614-8617 (1989).

$$V_{eff}(r) \approx \frac{m\omega_0^2}{2} r^2 + \frac{e^2}{R_0 - r} \exp\left(-\frac{R_0 - r}{\lambda_D}\right) \sqrt{\frac{2}{\pi}} \int_0^{(R_0 - r)/\Lambda_0} dx \exp\left(-\frac{1}{2} x^2\right)$$



- N=0
- - - N=10
- · - · N=17
- +++ Effective potential (x10 eV) by eq. (44) [P&L]
- x x x Harmonic potential (x10 eV)
- + + + Effective potential (x10 eV) at N=17 by eq. (45) [Schwinger]

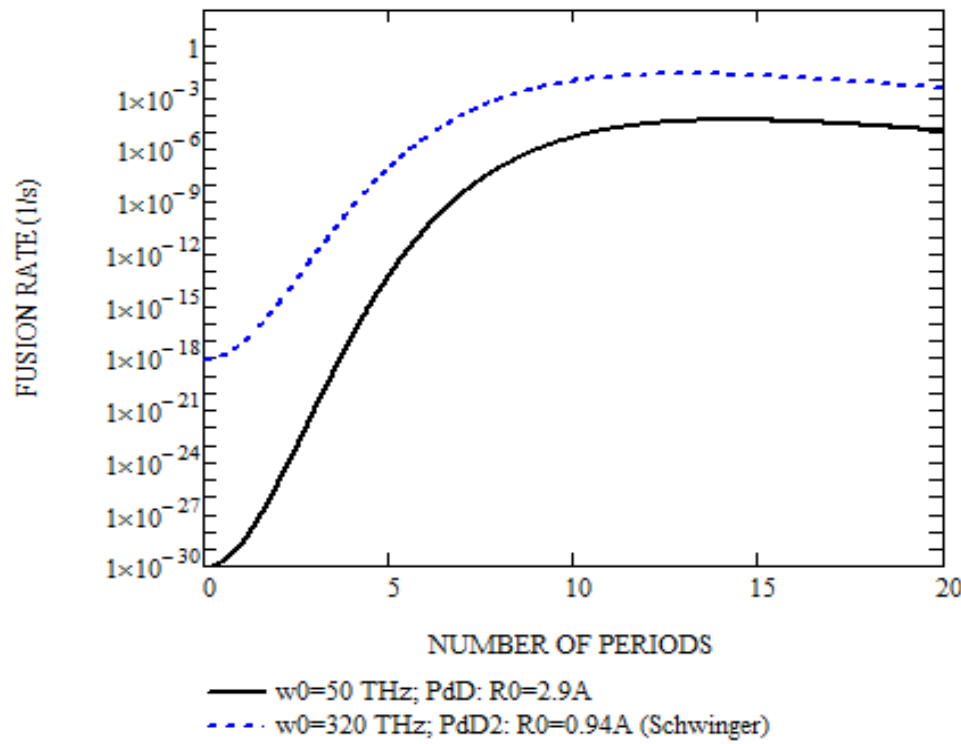
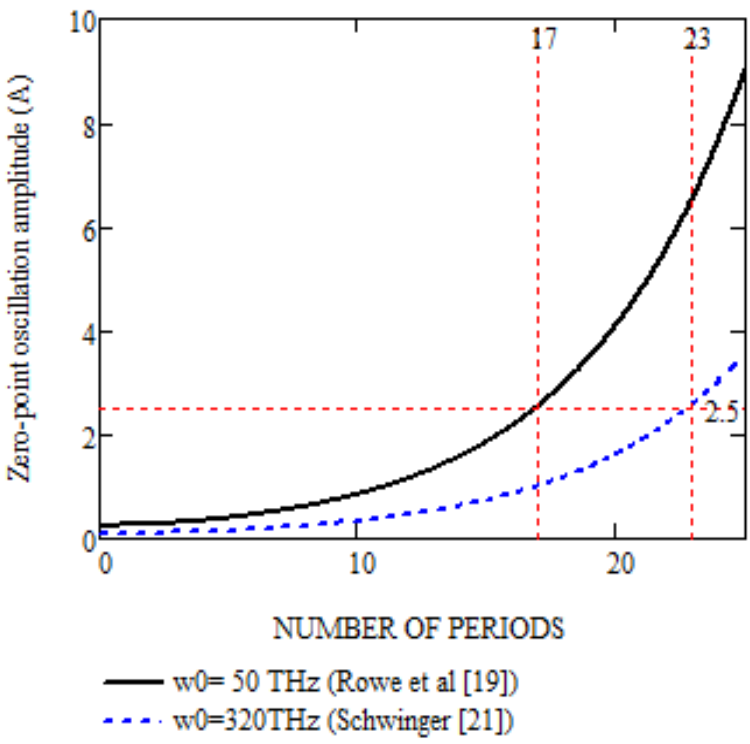


- w₀=50 THz (Rowe et al [19])
- · - · w₀=320 THz (Schwinger [21])

Schwinger, *Nuclear energy in an atomic lattice*. Proc. Cold Fusion Conf. (1990)
Dubinko, Laptev, *Chemical and nuclear catalysis driven by LAVs*, LetMat (2016)

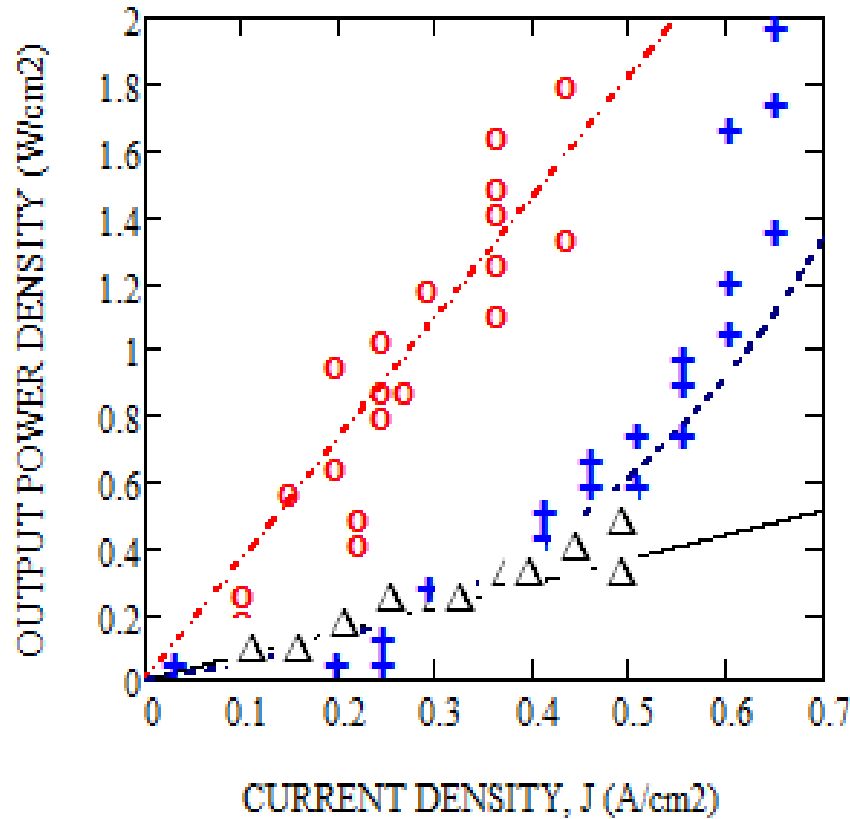
$$\frac{1}{T} \approx 2\pi\omega_0 \left(\frac{2\pi\hbar\omega_0}{E_{nucl}} \right)^{\frac{1}{2}} \left(\frac{r_{nucl}}{\Lambda} \right)^3 \exp \left[-\frac{1}{2} \left(\frac{R_0}{\Lambda_0} \right)^2 \right]$$

$\Lambda_0 = \left\{ \begin{array}{l} \sqrt{\frac{\hbar}{2m\omega_0}} = const \\ \sqrt{\frac{\hbar}{2m\omega_0} \cosh \frac{g\omega_0 t}{2}} \end{array} \right.$



LENR power density under D₂O electrolysis

$$P_{D-D}(T, J) = K_{DB}^J(E_{DB}^*, T, J) E_{D-D}$$



Parameter	Table 1	Value
D-D equilibrium spacing in PdD, b (Å)		2.9
DB excitation efficiency, k_{eff}		10^{-10}
Fusion energy, (MeV)		23.8
Mean DB energy, (eV)		1
DB oscillation frequency, ω_{DB} (THz)		20
Critical DB lifetime, τ_{DB} (ps/cycles)		10/100
Quodon excitation energy (eV)		0.8
Quodon excitation time, τ_{ex} (ps/cycles)		1/10
Quodon propagation range, l_q (nm)		2.9
Cathod size/thickness (mm)		5

BNC can provide up to 10^{14}
“collisions” per cm³ per second

Where to look for
Nuclear Active Environment?

Small Energy Gap
is required for

LAV formation

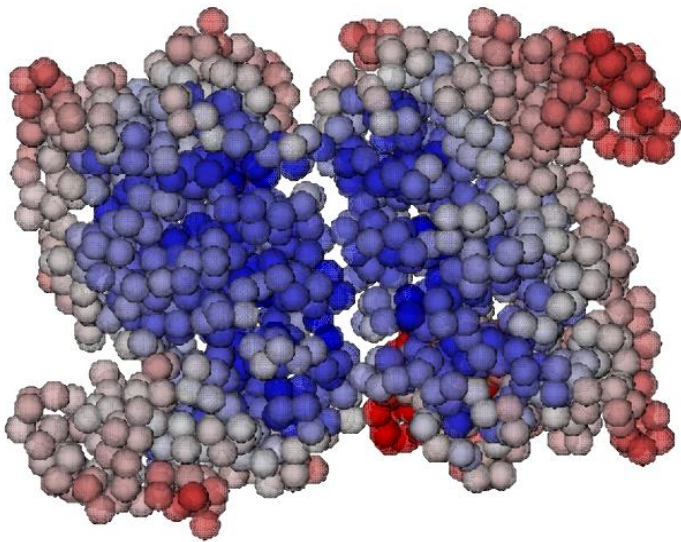


Nuclear Active Environment

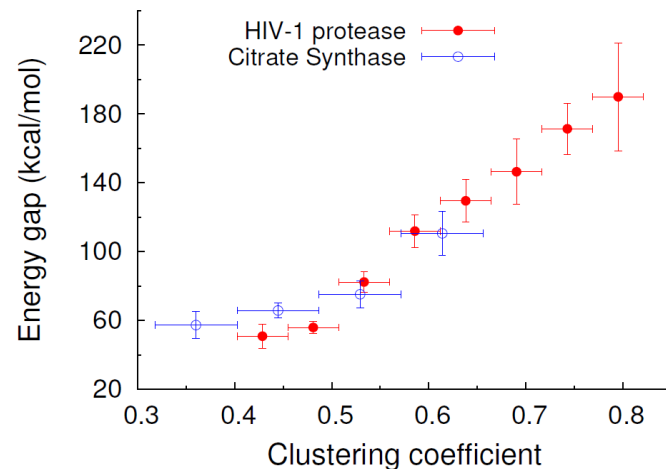
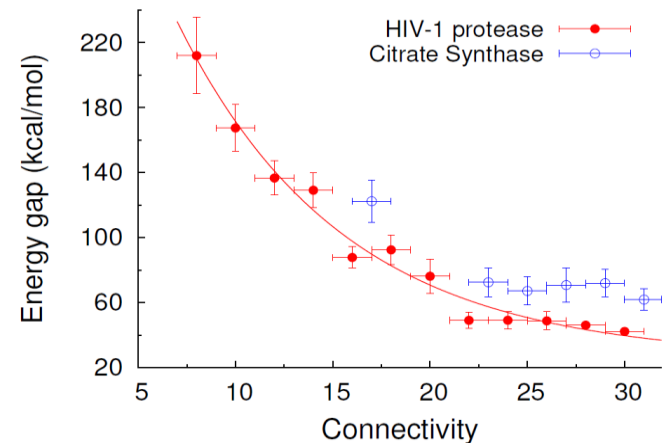
Chemical and Nuclear catalysis

the role of disorder

“Cracks and small particles are the Yin and Yang of the cold fusion environment” E. Storms

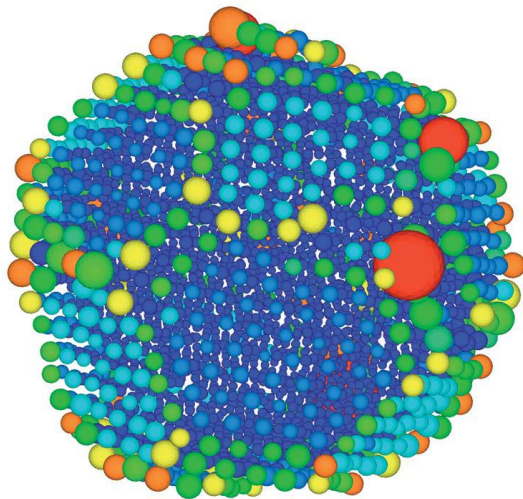
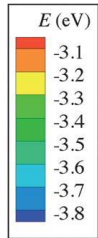


Structure of dimeric citrate synthase (PDB code 1IXE). Only α -carbons are shown, as spheres in a color scale corresponding to the crystallographic B-factors, from smaller (blue) to larger (red) fluctuations [Dubinko, Piazza, 2014]

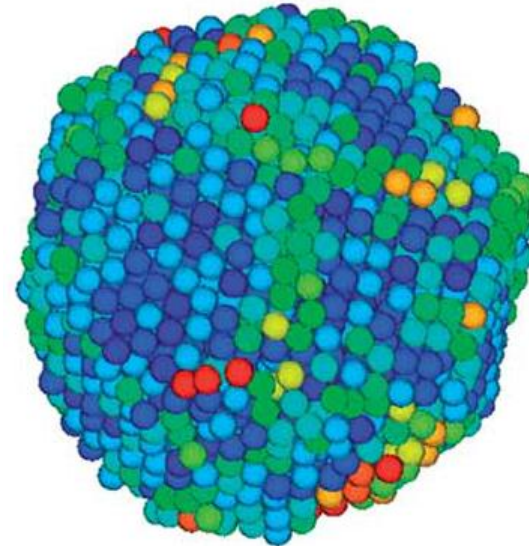


Chemical and Nuclear catalysis

Nickel nanoparticles, Zhang and Douglas (2013)

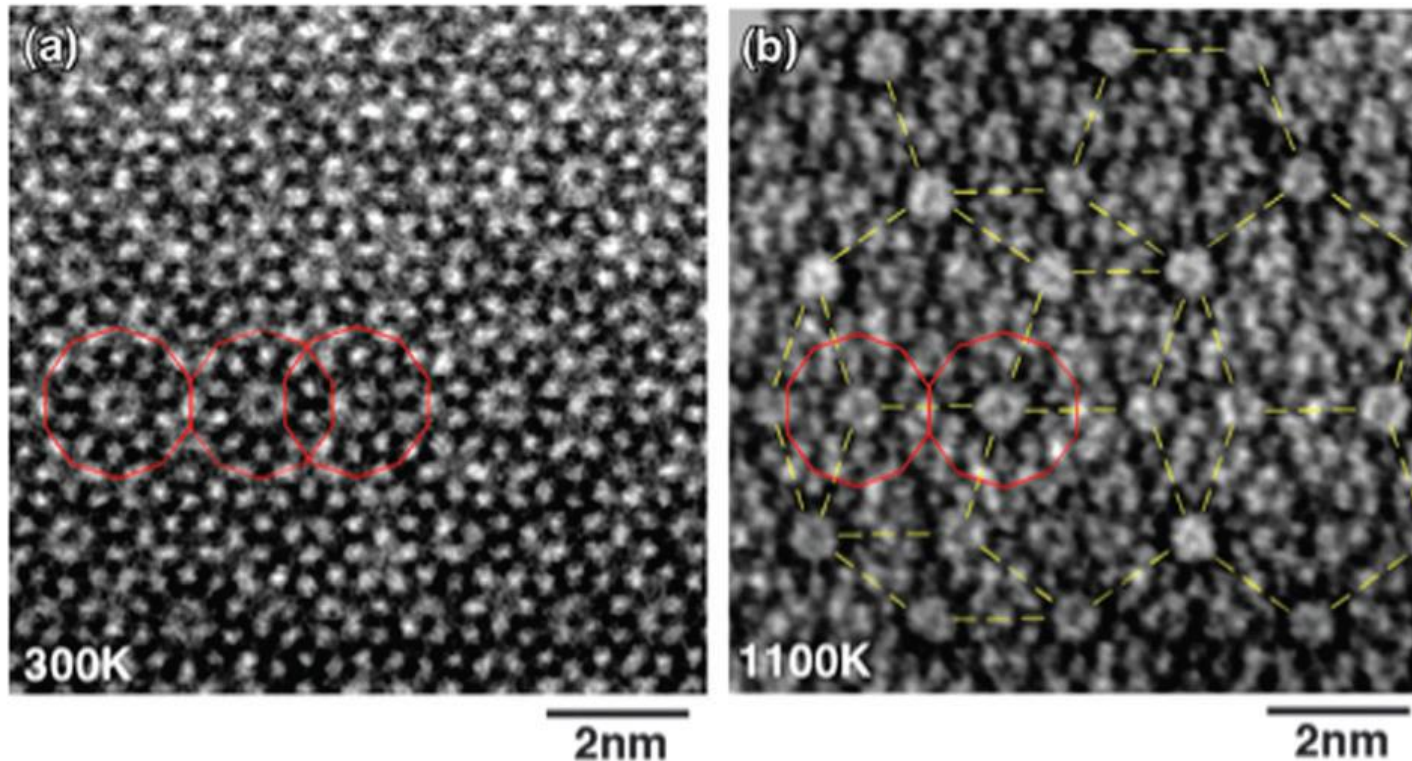


Atomic configuration of a Ni nanoparticle of 2899 atoms at $T = 1000$ K. The atoms are colored based on the potential energy and their size is proportional to Debye–Waller factor. Potential energy and DWF are time averaged over a 130 ps time window, corresponding to the time interval during which the strings show maximum length.

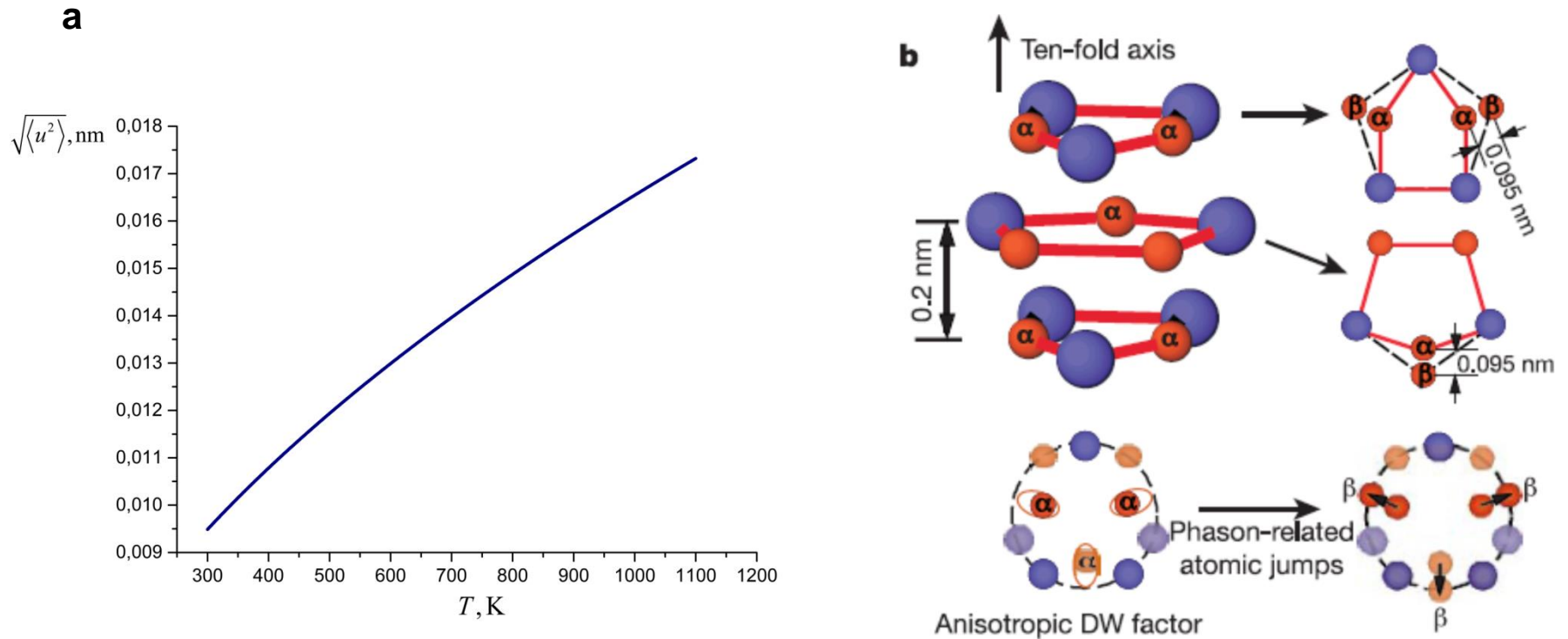


Map of the local Debye–Waller factor showing the heterogeneity of the atomic mobility at a temperature of 1450 K. Regions of high mobility string-like motion are concentrated in filamentary grain boundary like domains that separate regions having relatively strong short-range order.

E. Abe, S.J. Pennycook, A.P. Tsai, ***Direct observation of a local thermal vibration anomaly in a quasicrystal***, Nature (London) 421 (2003) 347-350



STEM images of LAVs of the decagonal $\text{Al}_{72}\text{Ni}_{20}\text{Co}_8$ at (a) 300 K and (b) 1100 K, according to Abe et al. Connecting the center of the 2 nm decagonal clusters (red) reveals significant temperature-dependent contrast changes, a pentagonal quasiperiodic lattice (yellow) with an edge length of 2 nm can be seen in (b).



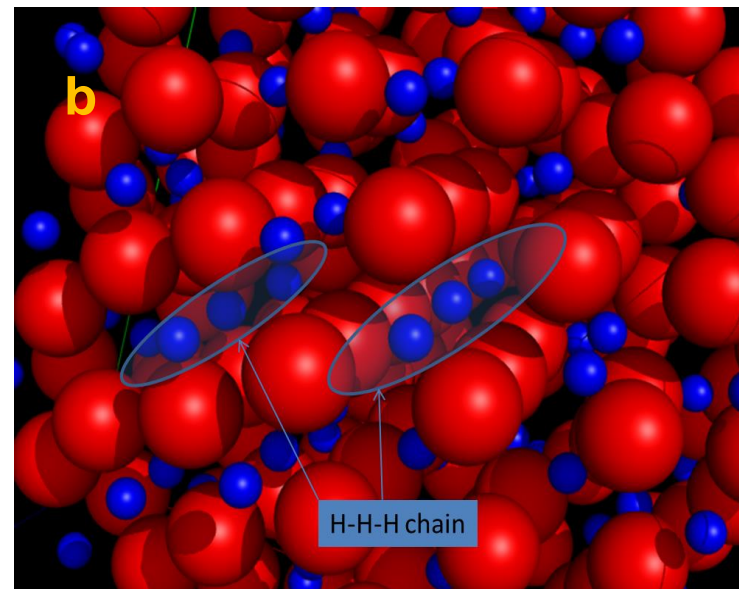
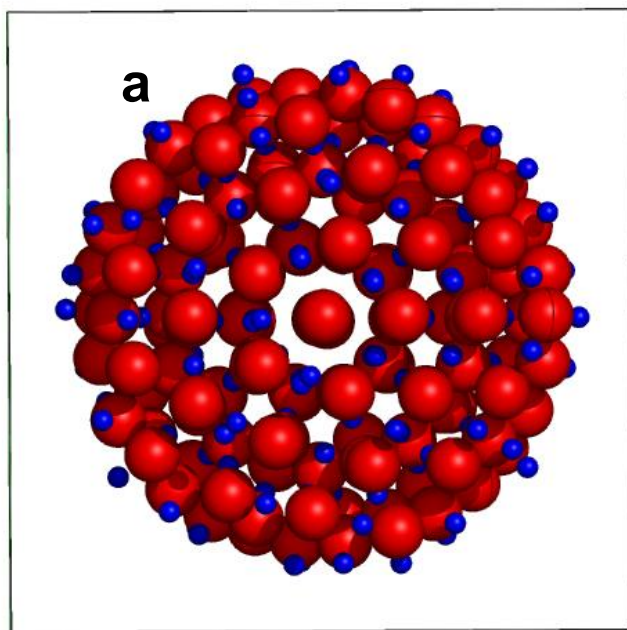
(a) **LAV amplitude** dependence on temperature in $\text{Al}_{72}\text{Ni}_{20}\text{Co}_8$, fitted by two points at 300 K and 1100 K, according to Abe et al. The maximum LAV amplitude at 1100K = 0.018 nm.

(b) **LAVs give rise to phasons** at $T > 990$ K, where a phase transition occurs, and additional quasi-stable sites β arise near the sites α . The phason amplitude of 0.095 nm is an order of magnitude larger than that of LAVs.

Chemical and Nuclear catalysis

DFT modeling of nanoclusters of Pd-H(D)

Terentyev, Dubinko (2015)



(a) Structure of Pd-H cluster containing 147 Pd and 138 H atoms having minimum free energy configuration, replicated using the method and parameters by Calvo et al; **(b)** H-H-H chains in the nanocluster, which are viable sites for LAV excitation

Magic clusters are clusters of certain ("magic") sizes, which, due to their specific structure, have increased stability compared to clusters of other sizes.

In **icosahedral clusters**, each “k” layer consists of $10k^2+2$ atoms.

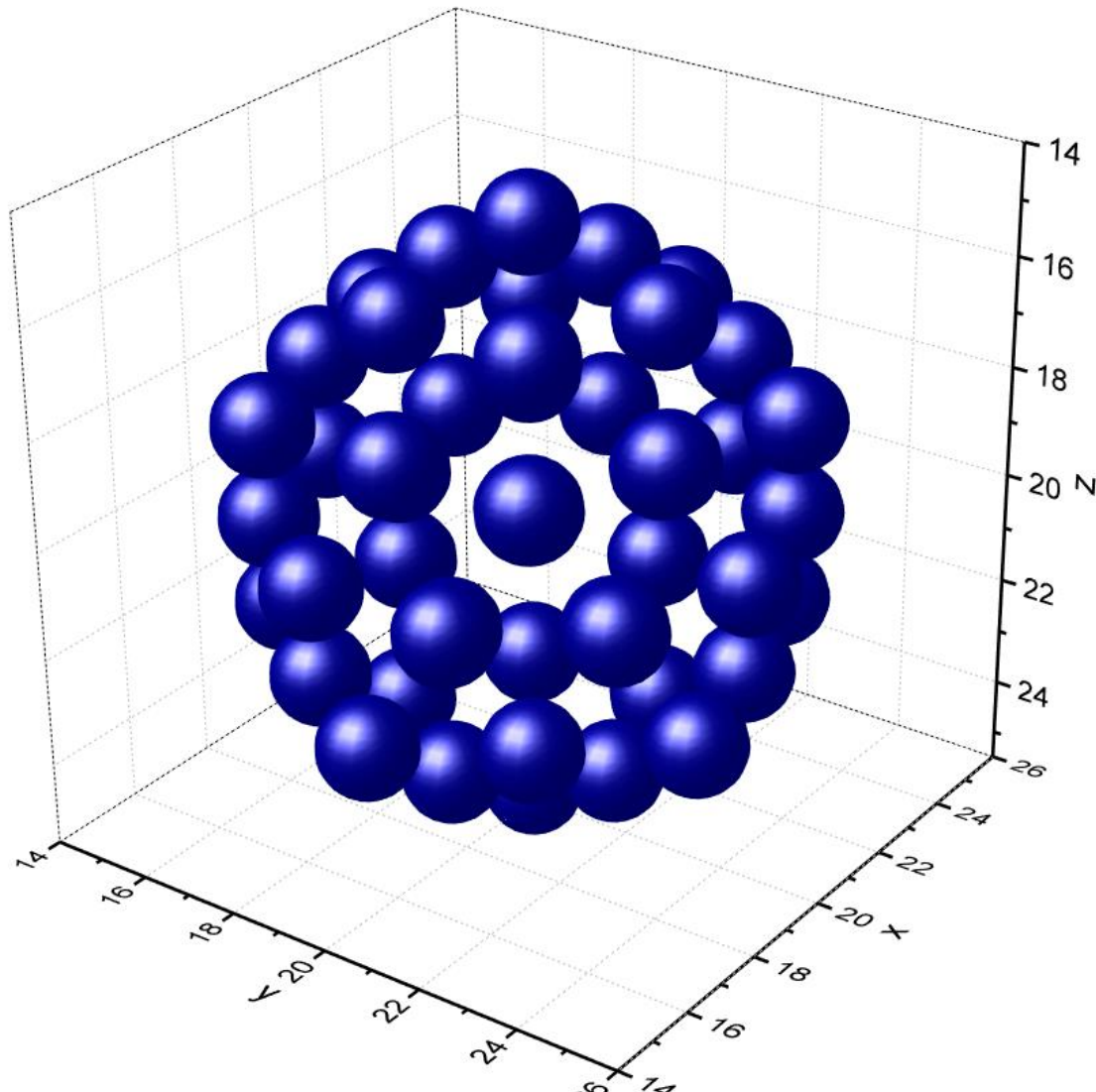
So the total number of atoms in a cluster with “N” layers is given by

$$n = (2N + 1) + 10 \sum_{k=1}^N k^2$$

$$n = 13, 55, 147, 309, 561 \quad \text{for } N=1, 2, 3, 4, 5$$

Magic icosahedral cluster of 55 Pd atoms

Consider a cluster of 55 Pd atoms with **quasicrystalline** 5th order symmetry axis.



Icosahedral cluster of 55 Pd atoms

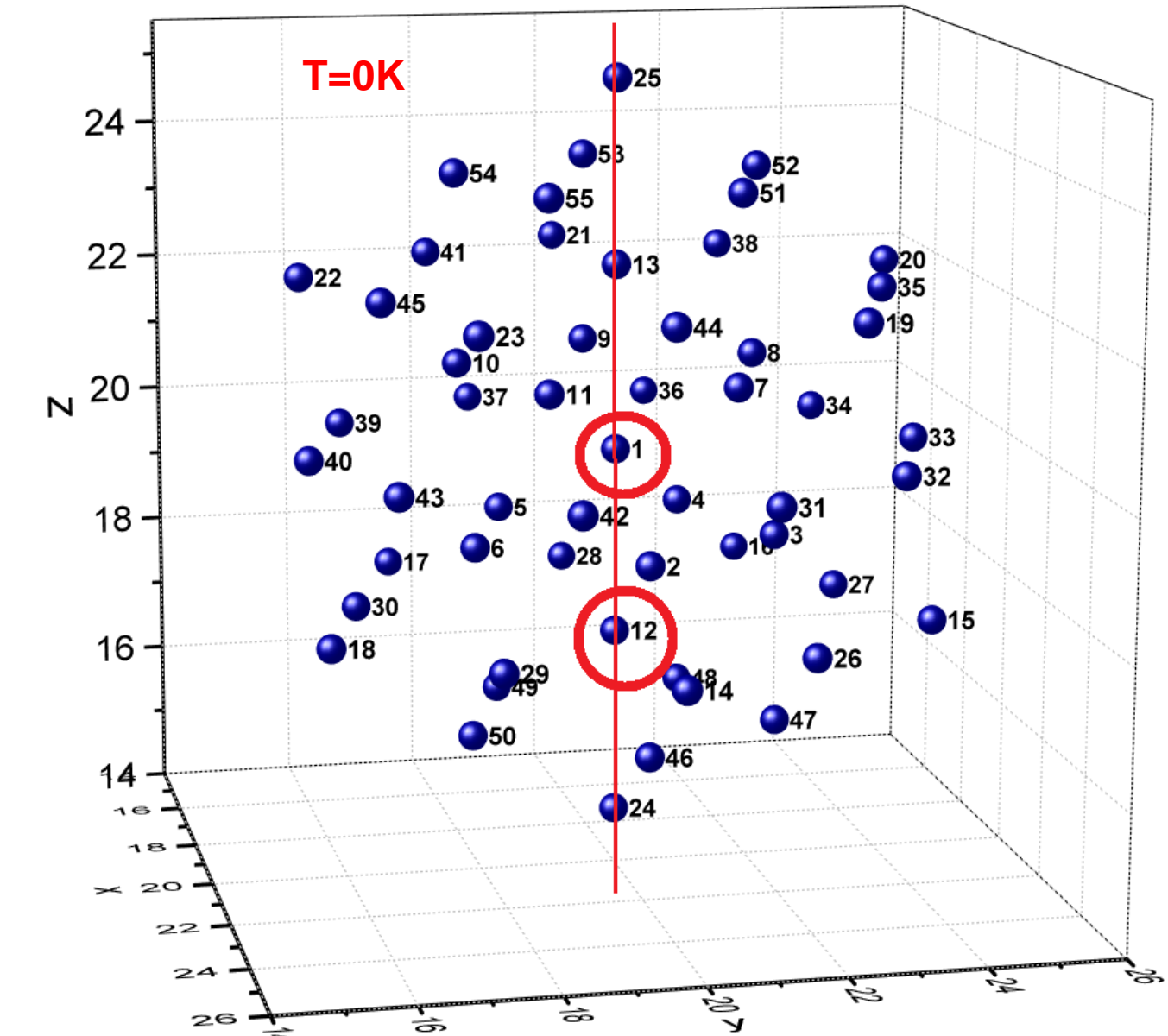
Initial conditions:

at the initial time
moment all
particles have zero
displacements
from equilibrium
positions.

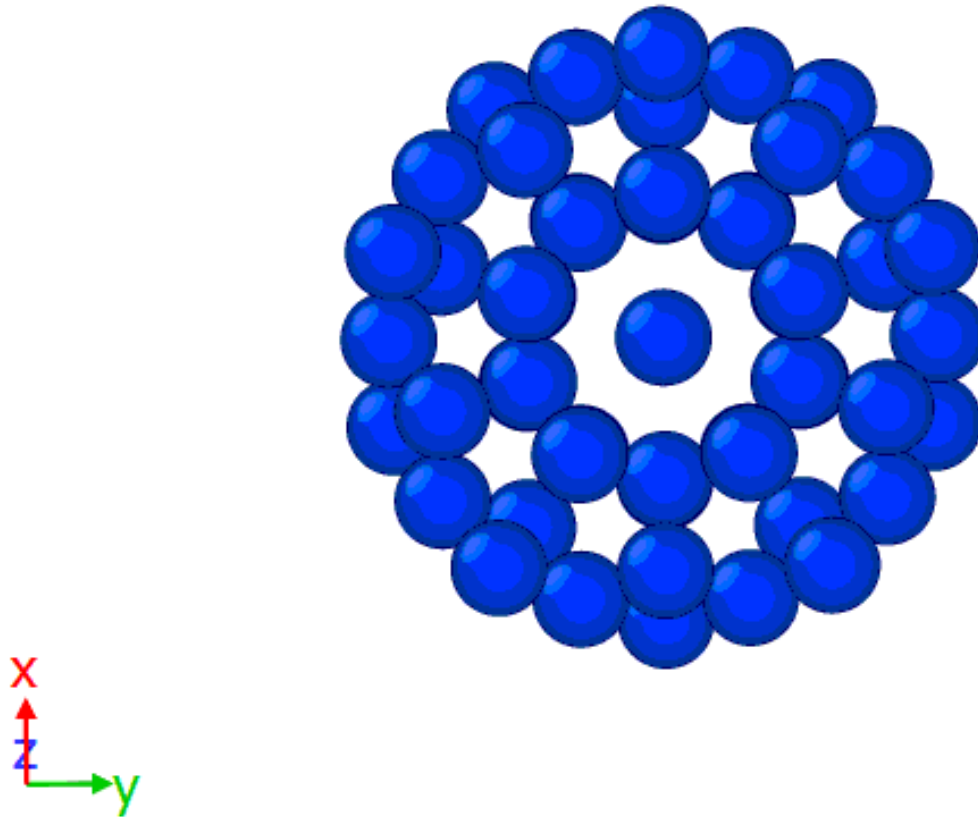
Atom #1 has initial
kinetic energy
1.5eV in [00-1]
direction.

Atom #12 has
initial kinetic
energy **1.5eV** in
[001] direction

Boundary
conditions: free
surfaces of cluster

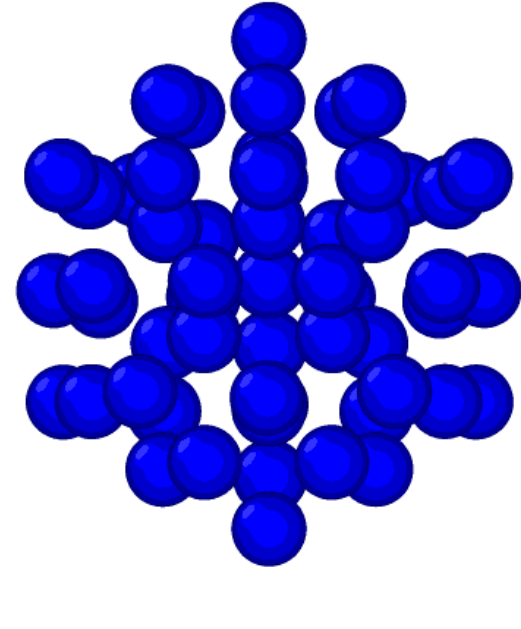
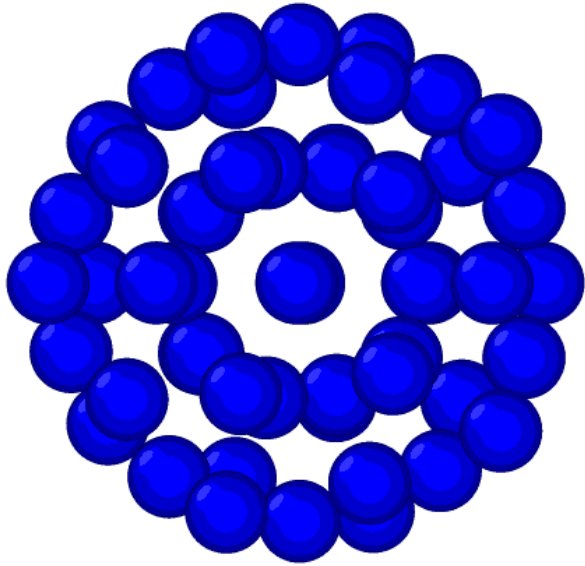


Dynamics of the icosahedral cluster of 55 Pd atoms



It is seen from the visualization, that Localized Anharmonic Vibration is generated. The observed LAV in the atomic cluster represents the coherent collective oscillations of Pd atoms along quasi-crystalline symmetry directions.

Dynamics of the Pd atomic cluster



If the initial energy, given to cluster is large enough (greater than the cohesive energy) then the cluster is destroyed after a certain period of time (\sim ps) .

Conclusions and outlook

New mechanism of chemical and nuclear catalysis in solids is proposed, based on **time-periodic driving** of the potential landscape induced by *emerging nonlinear phenomena*, such as LAVs or phasons.

The present mechanism explains the salient LENR requirements: (i, ii) **long initiation time and high loading of D** within the Pd lattice as preconditioning needed to prepare small PdD crystals, in which DBs can be excited more easily, and (iii, iv) the **triggering by D flux or electric current**, which facilitates the DB creation by the input energy transformed into the lattice vibrations.

The model (*under selected set of material parameters*) describes **quantitatively** the observed **exponential dependence on temperature and linear dependence on the electric (or ion) current**.

Atomistic modeling of LAVs and phasons in metal hydrides/deuterides is an important outstanding problem since it may offer ways of ***engineering the nuclear active environment***.

Publications

1. V.I. Dubinko, P.A. Selyshchev and F.R. Archilla, *Reaction-rate theory with account of the crystal anharmonicity*, **Phys. Rev. E** 83 (2011),041124-1-13
2. V.I. Dubinko, F. Piazza, *On the role of disorder in catalysis driven by discrete breathers*, **Letters on Materials** 4 (2014) 273-278.
3. V.I. Dubinko, *Low-energy Nuclear Reactions Driven by Discrete Breathers*, **J. Condensed Matter Nucl. Sci.**, 14, (2014) 87-107.
4. V.I. Dubinko, *Quantum tunneling in gap discrete breathers*, **Letters on Materials**, 5 (2015) 97-104.
5. V.I. Dubinko, *Quantum Tunneling in Breather ‘Nano-colliders’*, **J. Condensed Matter Nucl. Sci.**, 19, (2016) 1-12.
6. V. I. Dubinko, D. V. Laptev, *Chemical and nuclear catalysis driven by localized anharmonic vibrations*, **Letters on Materials** 6 (2016) 16–21.
7. V. I. Dubinko, *Radiation-induced catalysis of low energy nuclear reactions in solids*, **J. Micromechanics and Molecular Physics**, 1 (2016) 165006 -1-12.
8. V.I. Dubinko, O.M. Bovda, O.E. Dmitrenko, V.M. Borysenko, I.V. Kolodiy, *Peculiarities of hydrogen absorption by melt spun amorphous alloys Nd₉₀Fe₁₀*, *Vestnik KhNU* (2016).
9. V. Dubinko, D. Laptev, K. Irwin, *Catalytic mechanism of LENR in quasicrystals based on localized anharmonic vibrations and phasons*, **ICCF20**, <https://arxiv.org/abs/1609.06625>.

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**THANK YOU
FOR YOUR ATTENTION!**