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Module: Tensors

Author: Dominik Pabst

This module provides some tools for handling tensors for the module VorominkEstimation

A tensor of rank r is a linear mapping T , which takes r vectors from \mathbb{R}^d .

A symmetric tensor T is determined by the values $T(e_{i_1}, \dots, e_{i_r})$, where

$1 \leq i_1 \leq \dots \leq i_r \leq d$ and e_i is the i -th standard vector in \mathbb{R}^d .

In this code a tensor is represented by a dictionary, which has a key (i_1, \dots, i_r) for each choice of i_1, \dots, i_r .

For example the value corresponding to the key $(1, 1, 2)$ represents $T(e_1, e_1, e_2)$.

Modules

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Functions

Tvoronoi_measure(in_data, eta, R, res, r, s)

Estimates the Voronoi tensors with rank parameters r, s of the input data for different radii

Args:

in_data (numpy.ndarray): Input data
eta (list): Grid process (entries are the individual points)
R (list): Entries are the radii, for which the Voronoi tensor is estimated
res (float): Resolution of the grid process (compare Tools.grid_process)
r, s (int): Rank parameters of the tensors, that will be estimated

Returns:

list: Entries are the estimated Voronoi tensors. Therefore the list has the same length as the input R.

Tvoronoi_measure_1(in_data, eta, R, res, r, s)

Help function for Tvoronoi_measure

Tvoronoi_measure_2(in_data, eta, R, res, r, s)

Help function for Tvoronoi_measure

emptyTensor(dim, rank, LIST=False)

Creates an empty tensor (a tensor whose entries are all zero)

Args:

dim (int): Dimension of the tensor (Minkowski tensor of a set in \mathbb{R}^d has dimension d)
rank (int): Rank of the tensor (Minkowski or Voronoi tensor with rank parameters r, s has rank $r+s$)
LIST (boolean, optional): If True the entries of the tensor are not 0, but empty lists.
Can be used to bundle several tensors.

Returns:

dict: Empty tensor

evaluate(T, x)

Computes the values of a tensor at a given argument

Args:

T (dict): Tensor, which shall be evaluated
x (list): Entries are points in \mathbb{R}^d , where d is the dimension of t . Length has to be the rank of T .

Returns:

float: Computed value

get_tensors(V, R, dim, r, s)

Computes the Minkowski tensors from the Voronoi tensors by solving a Least Squares Problem

Args:

V (list): Entries are the Voronoi tensors (size should be at least $\dim+1$)

R (list): Corresponding radii to the Voronoi tensors in **V**
dim (int): Dimension of the set (resp. the data) for which the Voronoi tensors are given
r,s (int): Rank parameters of the Voronoi tensors

Returns:

list: Entries are the computed Minkowski tensors Φ_d, \dots, Φ_0 (in this order)

perm2(n)

Help function for Tvoronoi_measure

tensorproduct1(x, y, e, r, s)

Help function for Tvoronoi_measure

tensorproduct2(x, y, e, r, s)

Help function for Tvoronoi_measure

tensorsum1(dist, ind, in_data, eta, r, s, R)

Help function for Tvoronoi_measure

tensorsum2(dist, ind, in_data, eta, r, s, R)

Help function for Tvoronoi_measure

Data

gamma = <ufunc 'gamma'>